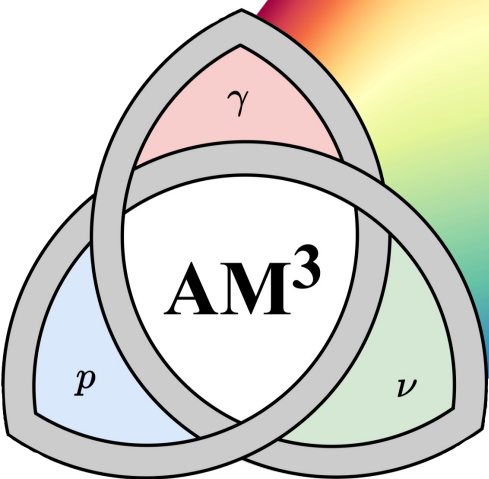


# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies



M. Klinger-Plaisier, 26.02.2025

*Workshop on Numerical Multi Messenger Modelling*

in collaboration with A. M. Taylor, W. Winter, C. Yuan, X. Rodrigues, A. Rudolph,  
S. Gao, G. Fichet de Clairfontaine, A. Fedynitch, M. Pohl

<https://maklinger.github.io/> - [m.klinger@uva.nl](mailto:m.klinger@uva.nl)



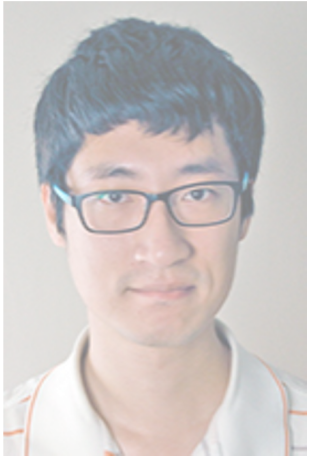
**HELMHOLTZ**  
HELMHOLTZ WEIZMANN  
RESEARCH SCHOOL  
MULTIMESSENGER ASTRONOMY



UNIVERSITEIT VAN AMSTERDAM

ANTON PANNEKOEK  
INSTITUUT

# The AM<sup>3</sup> Team



Gao



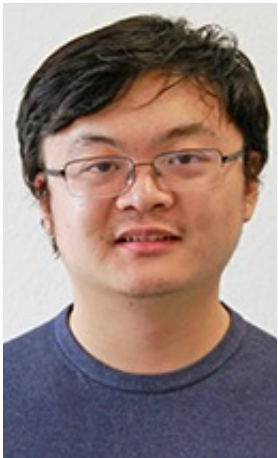
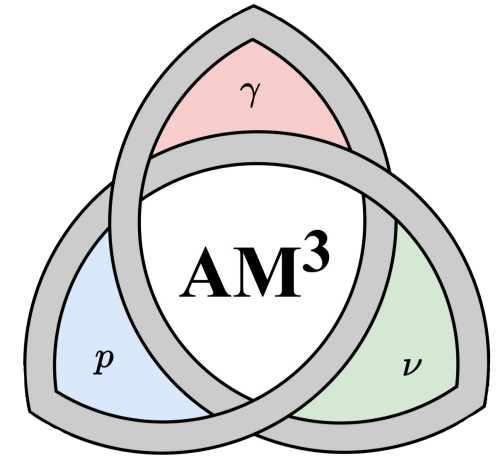
Klinger-Plaisier



Rudolph



Rodrigues



Yuan



Fichet De Clairfontaine



Fedynitch



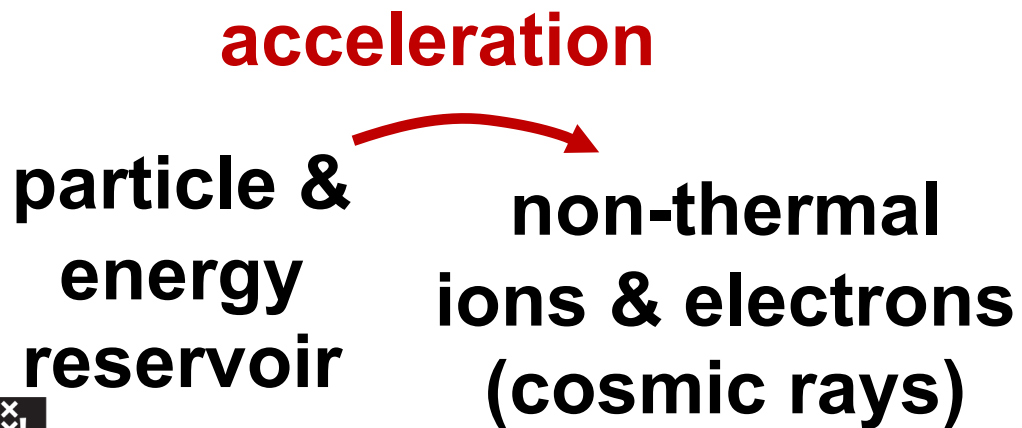
Winter



Pohl

# **AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies**

# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies



# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies

where? → GRB afterglow

how? → relativistic shock,  
but how exactly?

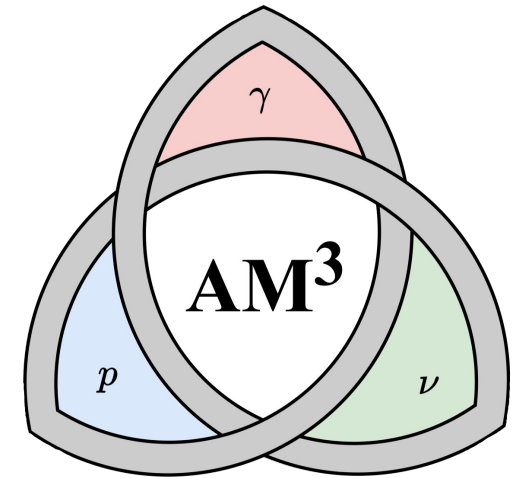
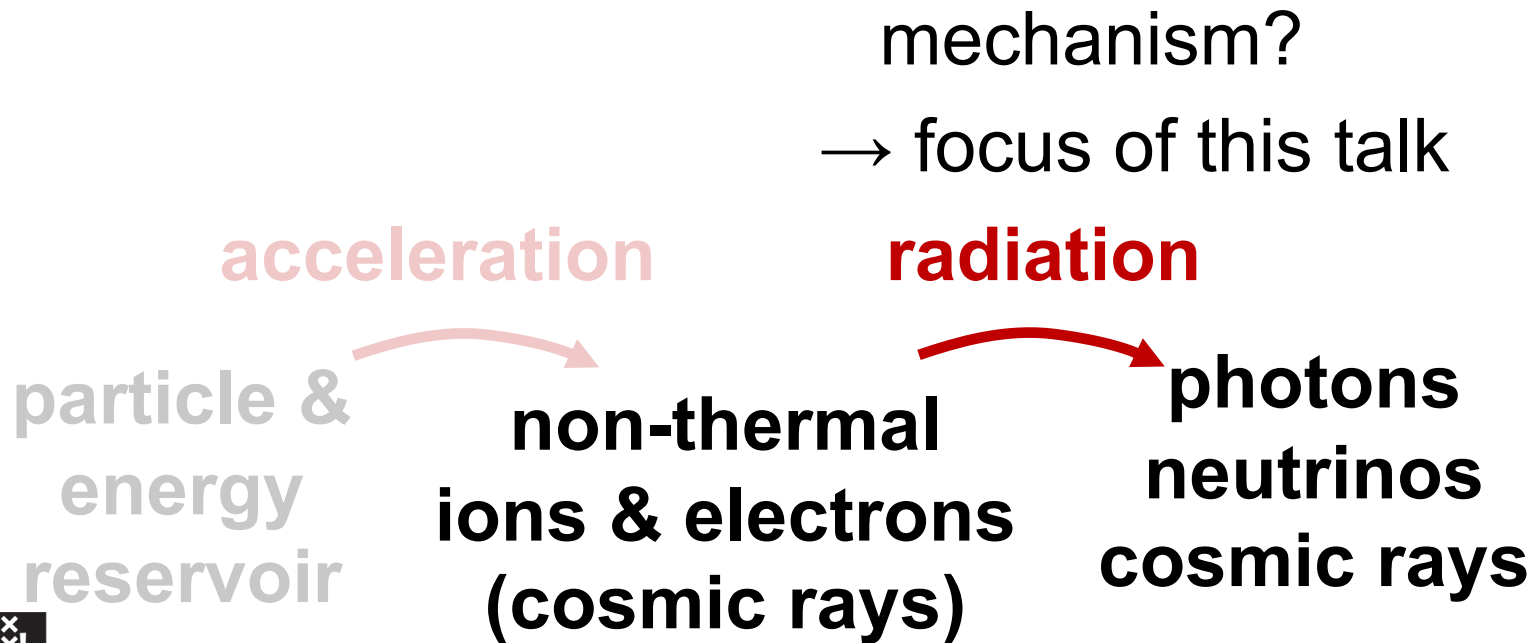
**acceleration**

**particle &  
energy  
reservoir**

**non-thermal  
ions & electrons  
(cosmic rays)**

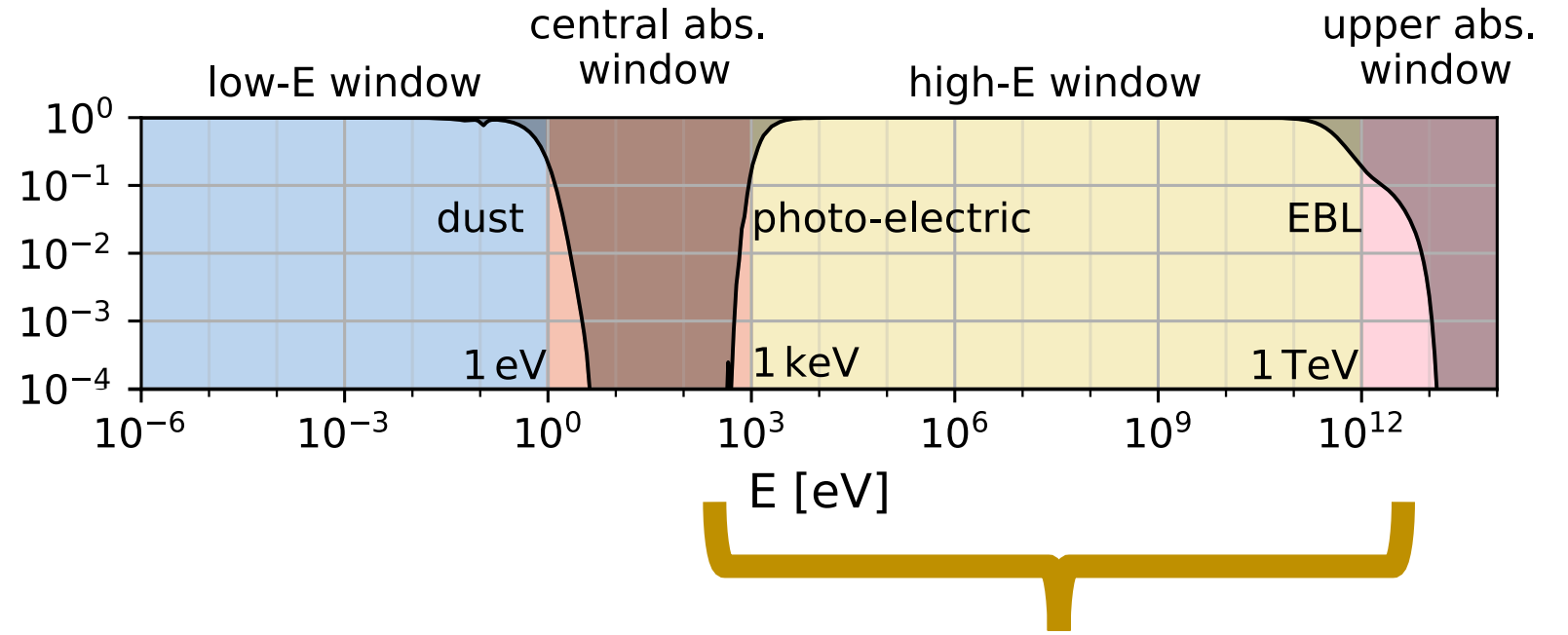


# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies

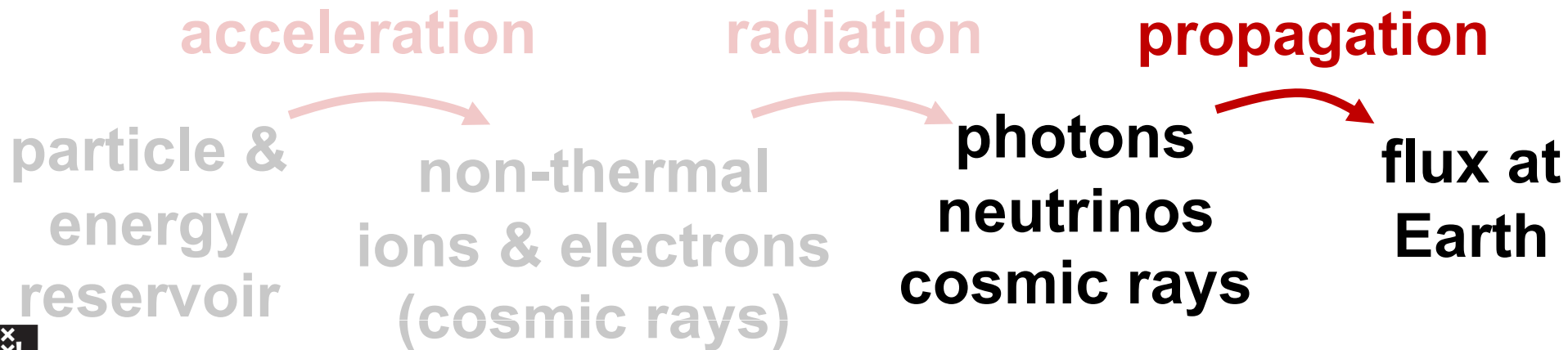


# photons:

absorption factor  $e^{-\tau(E)}$

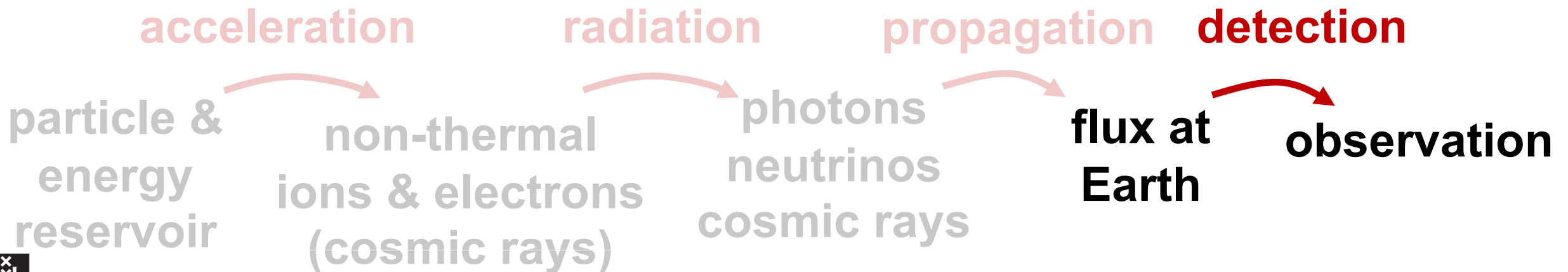


→ keV–TeV window



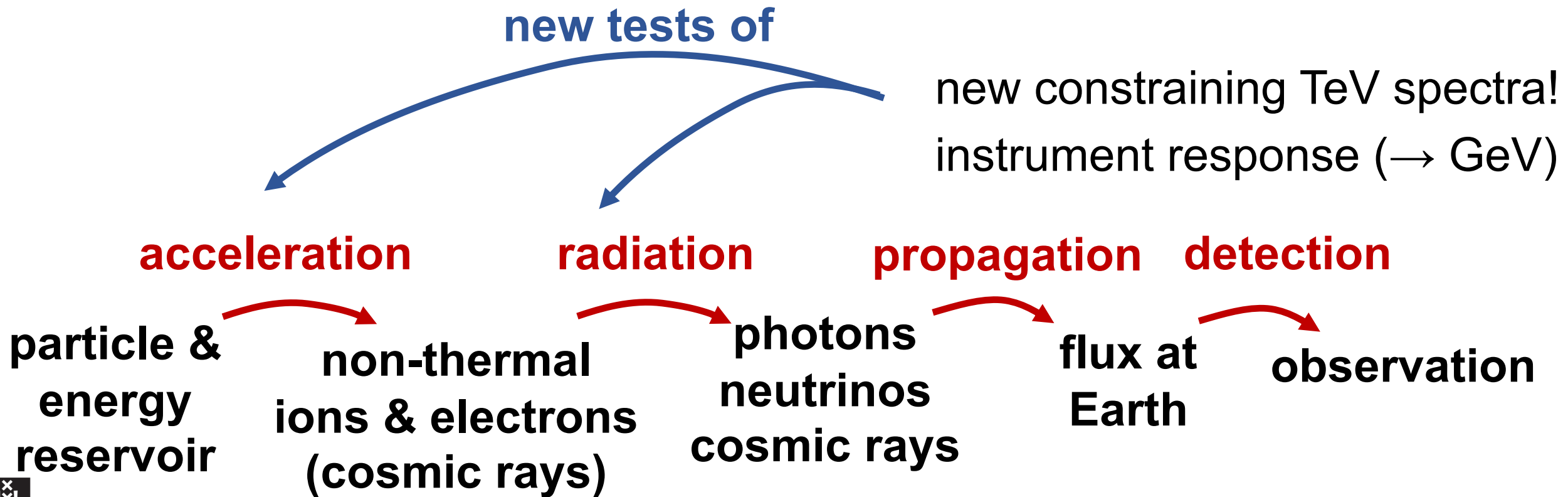
# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies

new constraining TeV spectra!  
instrument response ( $\rightarrow$  GeV)

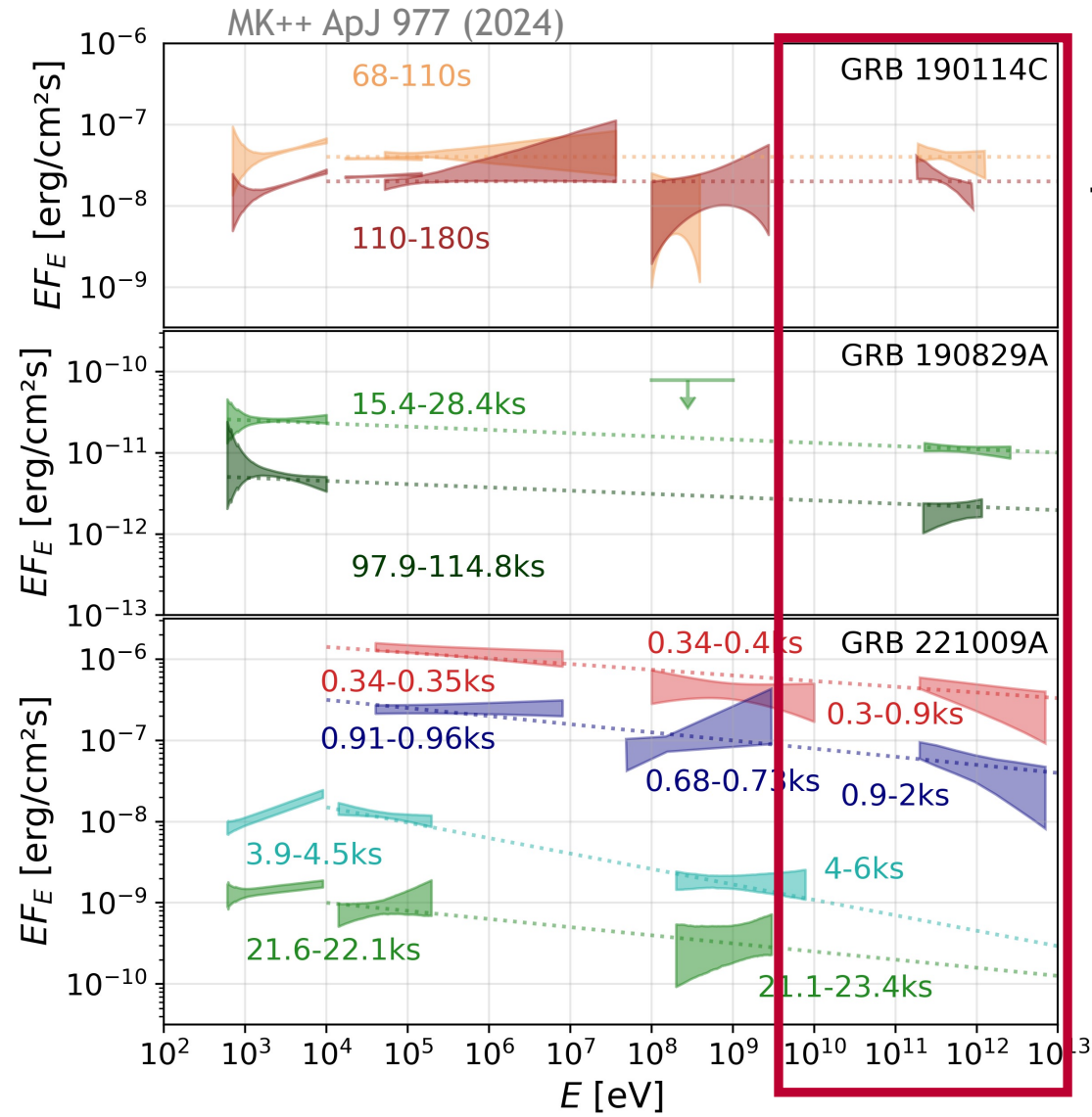




# AM<sup>3</sup> and Lepto-Hadronic Gamma-ray Burst Afterglow Spectra up to TeV Energies



# GRB afterglows detected at VHE!



→ **MAGIC**

very early (~100s)

→ **H.E.S.S.**

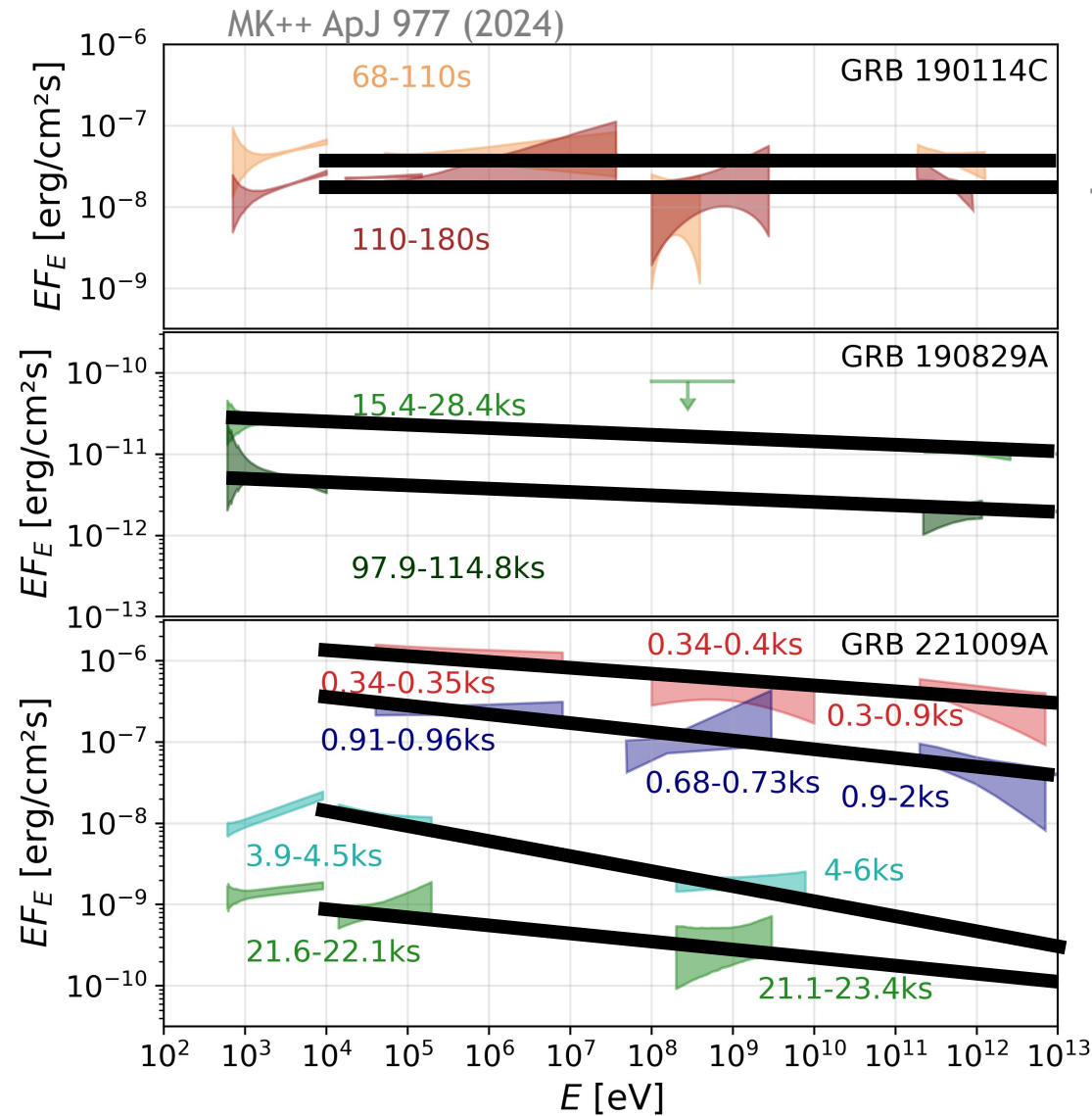
very close (z~0.08)

→ **LHAASO**

very bright (BOAT)

data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
 Liu++ APJL 943 (2023)  
 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)

# GRB afterglows detected at VHE!



→ MAGIC

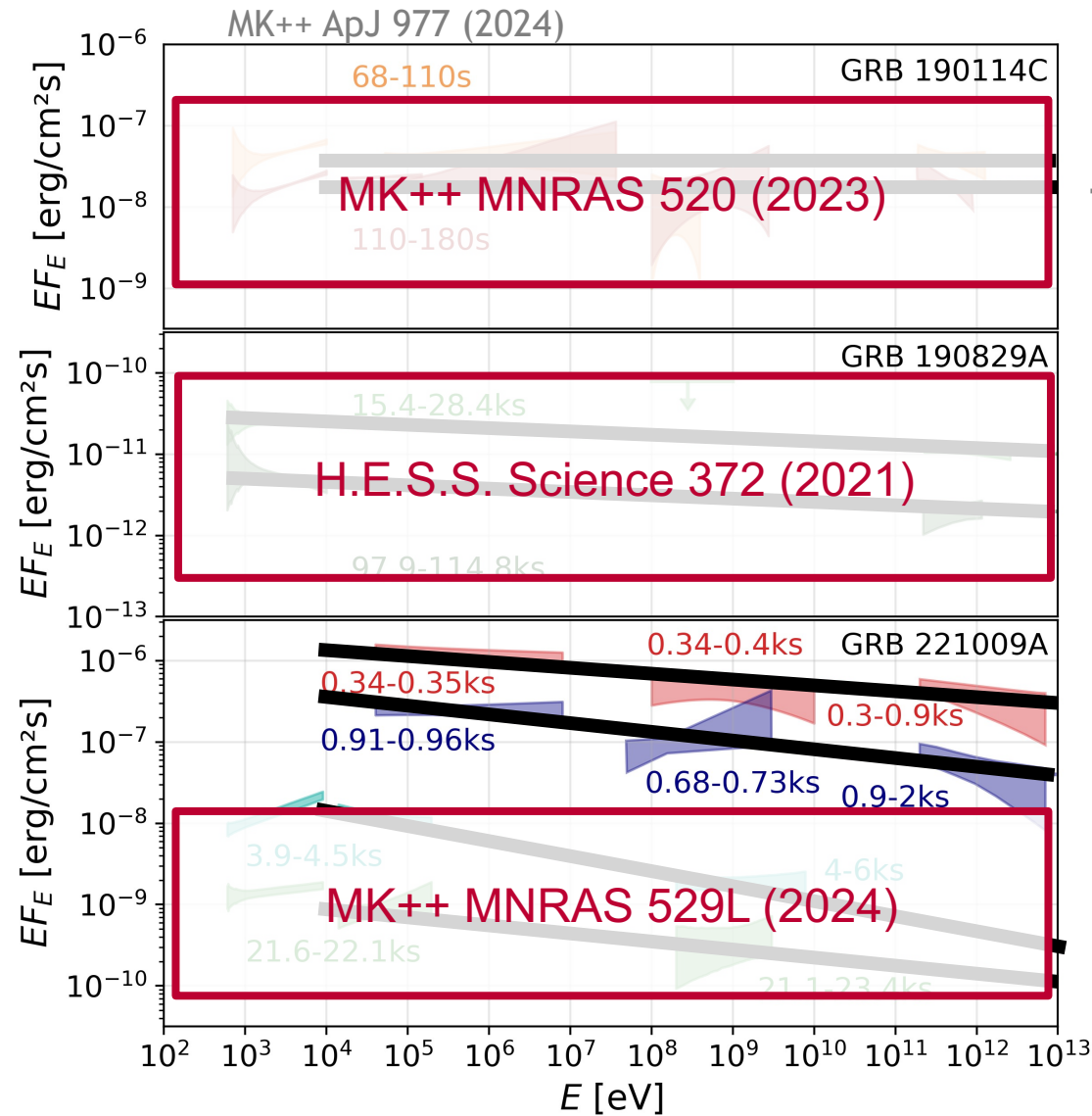
- Flat power-law spectra extending up to >TeV
- Single component?

→ H.E.S.S.

→ LHAASO

data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
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# GRB afterglows detected at VHE!



→ MAGIC

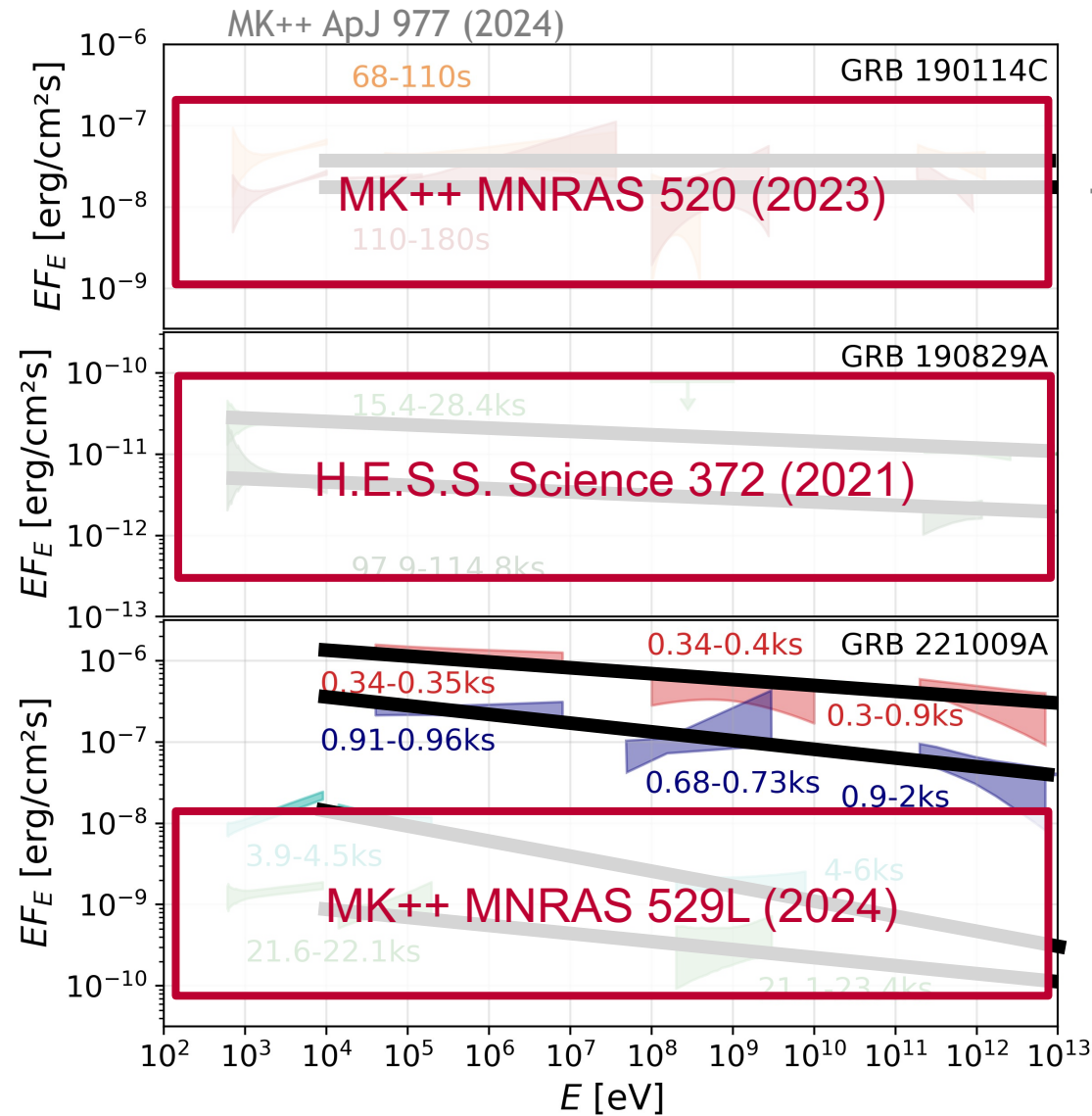
→ H.E.S.S.

→ LHAASO

- Flat power-law spectra extending up to >TeV
- Single component?
- **No preference at counts-level**

data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
 Liu++ APJL 943 (2023)  
 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)

# GRB afterglows detected at VHE!



→ MAGIC

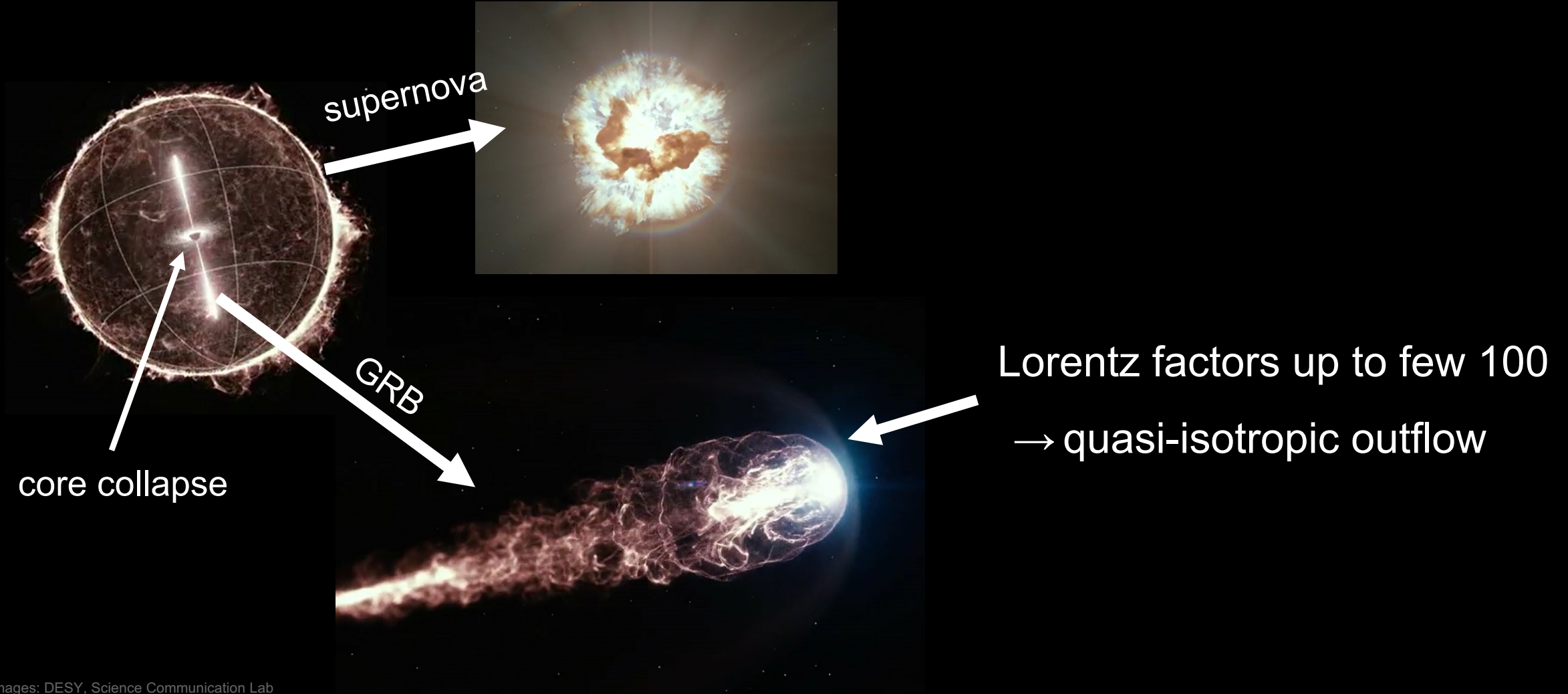
→ H.E.S.S.

→ LHAASO

- Flat power-law spectra extending up to >TeV
- Single component?
- No preference at counts-level
- **How to interpret this?**

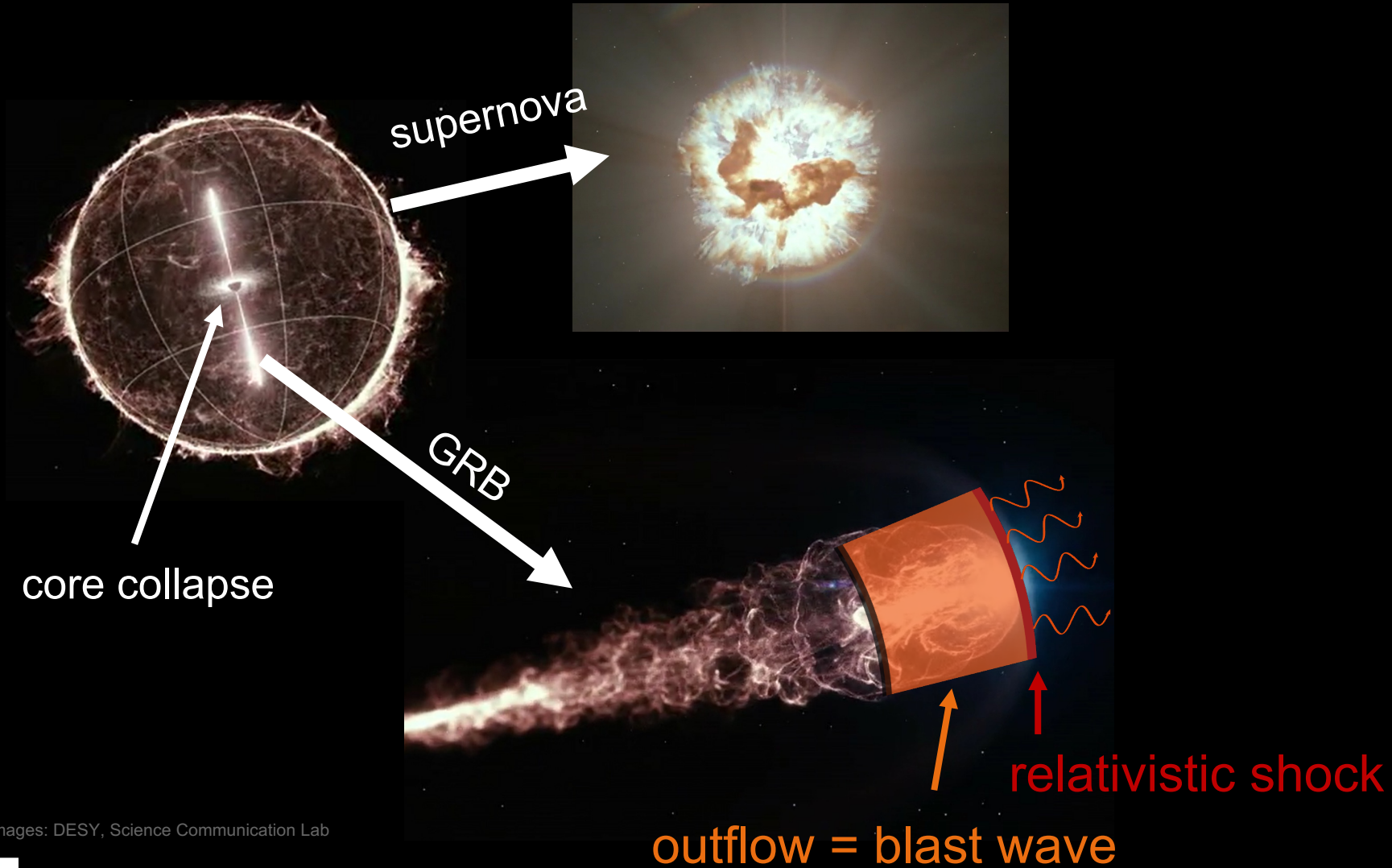
data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
 Liu++ APJL 943 (2023)  
 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)

# Long GRBs



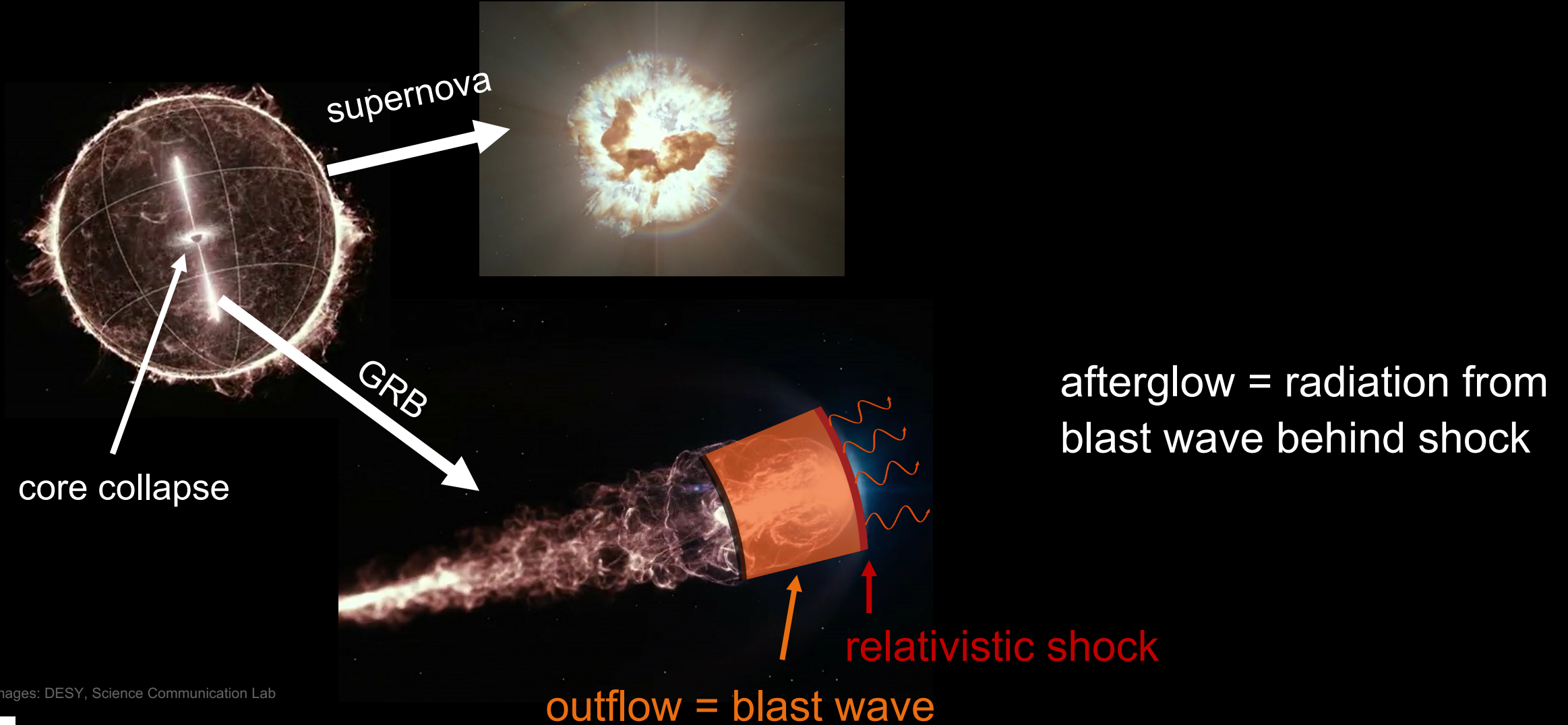
images: DESY, Science Communication Lab

# Long GRBs



images: DESY, Science Communication Lab

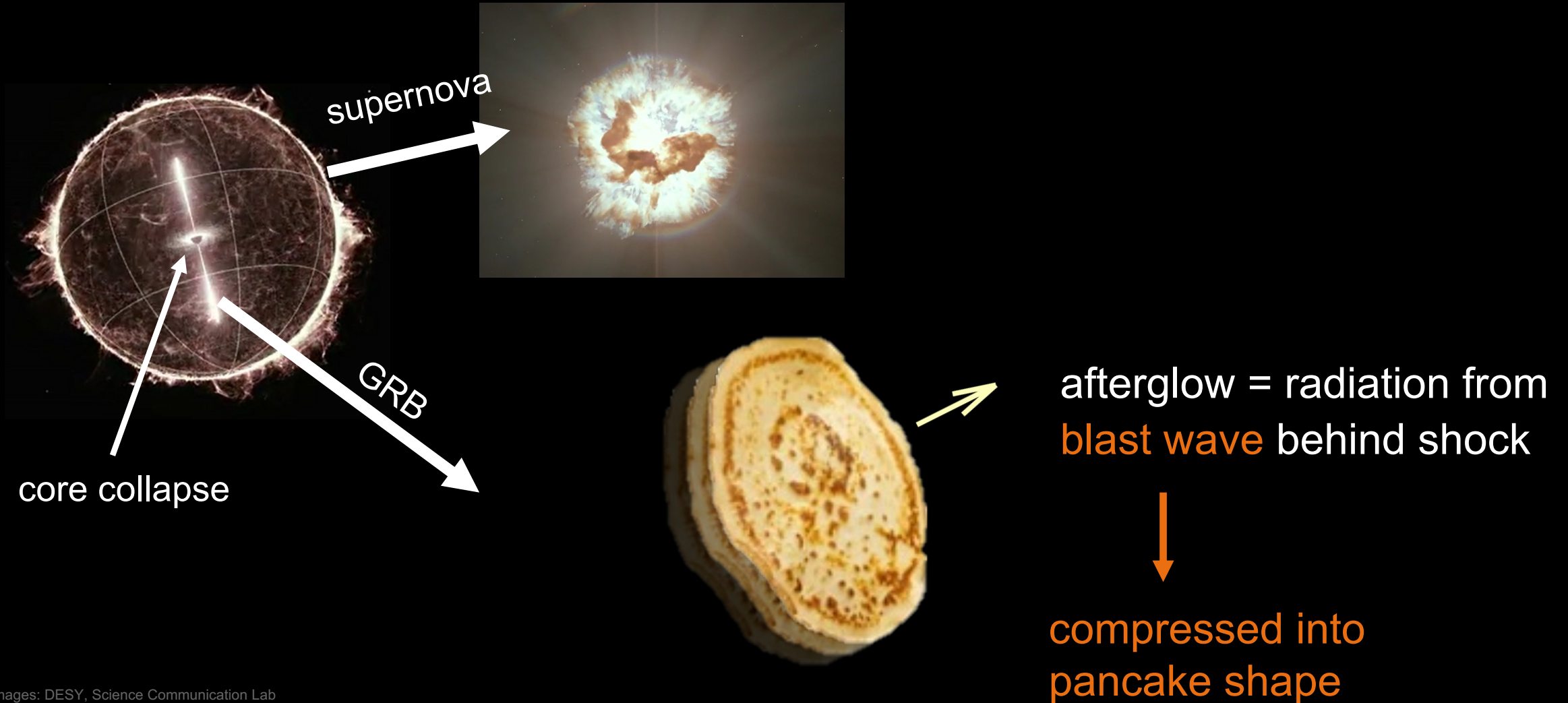
# Long GRBs



images: DESY, Science Communication Lab



# Long GRBs



images: DESY, Science Communication Lab

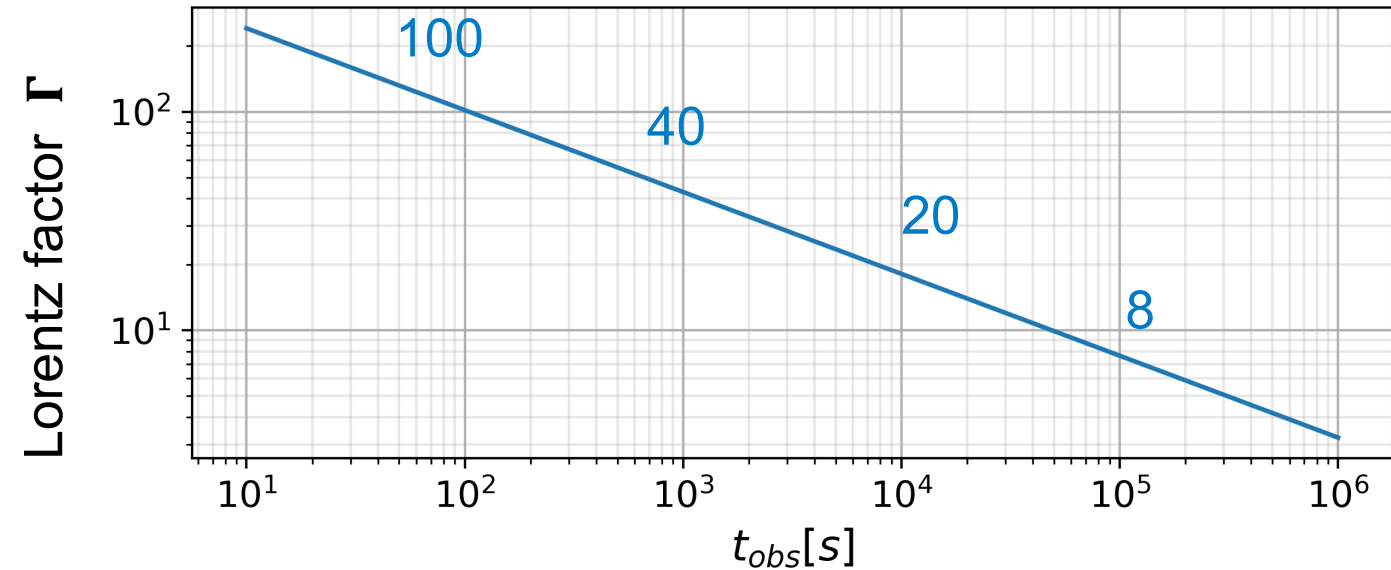
# Pancake dynamics

energy conservation:

- sweeping up
- slowing down

power-law deceleration  
(Blandford&McKee 1976)

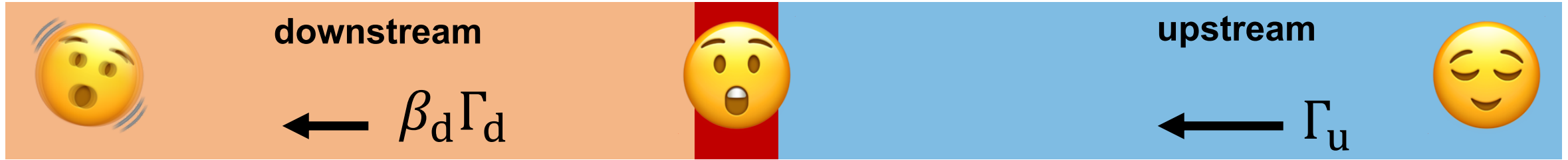
$$E_{\text{kin,iso}} = 10^{54} \text{ erg}, n_{\text{u}} = 1 \text{ cm}^{-3}$$



$$\rightarrow \Gamma(t_{\text{obs}}) \propto 100 \left( \frac{E_{\text{kin,iso}}}{10^{54} \text{ erg}} \right)^{\frac{1}{8}} \left( \frac{1 \text{ cm}^{-3}}{n_{\text{u}}} \right)^{\frac{1}{8}} \left( \frac{100 \text{ s}}{t_{\text{obs}}} \right)^{\frac{3}{8}}$$

# Energy conversion at the shock

in shock rest frame



heat (isotropic)

slower outflow (anisotropic)

turbulent magnetic fields ( $\varepsilon_B$ )

non-thermal particles

(power law:  $s_{inj}, E_{min}, E_{max}, \varepsilon_{e/p}$ )

kinetic energy/  
ram pressure

$$p_{ram}^u = \Gamma_u^2 \rho_u c^2$$

with  $\rho_u = n_u m_p c^2$

$$\varepsilon_X = \frac{p_X^d}{p_{ram}^u}$$

# Astrophysical Multi-Messenger Modeling (AM<sup>3</sup>)

- 1 homogeneous, isotropic fluid cell
- **solve comoving transport equations**

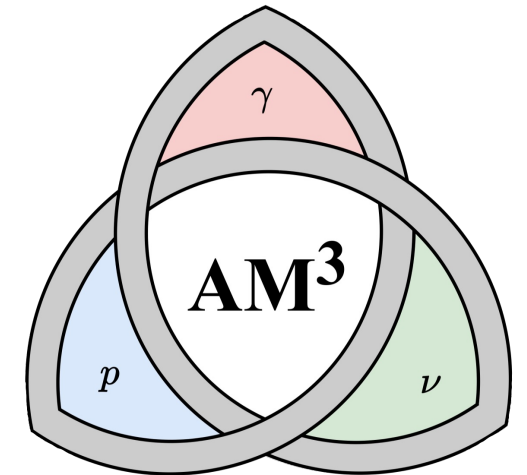
for species  $i \in [p, n, e, \pi, \mu, \nu, \gamma]$

$$\partial_t n_i = Q + \partial_E (\dot{E} n_i) - \alpha n_i$$

depend in general on  $E, t, n_j$

particle number density

$$n_i(E, t) = \frac{\partial^2 N_i}{\partial E \partial V}$$

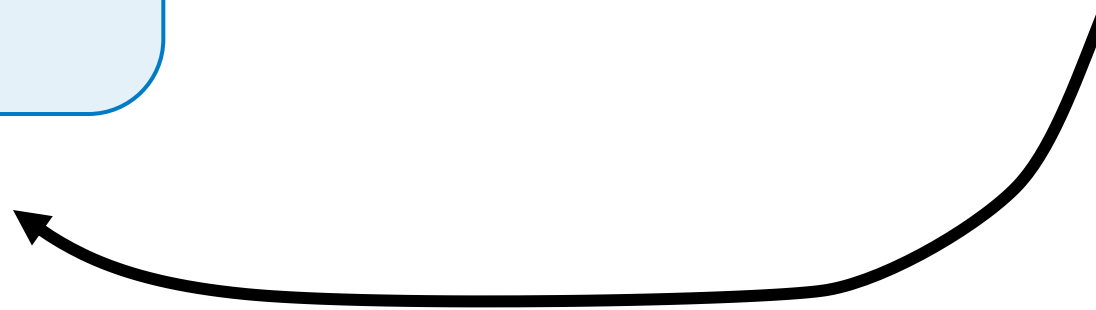


# AM<sup>3</sup> workflow

estimate the  
coefficients  $Q$ ,  $\dot{E}$ ,  $\alpha$   
(time scales)  
based on current state  
of system



evolve particle densities  $n_i$   
in time for small step



# AM<sup>3</sup> workflow

estimate the  
coefficients  $Q$ ,  $\dot{E}$ ,  $\alpha$   
(time scales)  
based on current state  
of system



evolve particle densities  $n_i$   
in time for small step

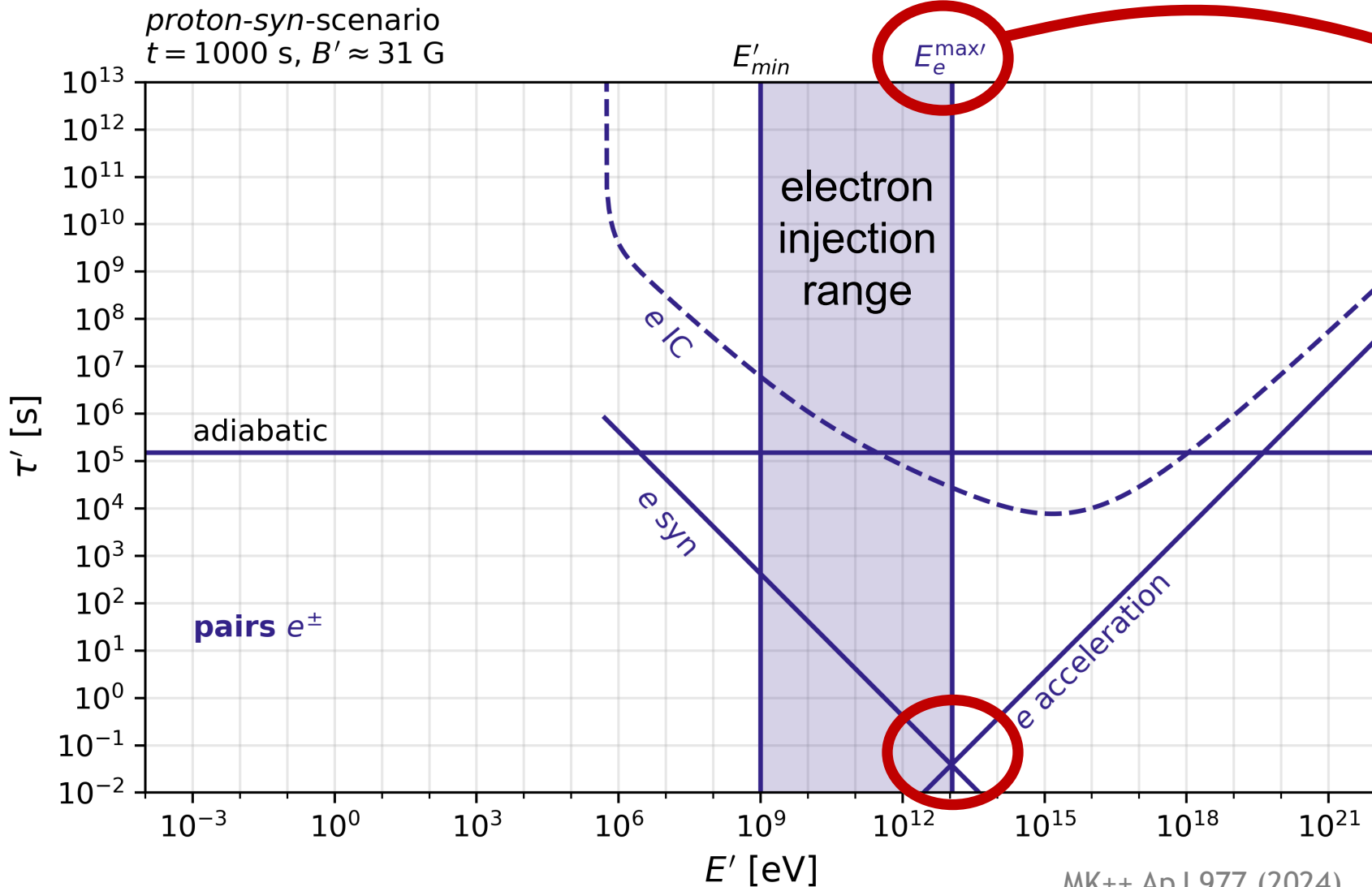


# Estimate the coefficients

	$e^-$	$e^+$	$\gamma$	$n$	$p$	$\nu$	$\mu^\pm$	$\pi^\pm$
Injection	$Q_{e^-,inj}$	–	$Q_{\gamma,inj}$	–	$Q_{p,inj}$	–	–	–
Escape	$\alpha_{e^-,esc}$	$\alpha_{e^+,esc}$	$\alpha_{\gamma,esc}$	$\alpha_{n,esc}$	$\alpha_{p,esc}$	$\alpha_{\nu,esc}$	$\alpha_{\mu,esc}$	$\alpha_{\pi,esc}$
Synchrotron	$\dot{E}_{e^-,SY}$	$\dot{E}_{e^+,SY}$	$\alpha_{\gamma,SY}, Q_{\gamma,SY}$	–	$\dot{E}_{p,SY}$	–	$\dot{E}_{\mu,SY}$	$\dot{E}_{\pi,SY}$
Inverse Compton	$\dot{E}_{e^-,IC}$	$\dot{E}_{e^+,IC}$	$\alpha_{\gamma,IC}, Q_{\gamma,IC}$	–	$\dot{E}_{p,IC}$	–	$\dot{E}_{\mu,IC}$	$\dot{E}_{\pi,IC}$
Pair annihilation	$Q_{e^-,pair}$	$Q_{e^+,pair}$	$\alpha_{\gamma,pair}$	–	–	–	–	–
Bethe-Heitler	$Q_{e^-,BH}$	$Q_{e^+,BH}$	–	–	$\dot{E}_{p,BH}$	–	–	–
Photo-pion	–	–	$\alpha_{\gamma,p\gamma}, Q_{\gamma,p\gamma}$	$\alpha_{n,p\gamma}, Q_{n,p\gamma}$	$\alpha_{p,p\gamma}, Q_{p,p\gamma}$	–	–	$Q_{\pi,p\gamma}$
Proton-proton	–	–	$Q_{\gamma,pp}$	–	$\dot{E}_{p,pp}$	–	–	$Q_{\pi,pp}$
Adiabatic/Expansion	$\dot{E}_{e^-,ad}, \alpha_{e^-,exp}$	$\dot{E}_{e^+,ad}, \alpha_{e^+,exp}$	$\alpha_{\gamma,exp}$	$\dot{E}_{p,ad}, \alpha_{p,exp}$	$\alpha_{n,exp}$	$\alpha_{\nu,exp}$	$\dot{E}_{\mu,ad}, \alpha_{\mu,exp}$	$\dot{E}_{\pi,ad}, \alpha_{\pi,exp}$
Pion Decay	–	–	–	–	–	$Q_{\nu,\pi-dec}$	$Q_{\mu,\pi-dec}$	$\alpha_{\pi,\pi-dec}$
Muon Decay	$Q_{e^-,\mu-dec}$	$Q_{e^+,\mu-dec}$	–	–	–	$Q_{\nu,\mu-dec}$	$\alpha_{\mu,\mu-dec}$	–

→ see appendix of [Klinger et al. 2024 ApJS 275 4](#) for details

# GRB afterglow example

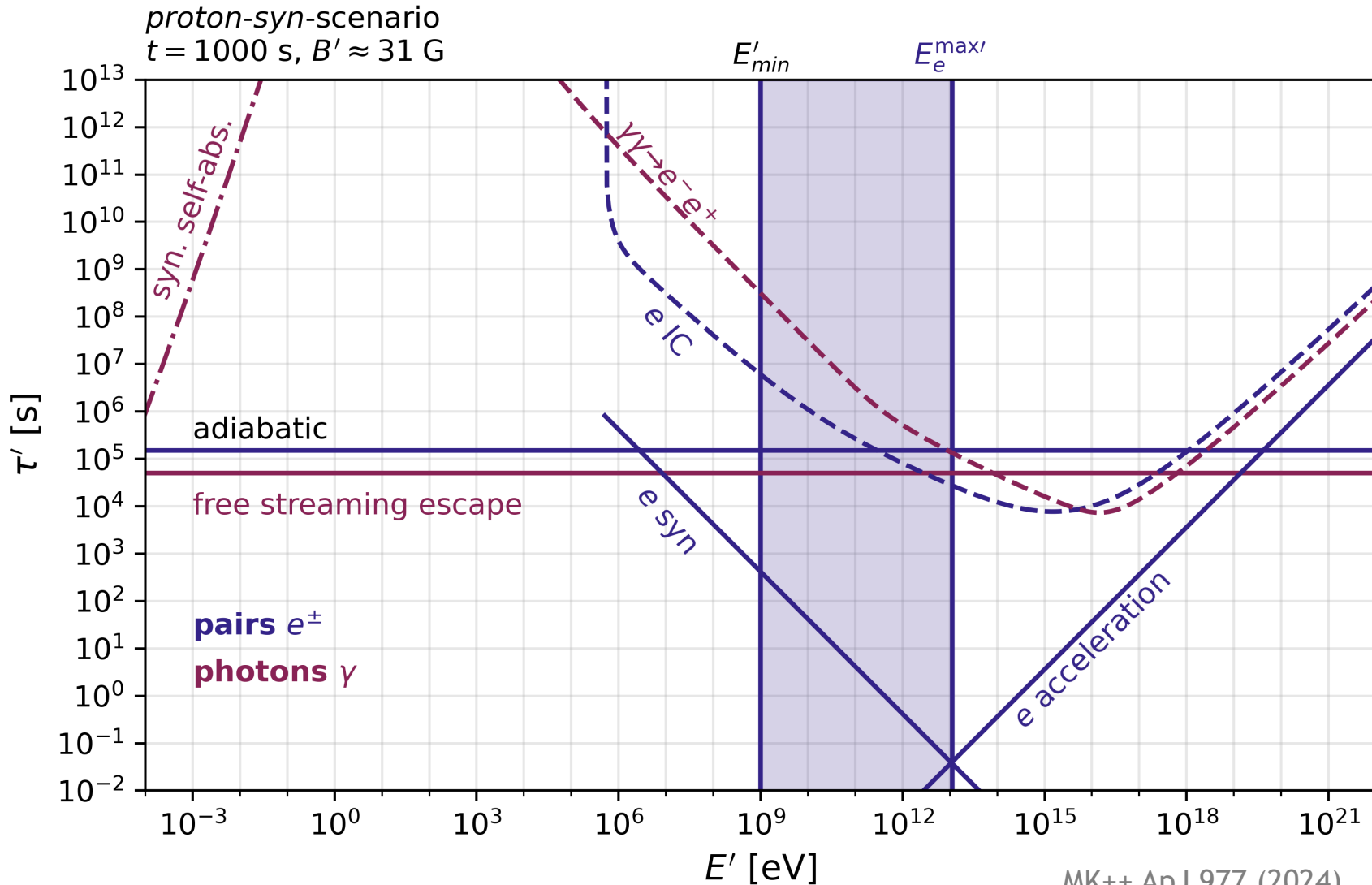


reparameterise  $E'_{e/p}^{max}$   
 via (inverse) efficiency  $\eta$   
 $\rightarrow$  acceleration vs.  
 cooling

MK++ ApJ 977 (2024)



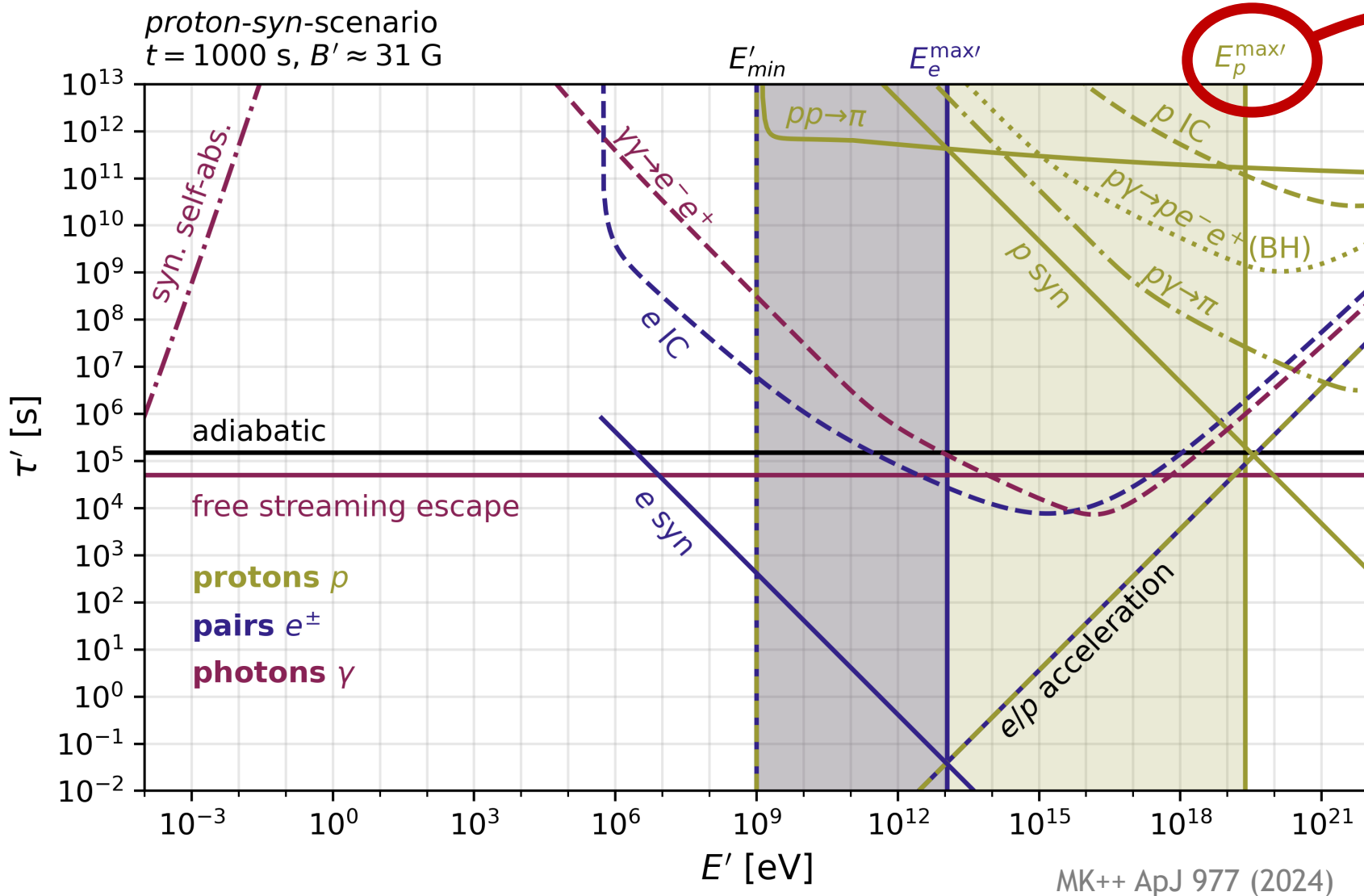
# GRB afterglow example



→ including photons

MK++ ApJ 977 (2024)

# GRB afterglow example

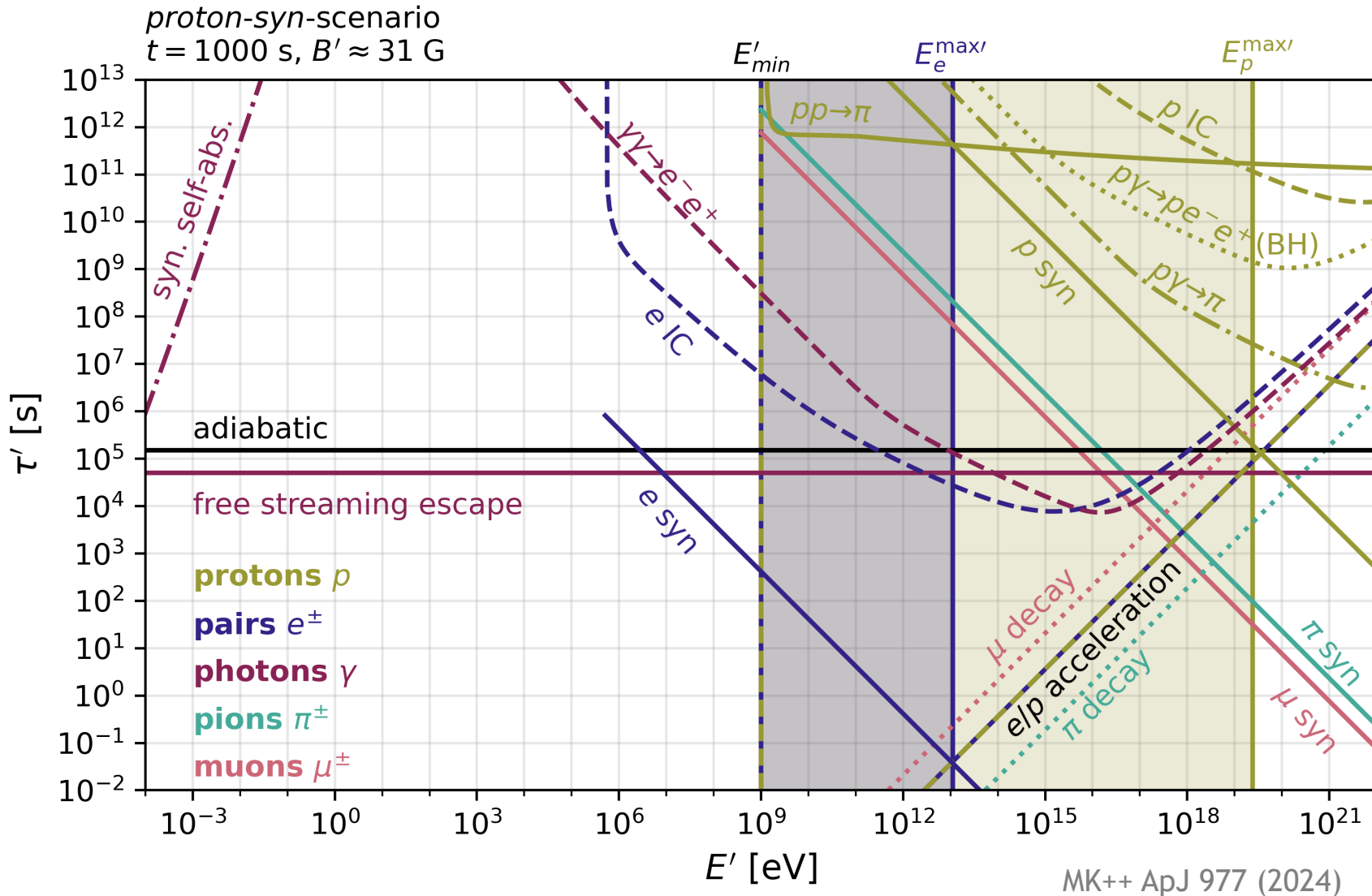


same  $\eta$

→ including protons

MK++ ApJ 977 (2024)

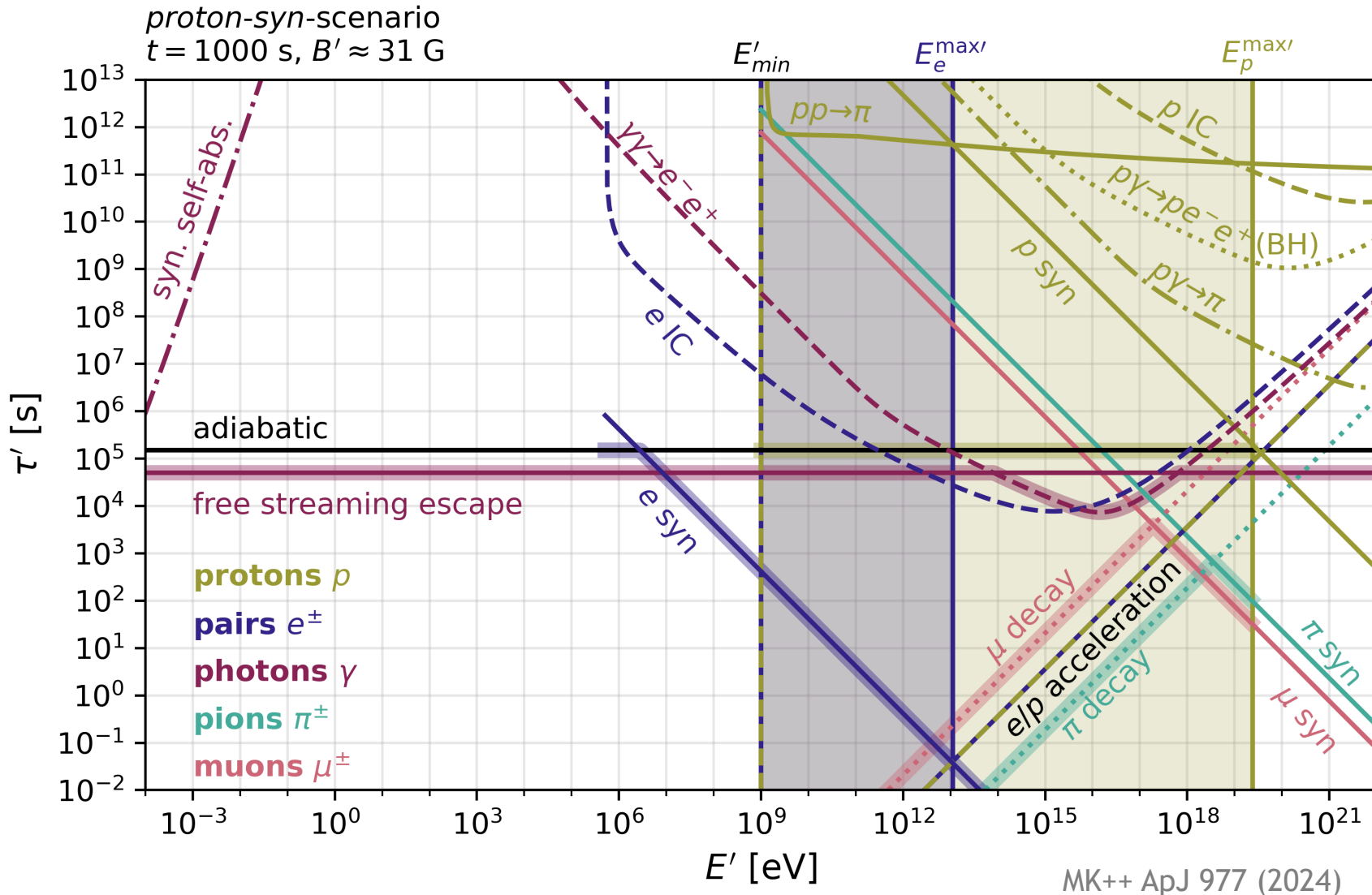
# GRB afterglow example



→ including muons and pions from cascade

MK++ ApJ 977 (2024)

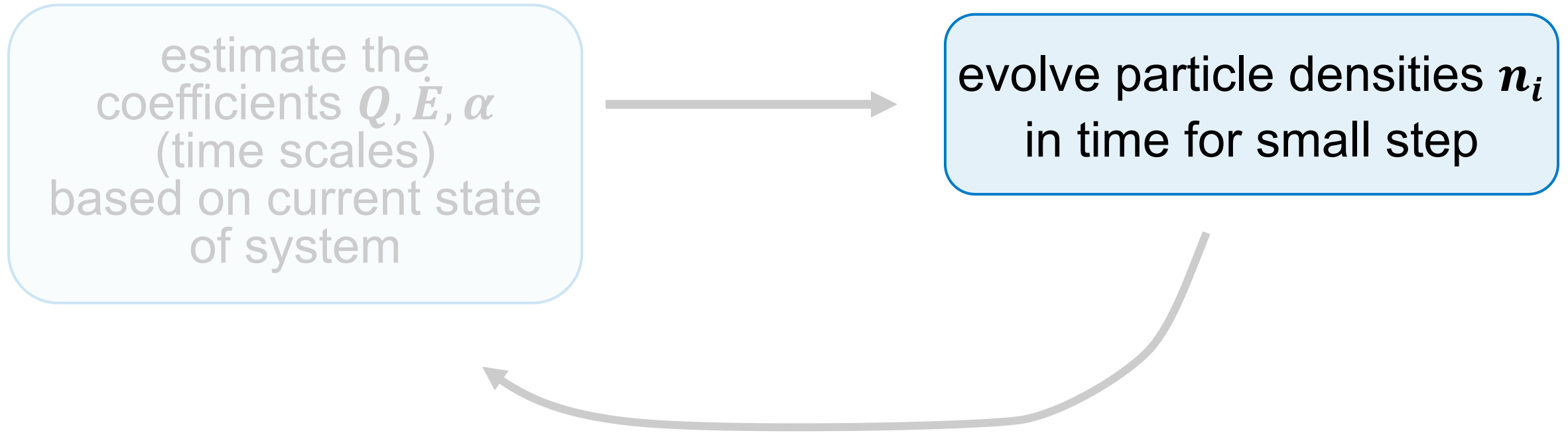
# GRB afterglow example



→ effect on (quasi)  
 steady state  $\propto Q \times \tau_{min}$

MK++ ApJ 977 (2024)

# AM<sup>3</sup> workflow

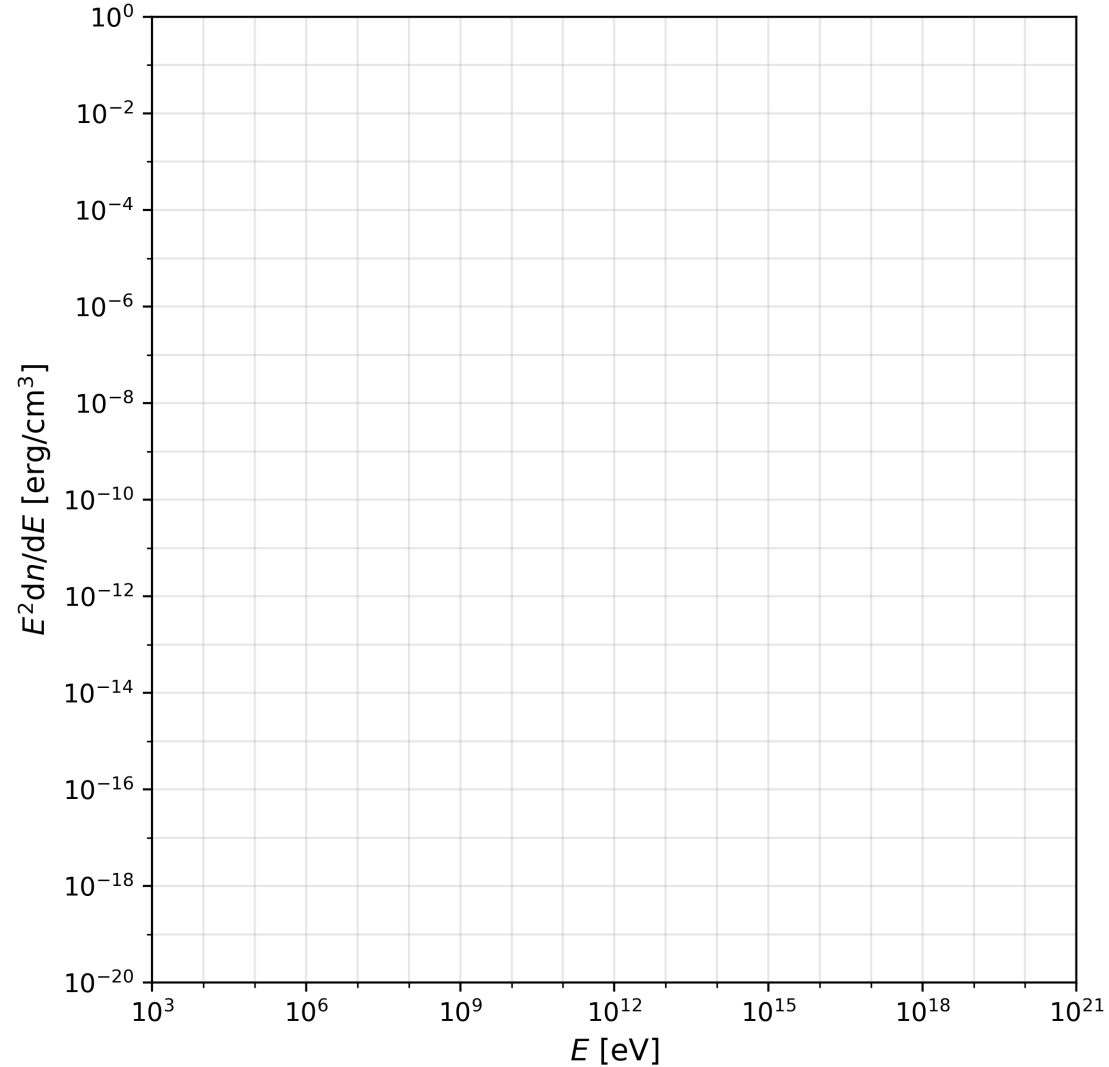


## fast solver combining

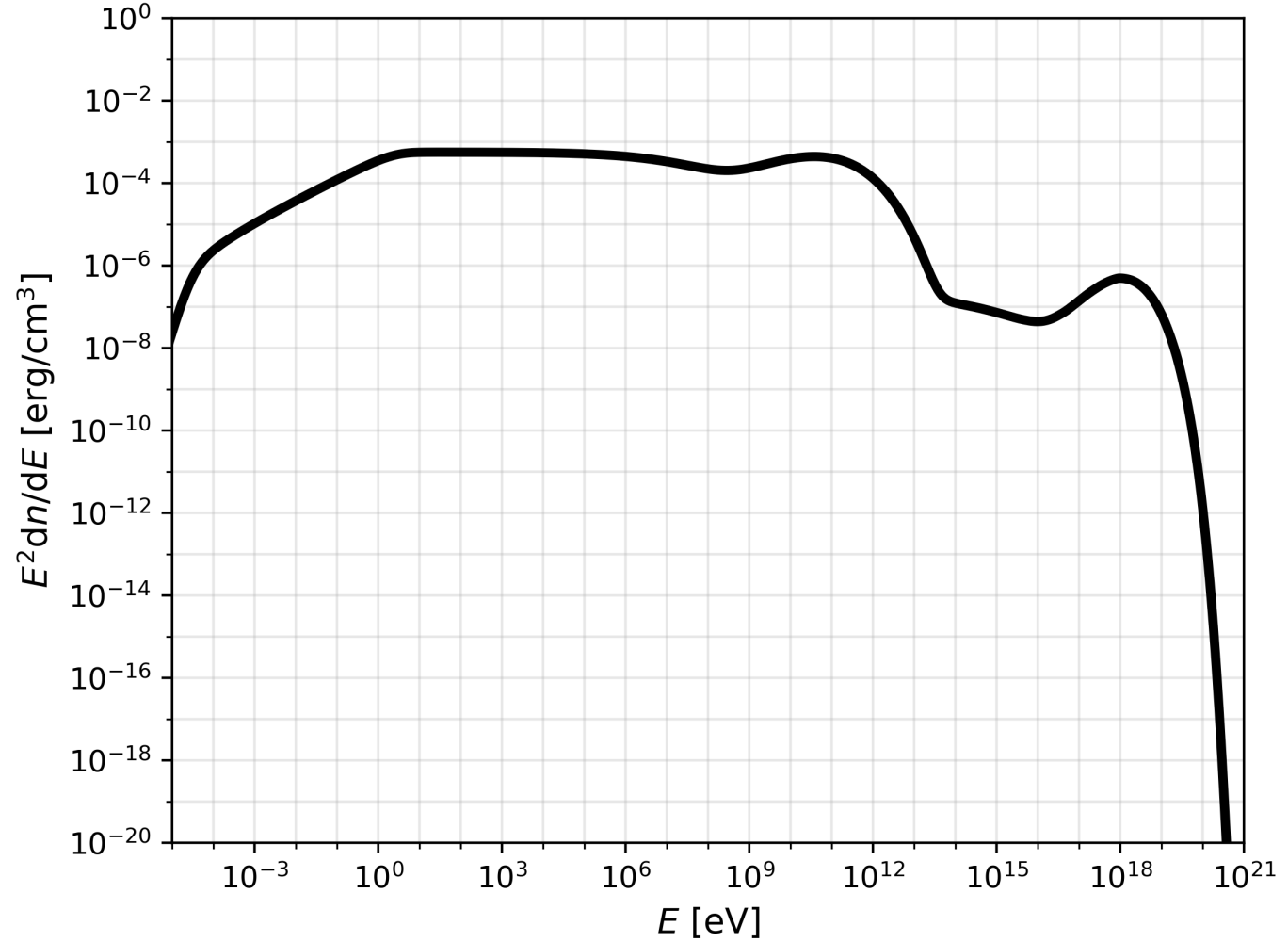
- tridiagonal matrix method
- semi-analytical approximations
- see [Klinger et al. 2024 ApJS 275 4](#) for details (or my talk from last year)

# Particle Densities $\rightarrow$ $AM^3$ is trackable

comoving particle SEDs

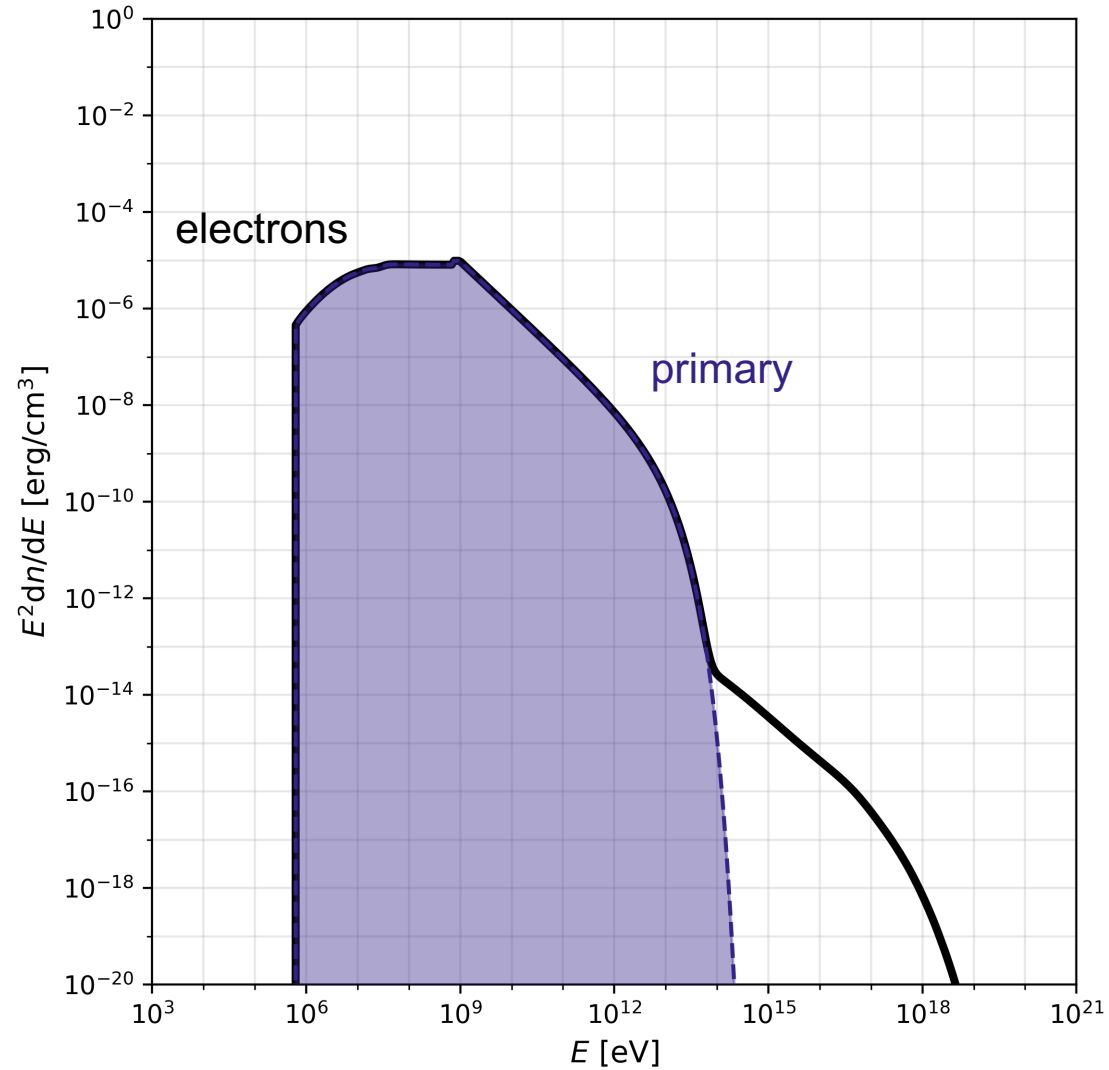


comoving photon SED

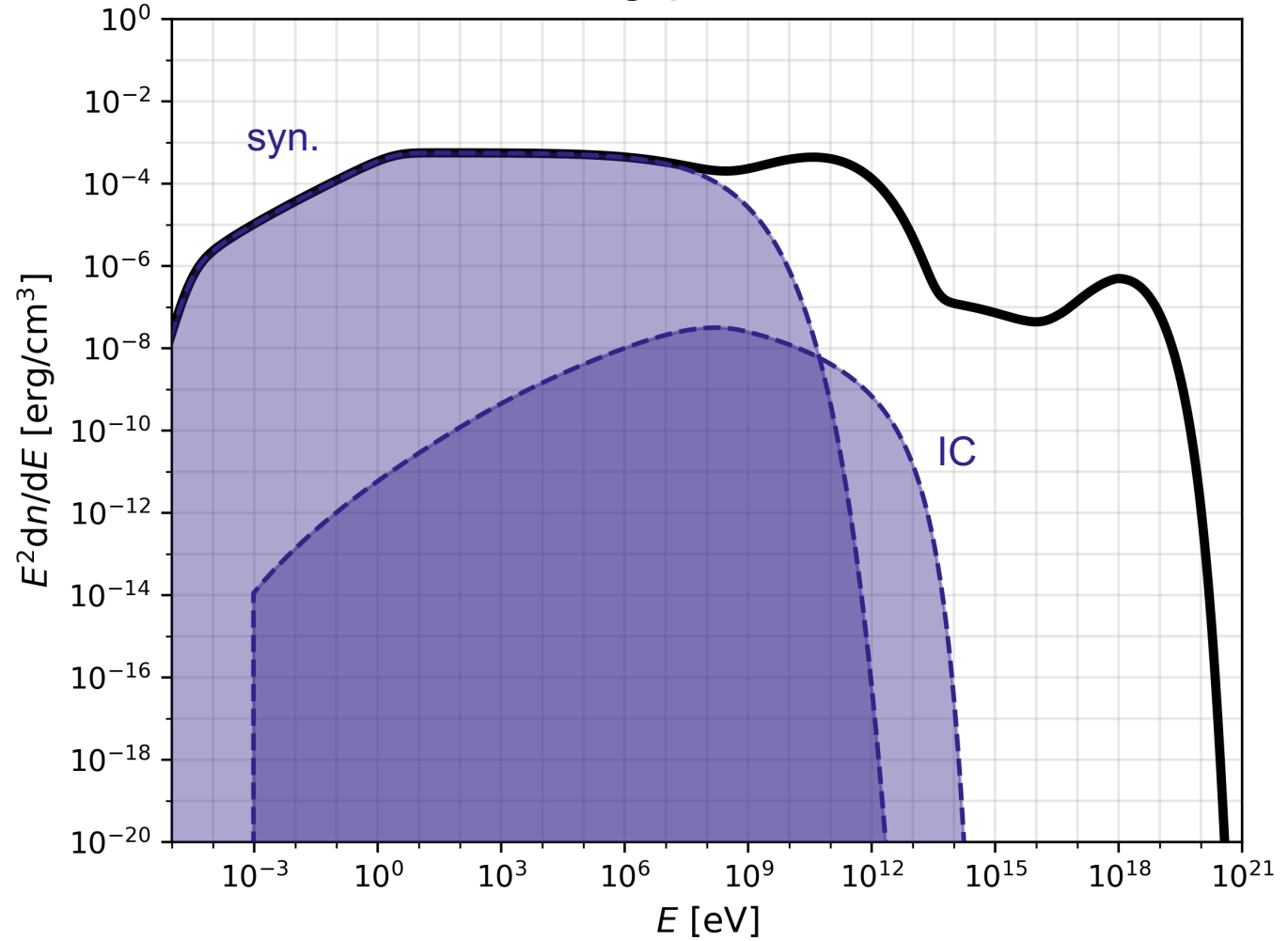


# Trackable

## comoving particle SEDs

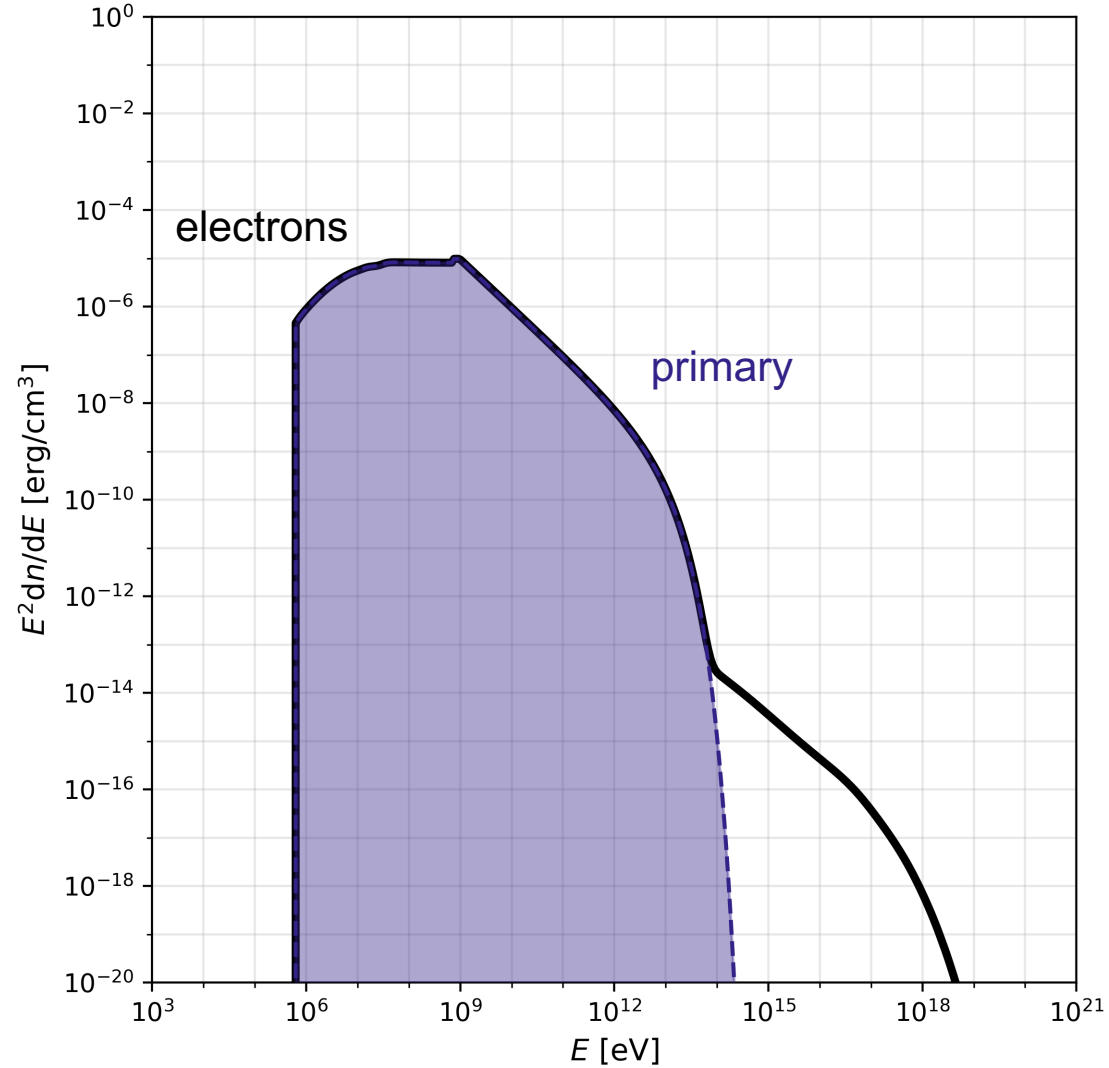


## comoving photon SED

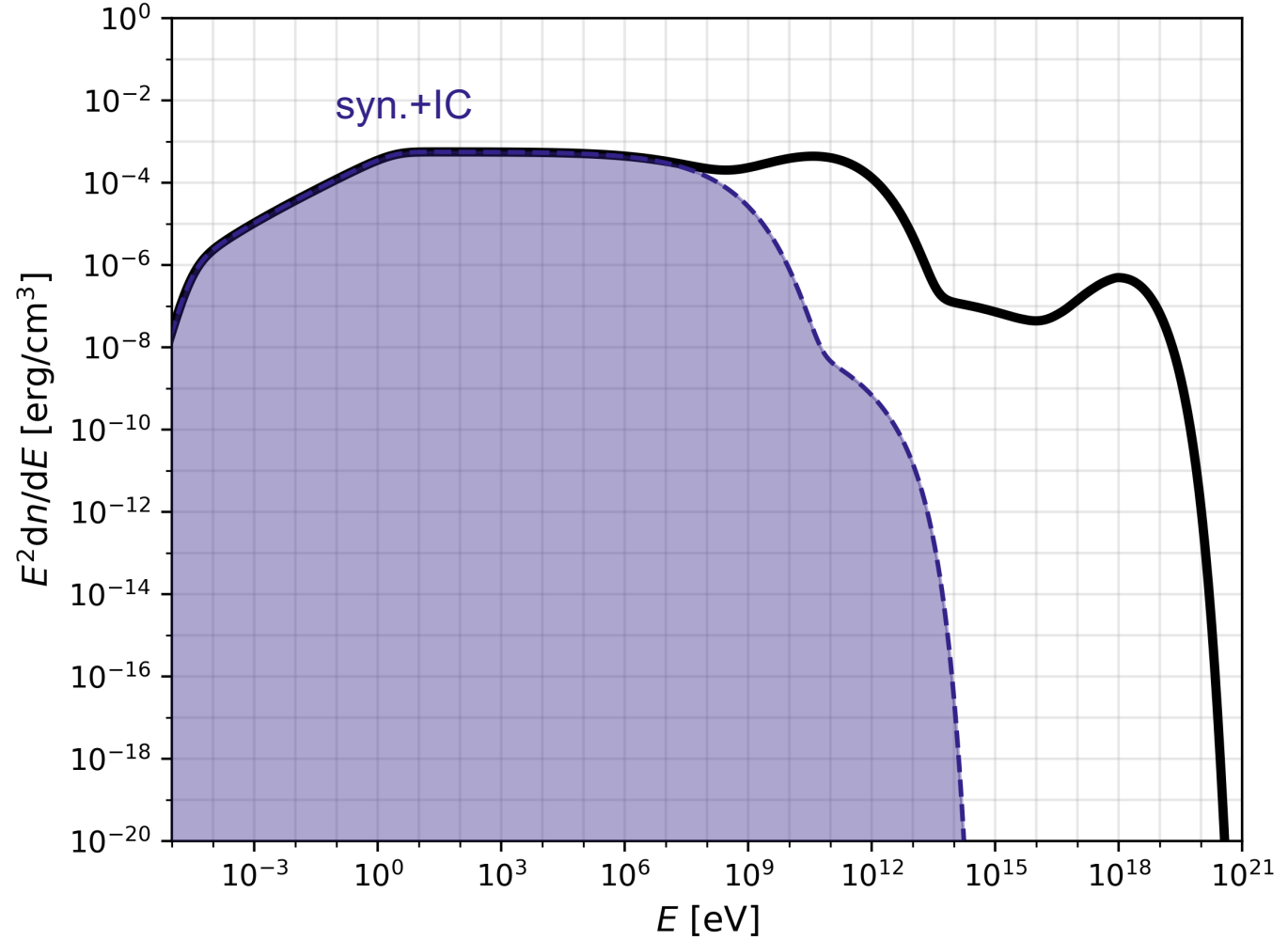


# Trackable

## comoving particle SEDs



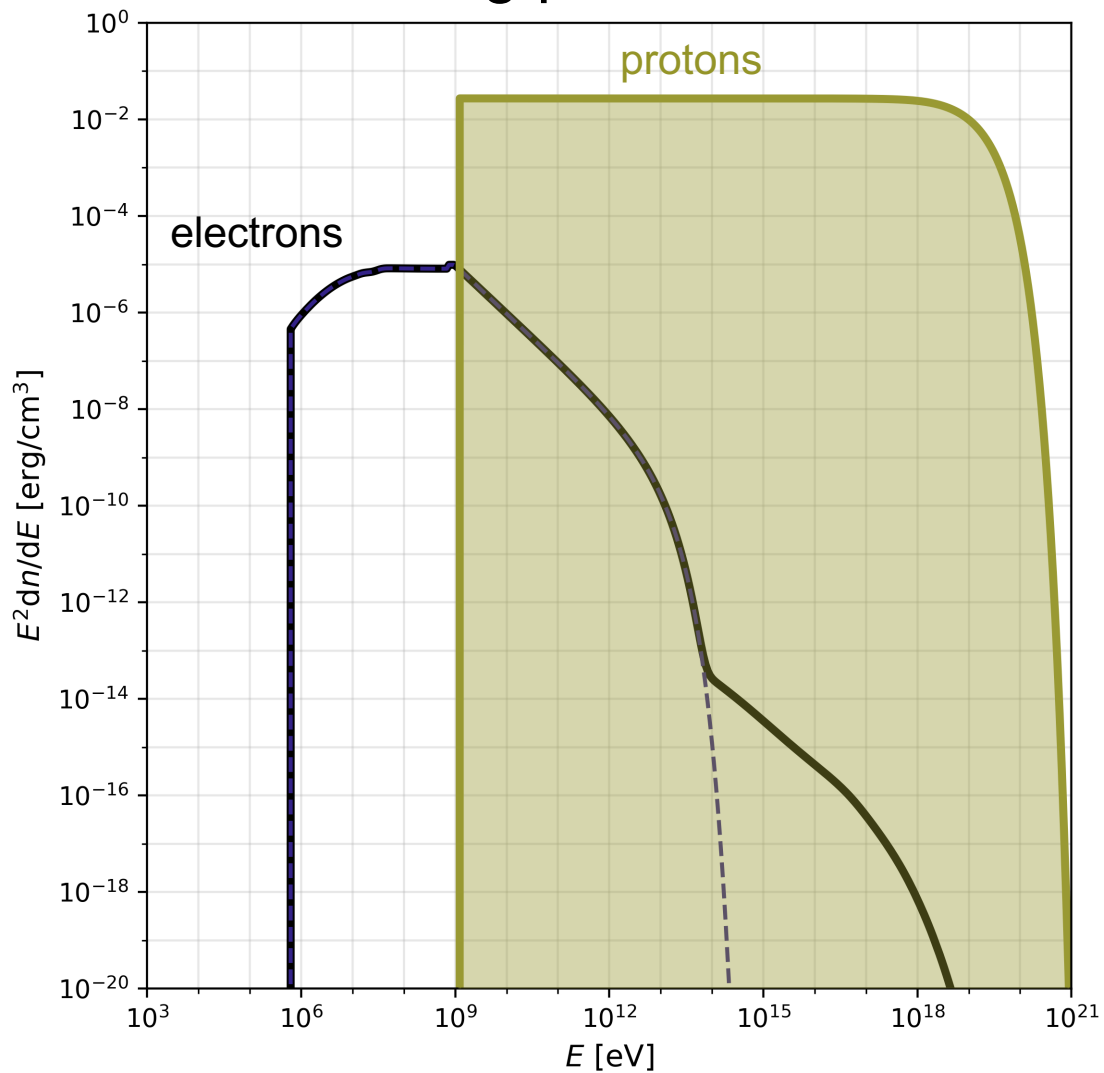
## comoving photon SED



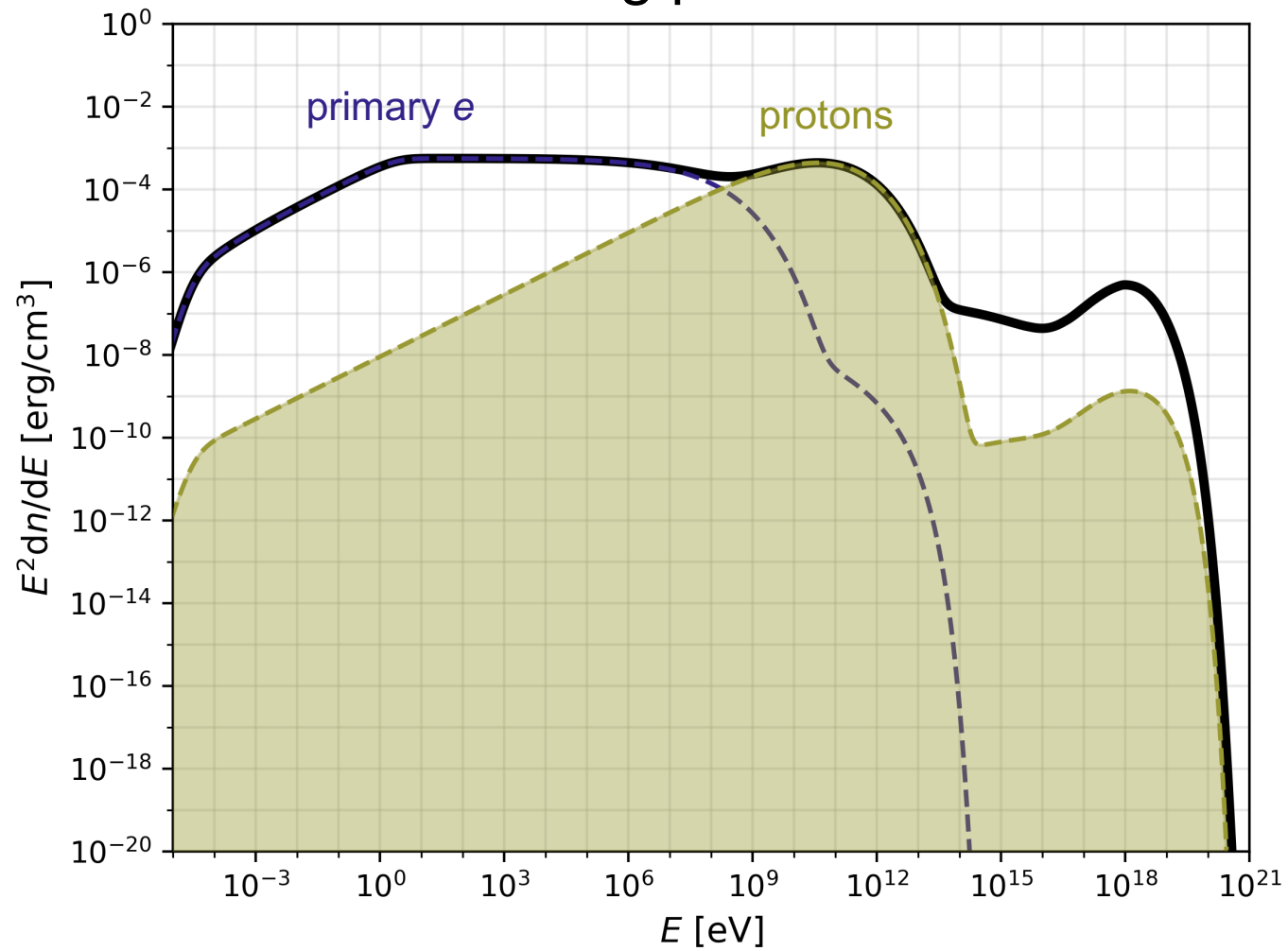


# Trackable

## comoving particle SEDs

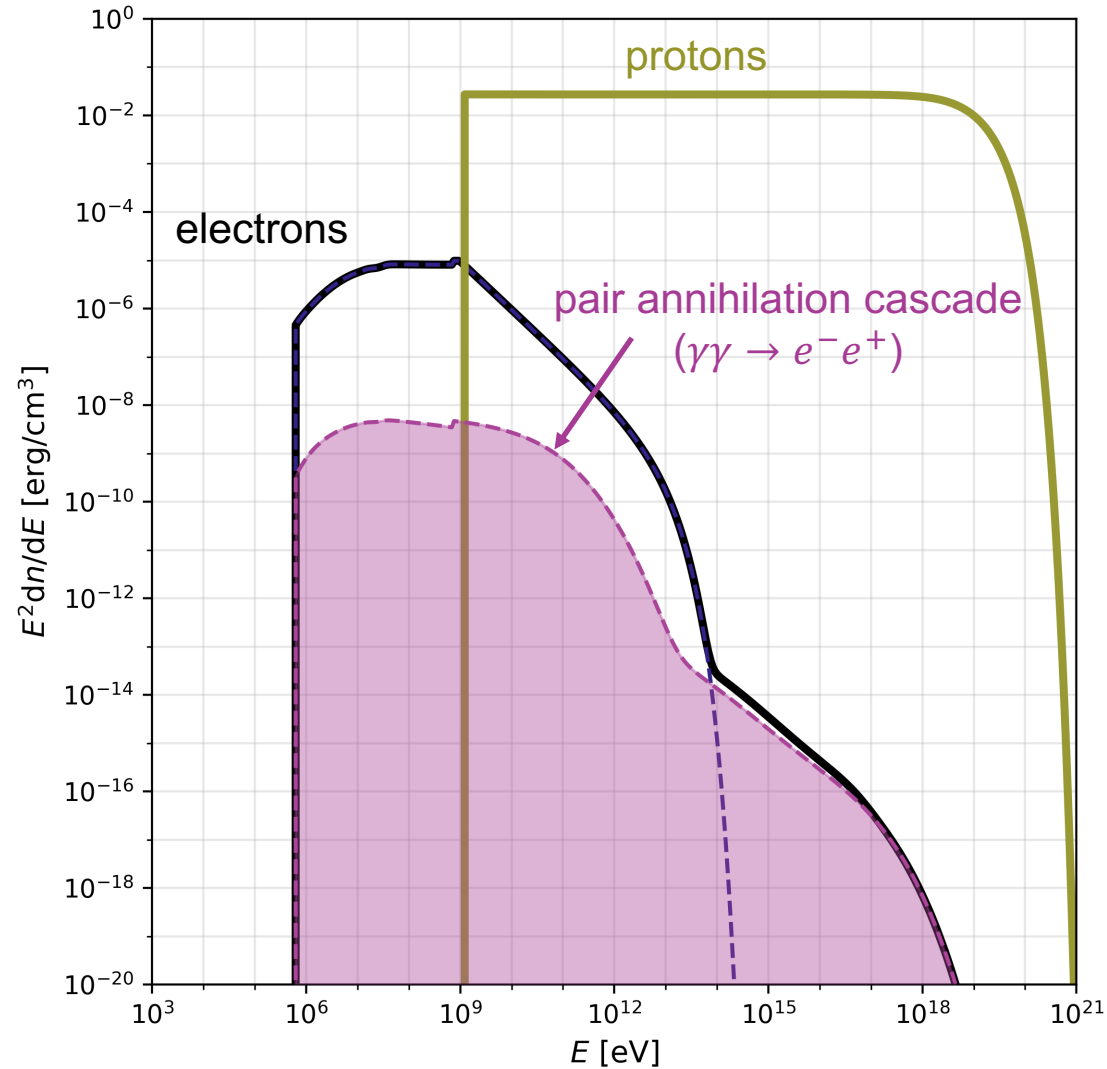


## comoving photon SED

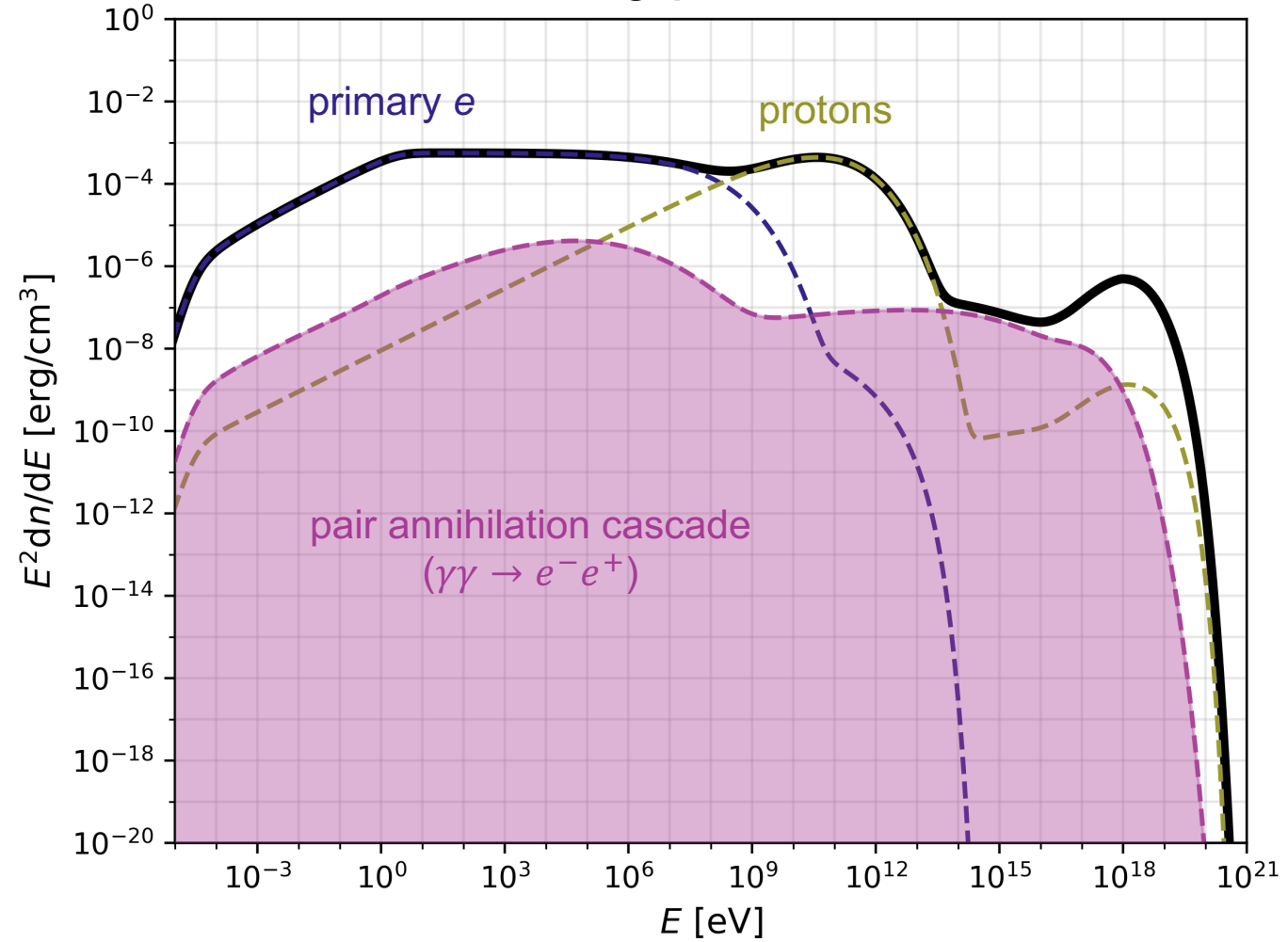


# Trackable - pair annihilation

comoving particle SEDs

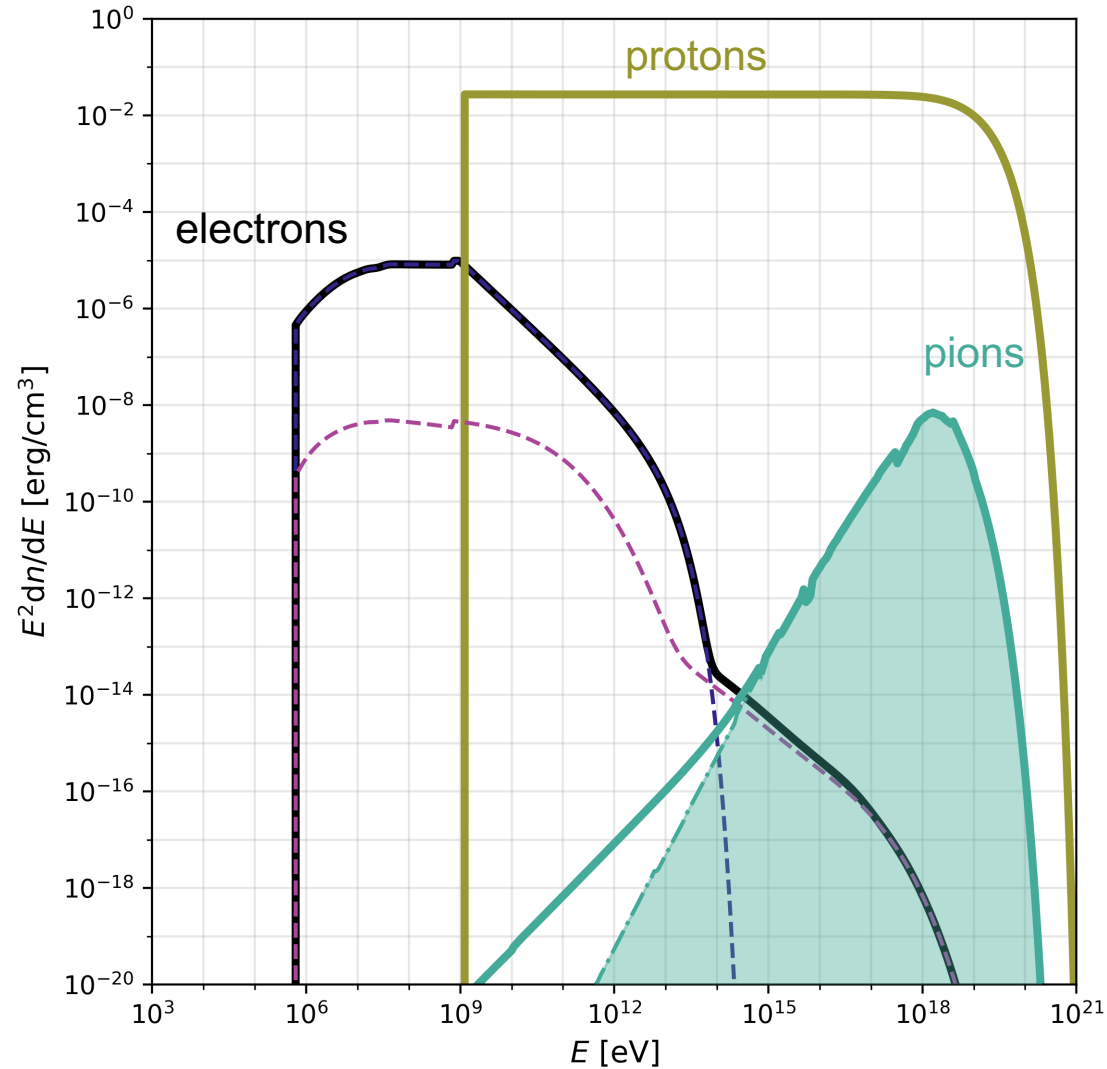


comoving photon SED

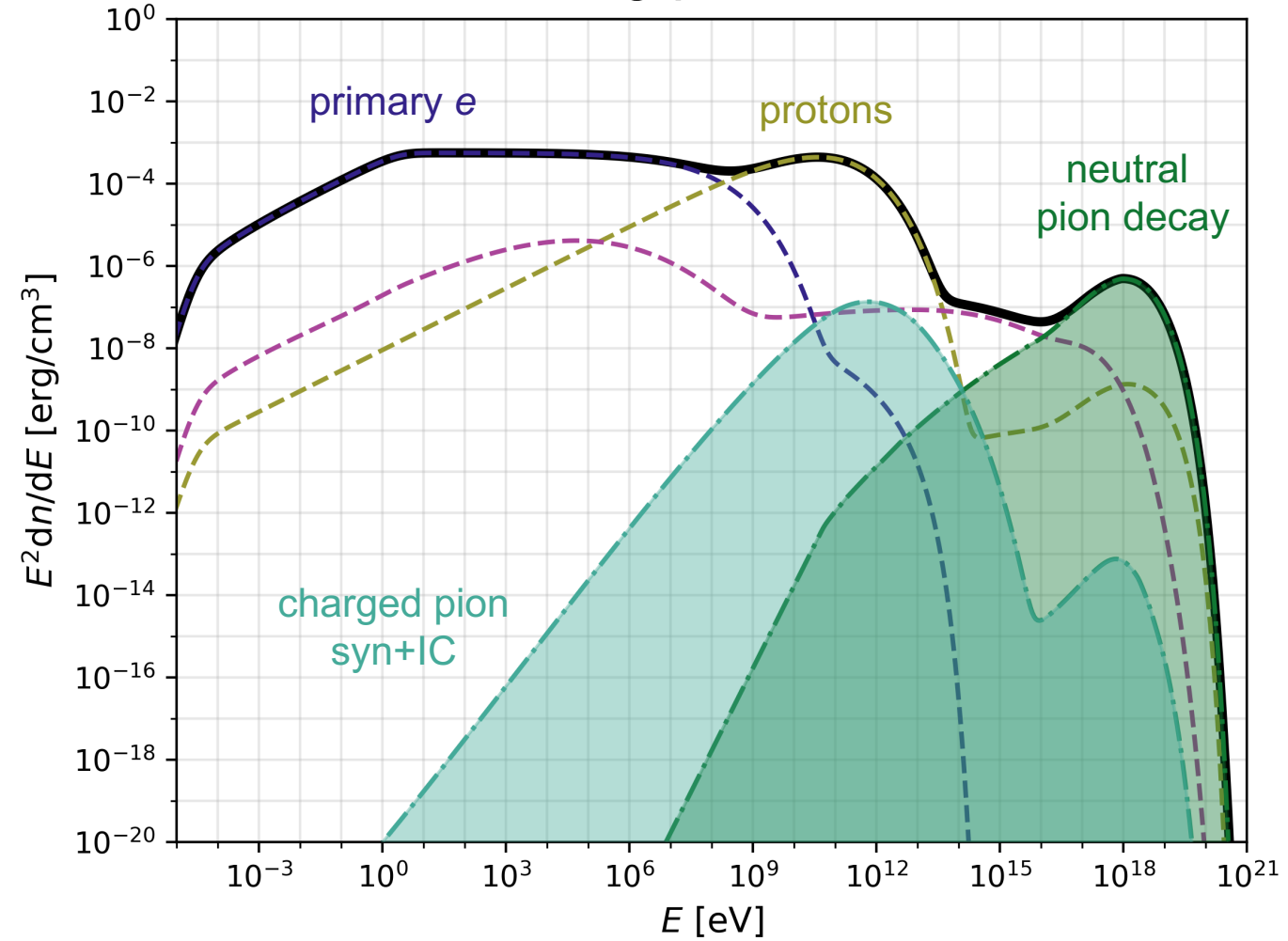


# Trackable - photo-pion cascade: $p\gamma \rightarrow \pi$

comoving particle SEDs

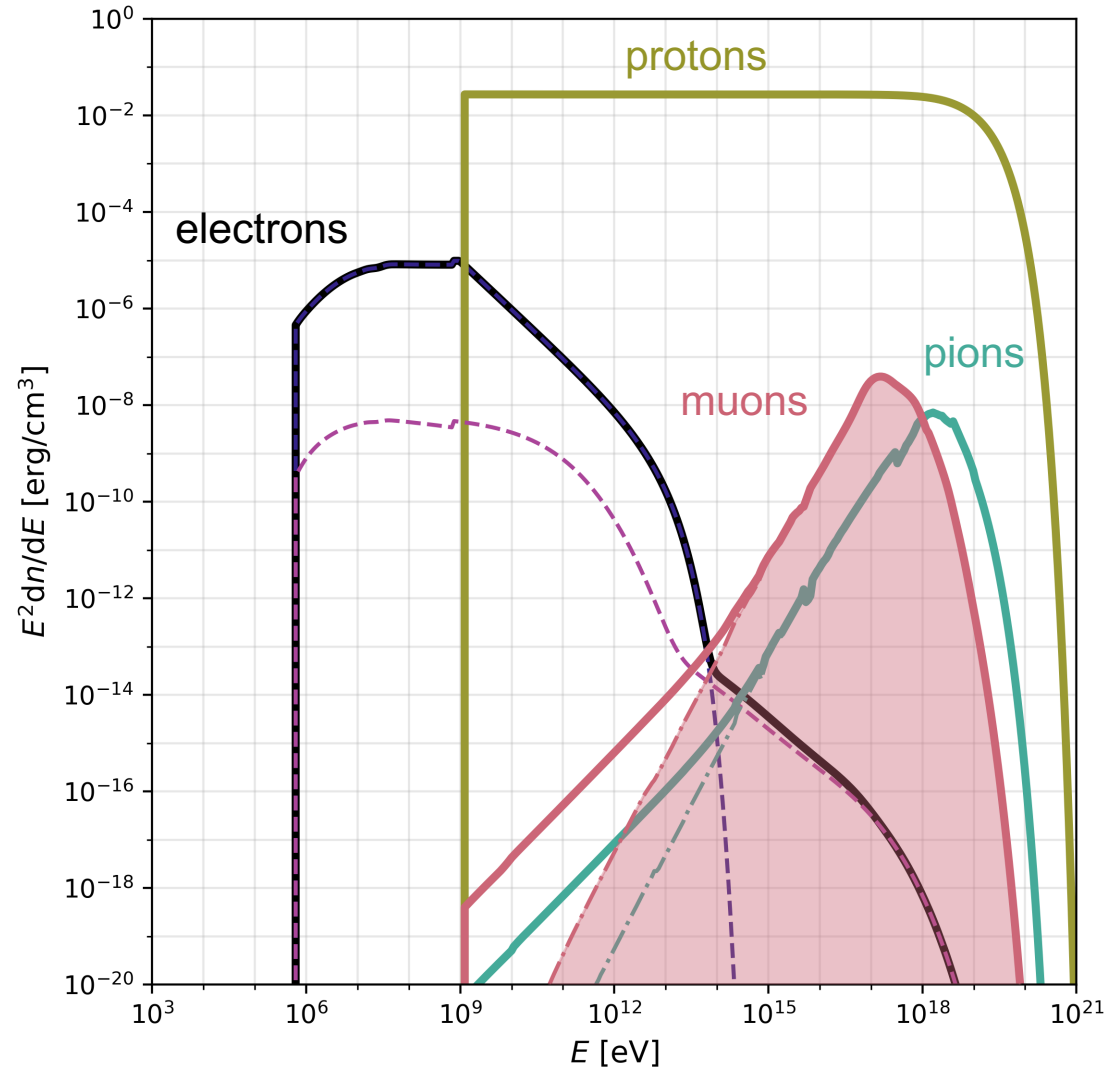


comoving photon SED

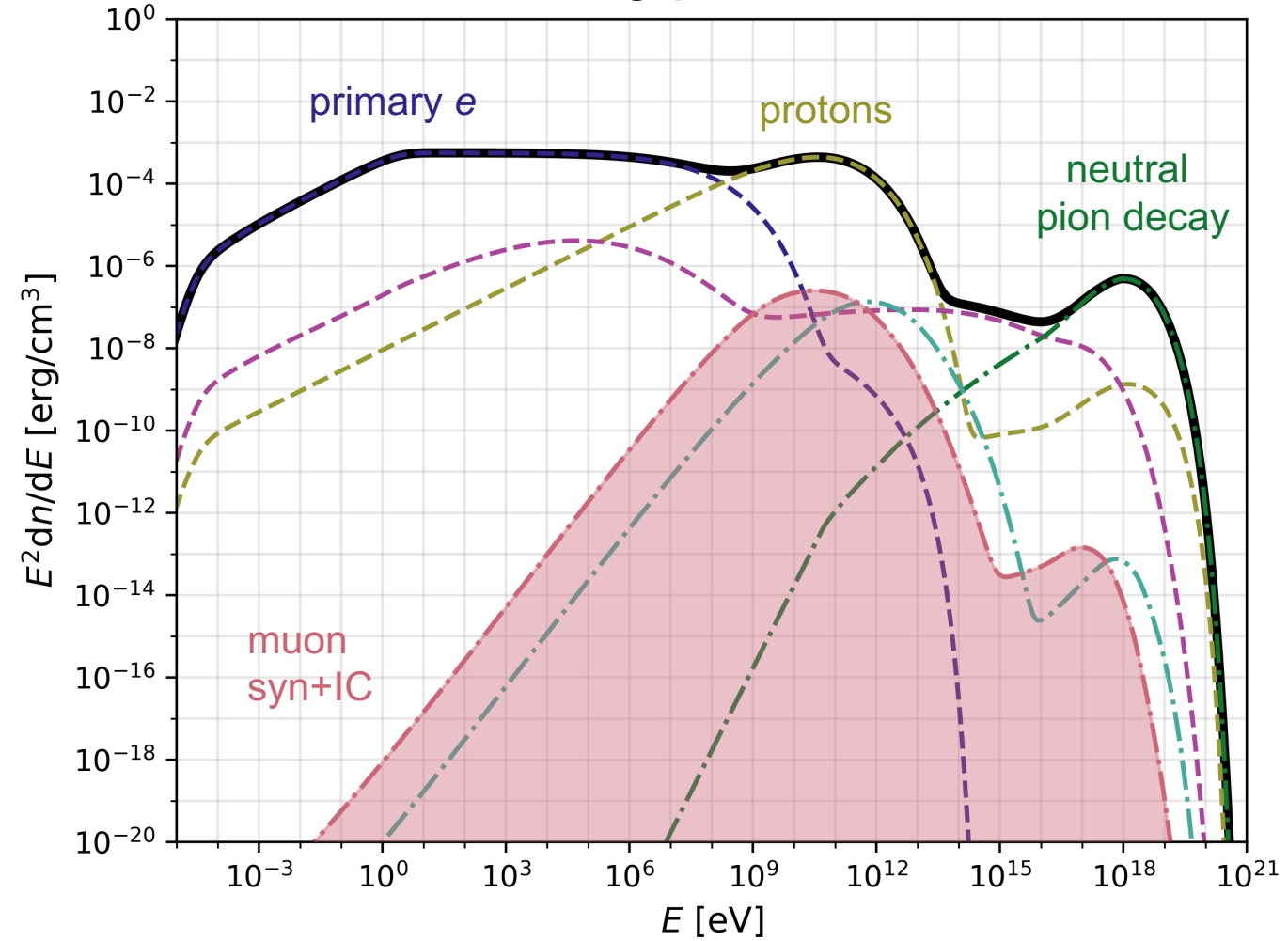


# Trackable - photo-pion cascade: $p\gamma \rightarrow \pi \rightarrow \mu$

comoving particle SEDs

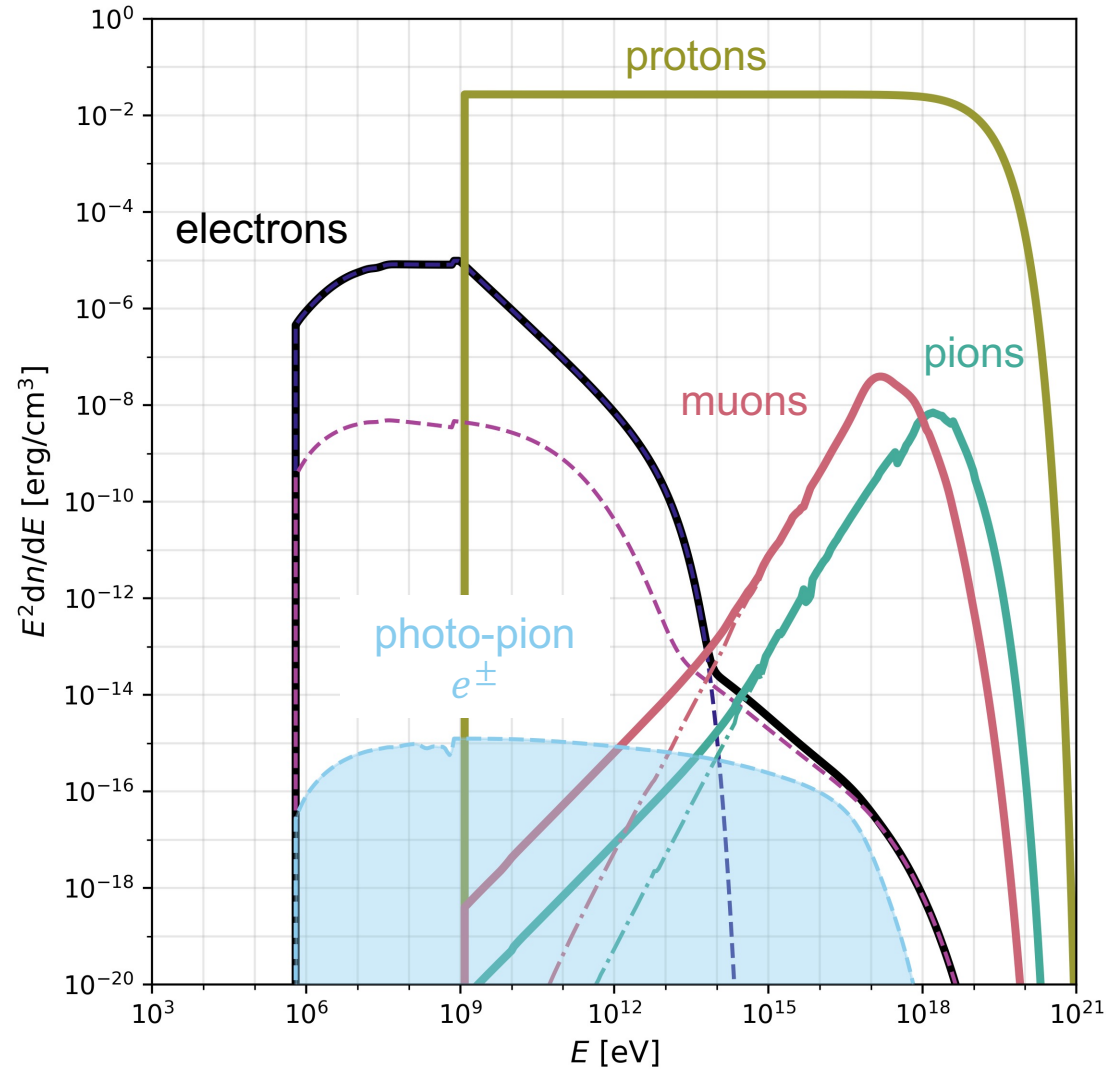


comoving photon SED

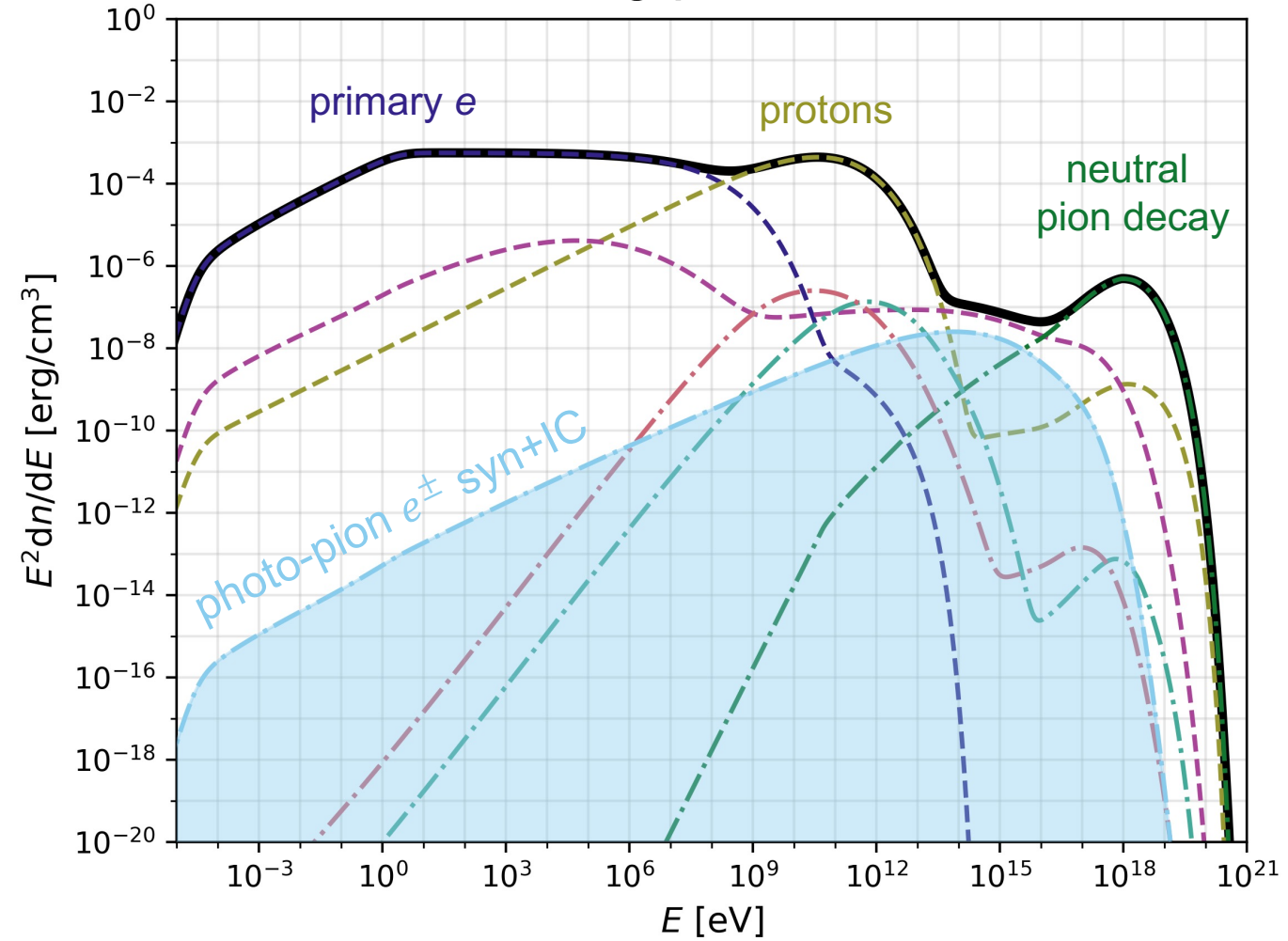


# Trackable - photo-pion cascade: $p\gamma \rightarrow \pi \rightarrow \mu \rightarrow e^\pm$

comoving particle SEDs

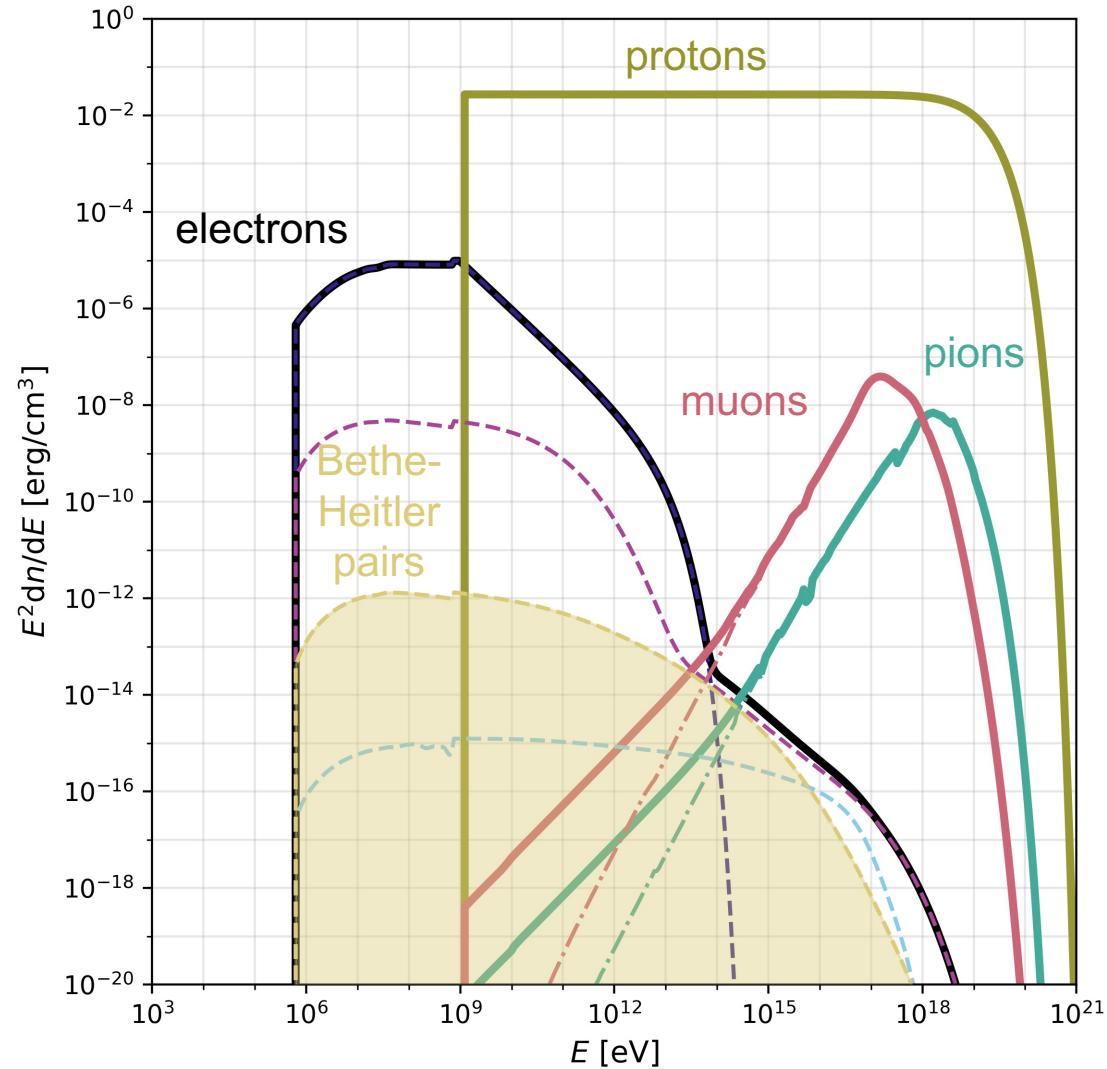


comoving photon SED

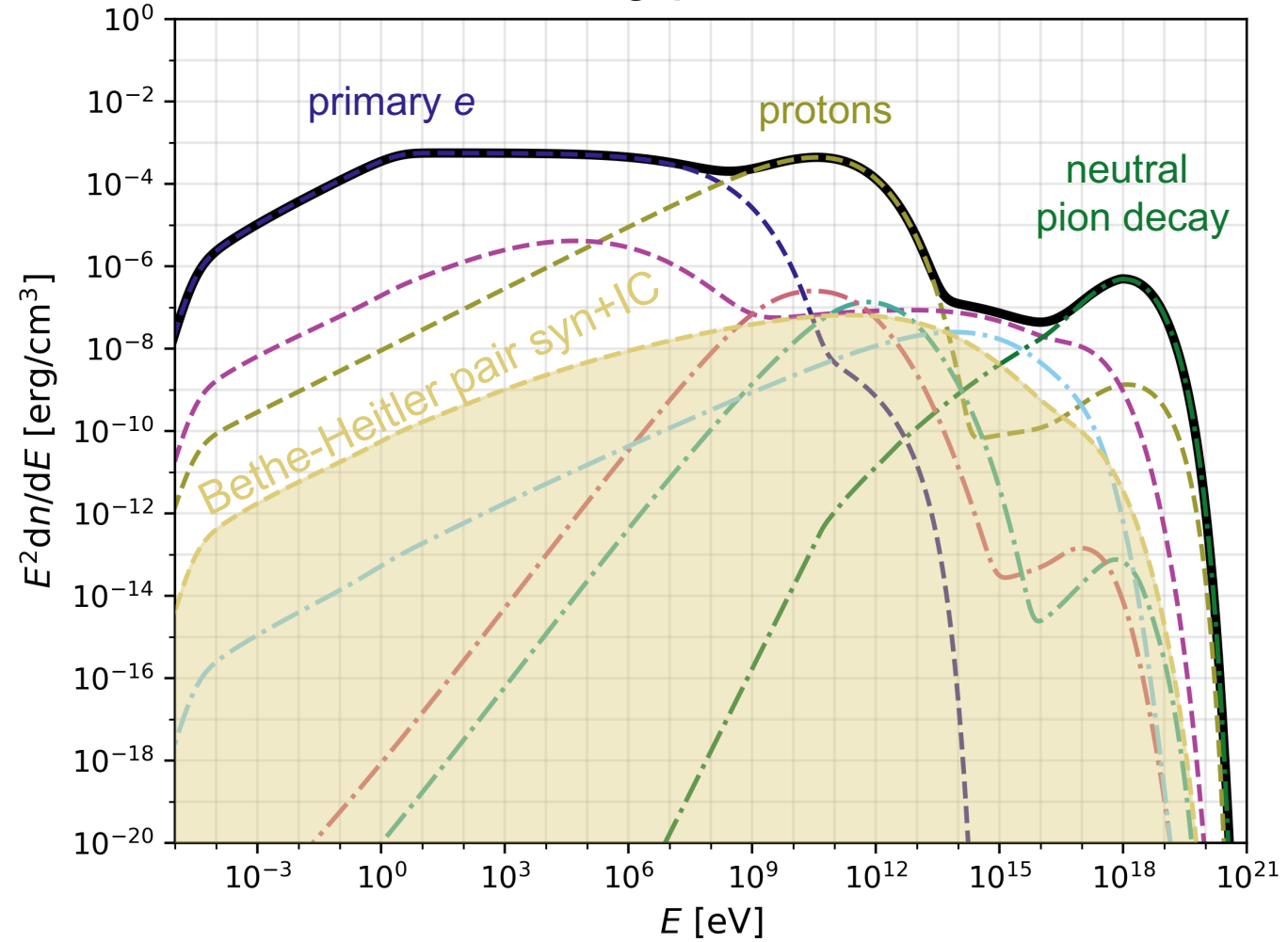


# Trackable - Bethe-Heitler : $p\gamma \rightarrow pe^+e^-$

comoving particle SEDs

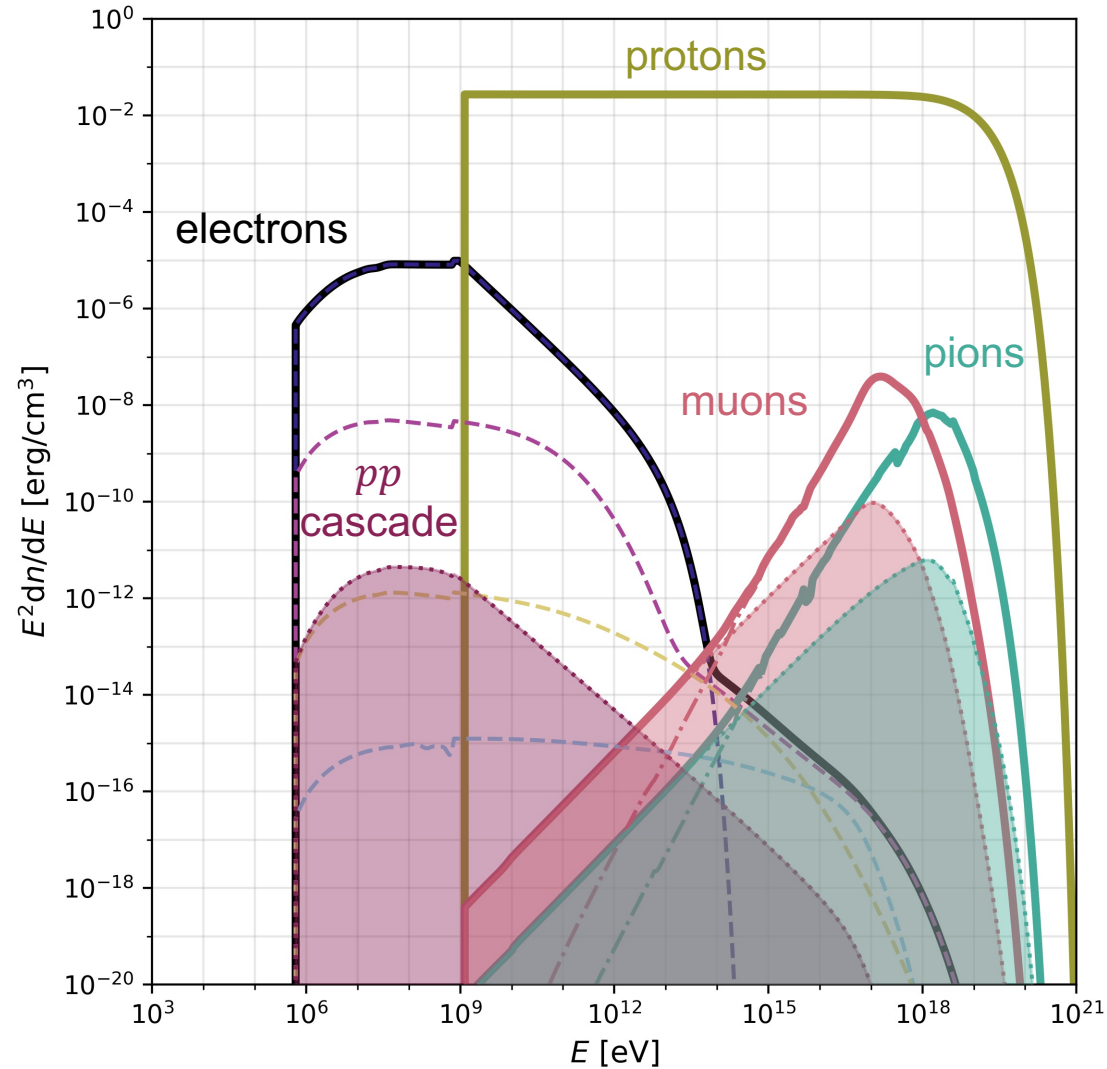


comoving photon SED

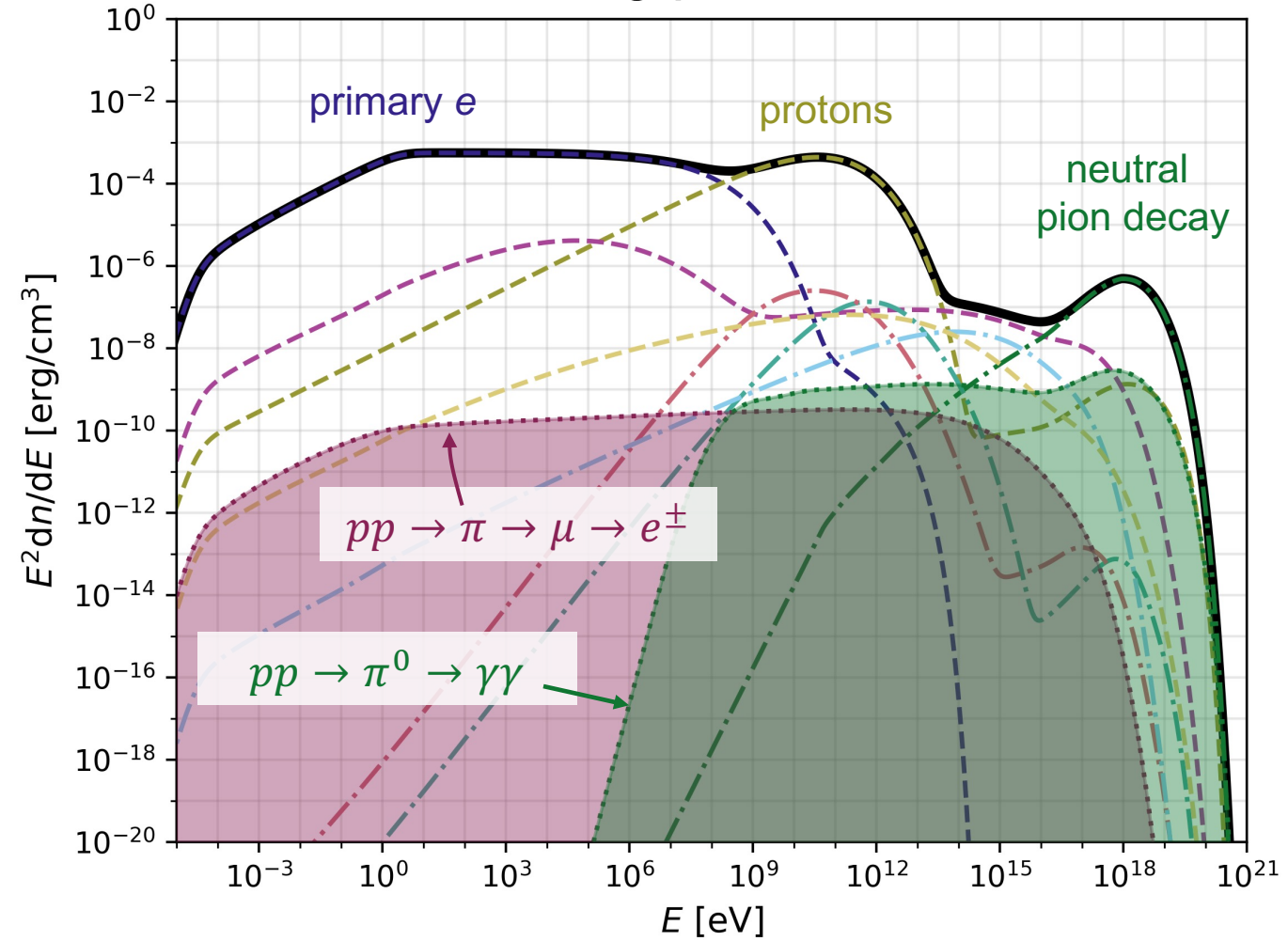


# Trackable - proton-proton : $pp \rightarrow \pi \rightarrow \mu \rightarrow e^\pm$

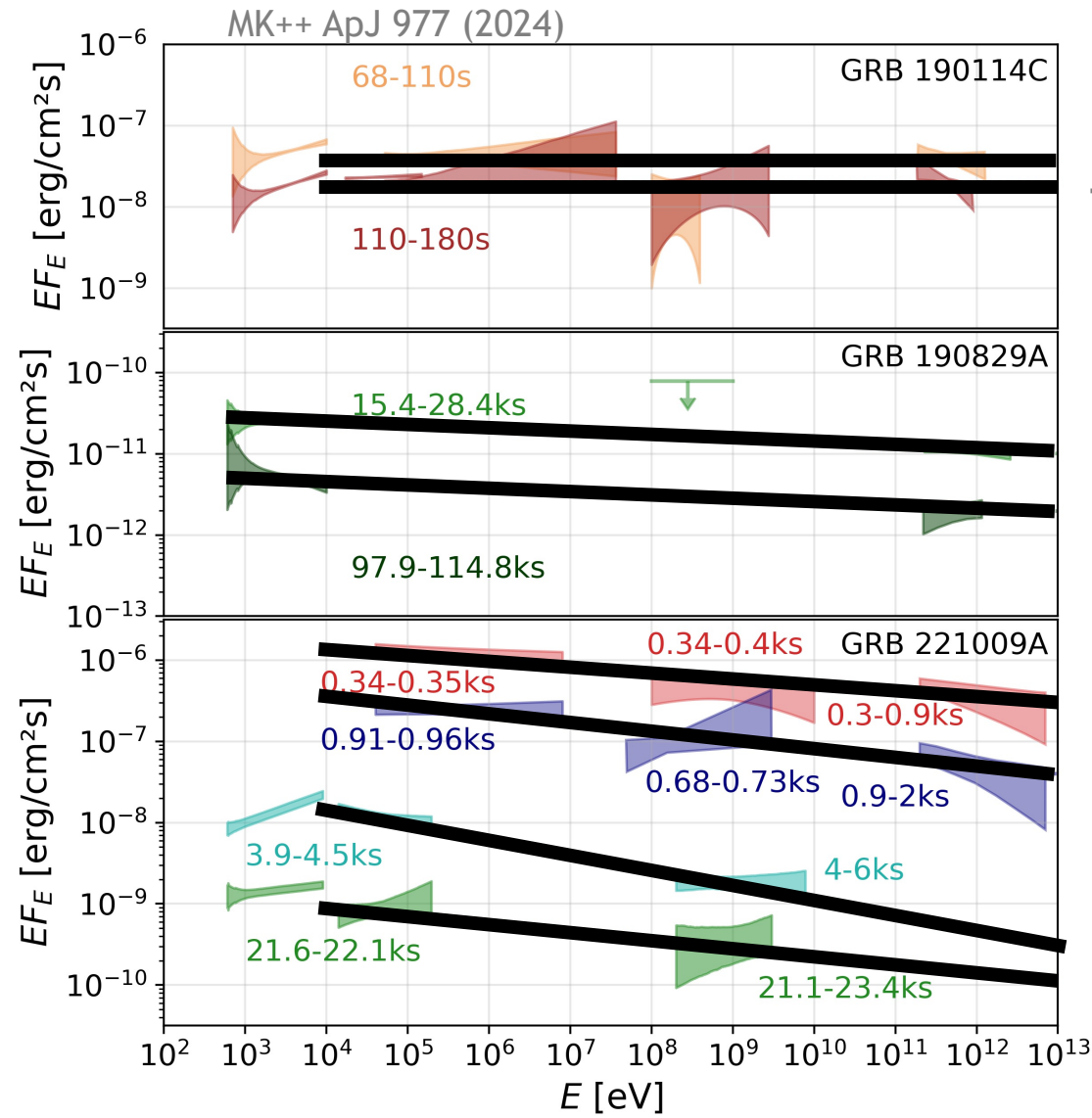
comoving particle SEDs



comoving photon SED



# Which scenarios fit GRB afterglow observations?



→ MAGIC

→ H.E.S.S.

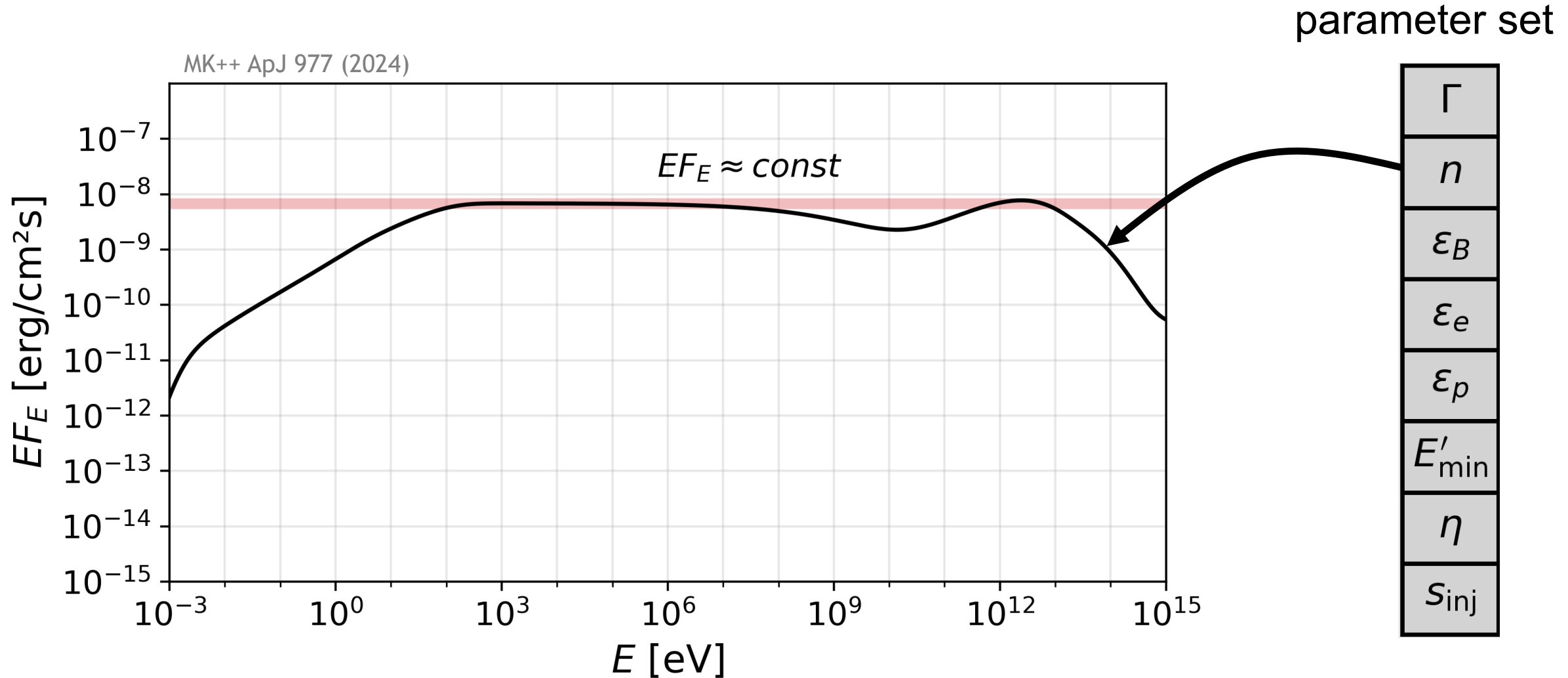
→ LHAASO



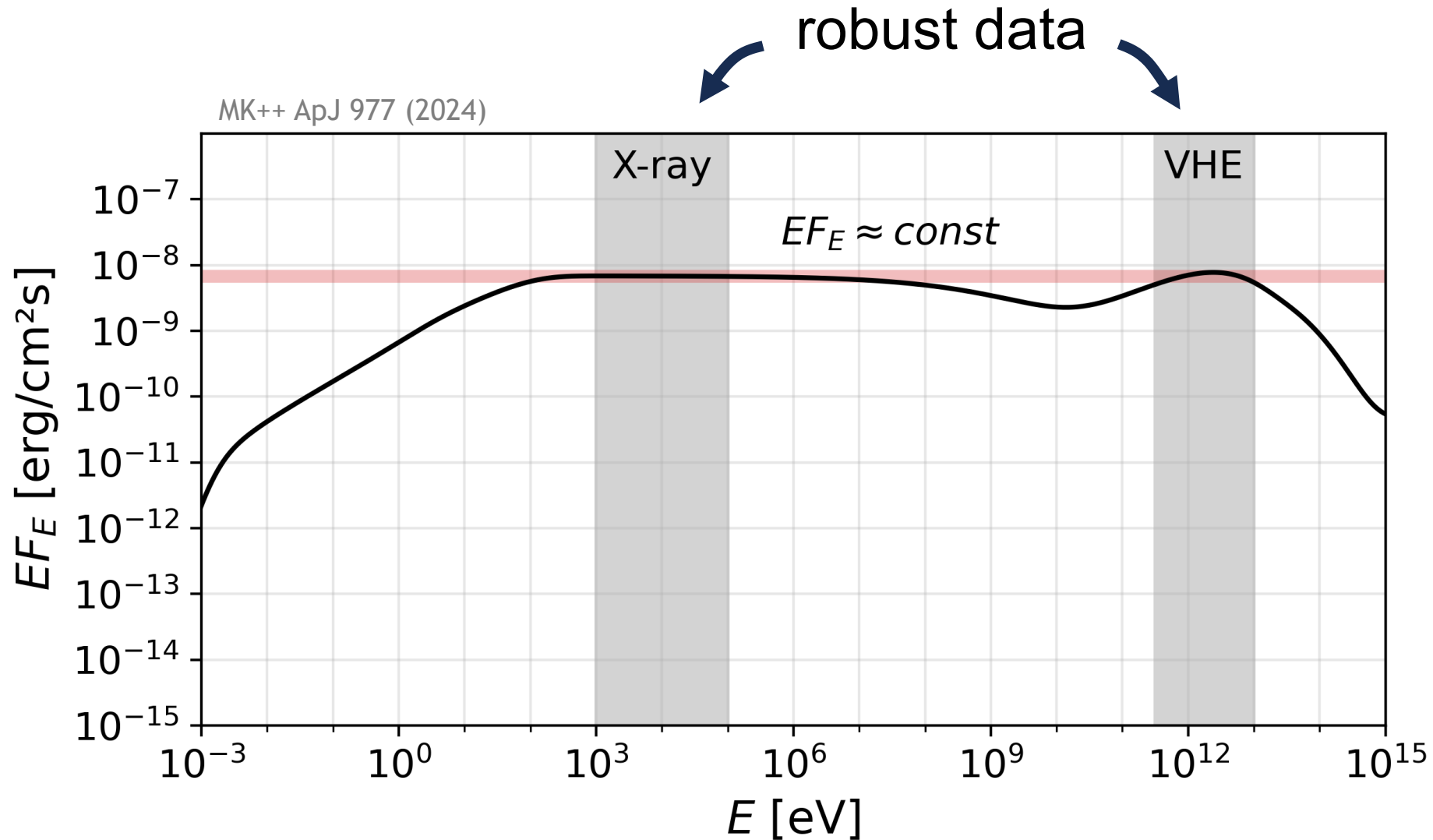
data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
 Liu++ APJL 943 (2023)  
 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)



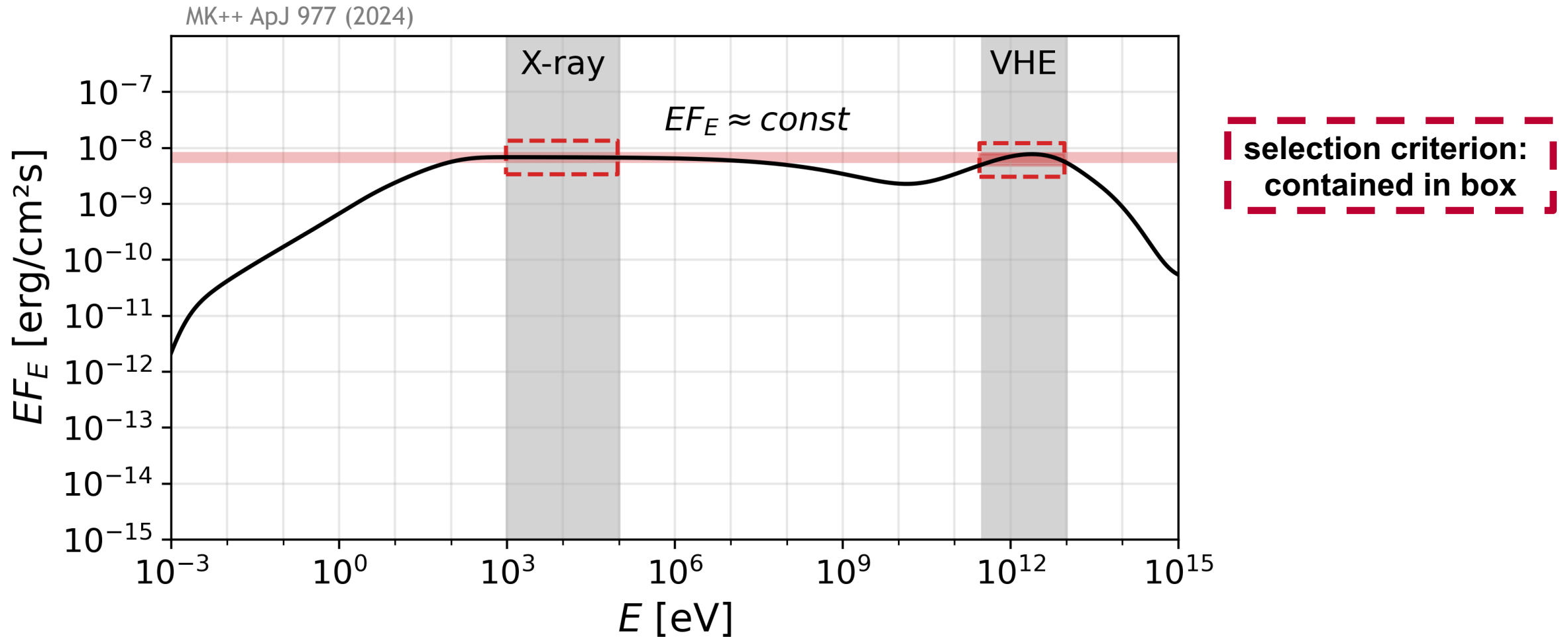
# Systematic parameter scan - selection



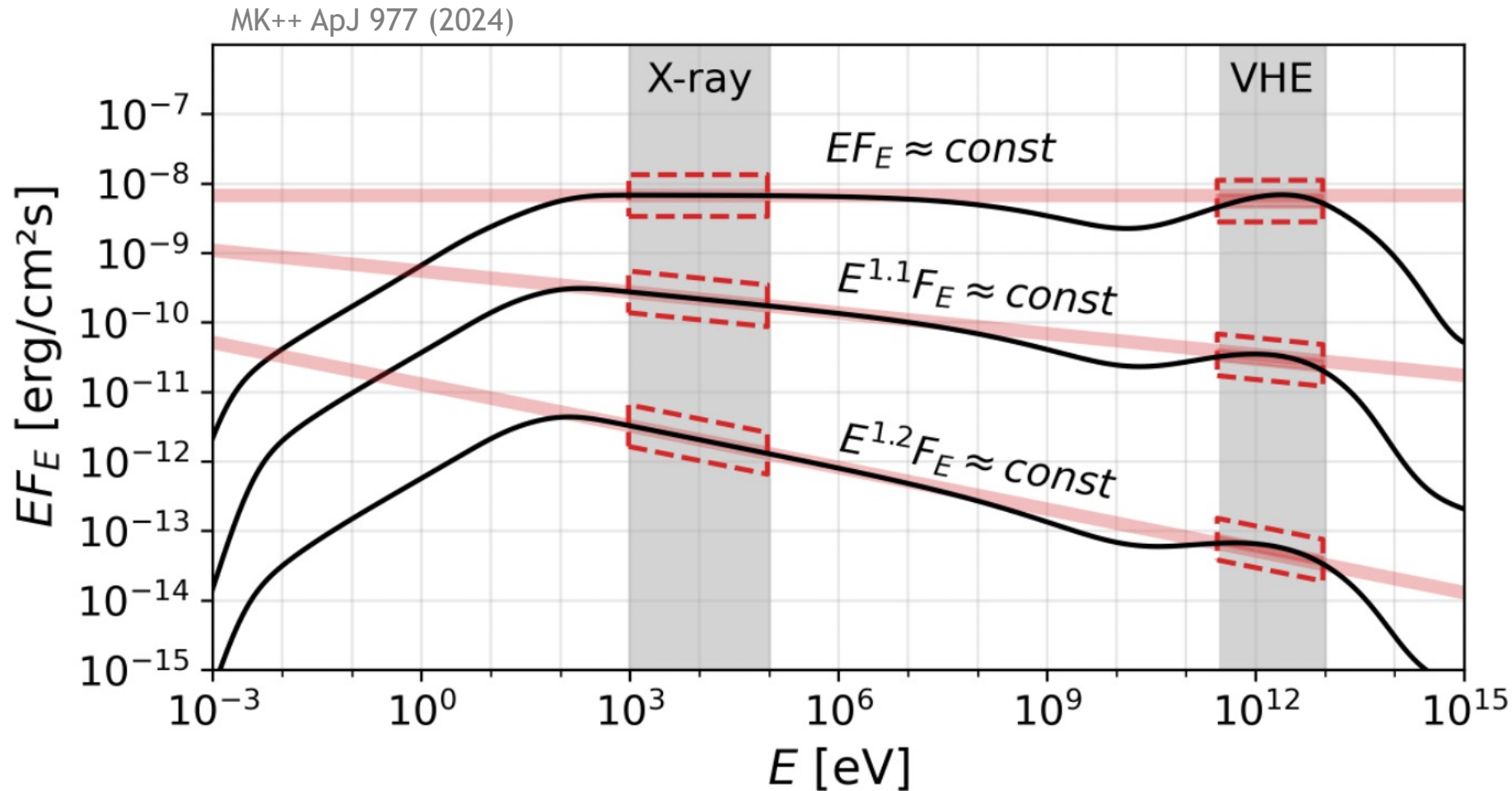
# Systematic parameter scan - selection



# Systematic parameter scan - selection



# Systematic parameter scan



spectral index

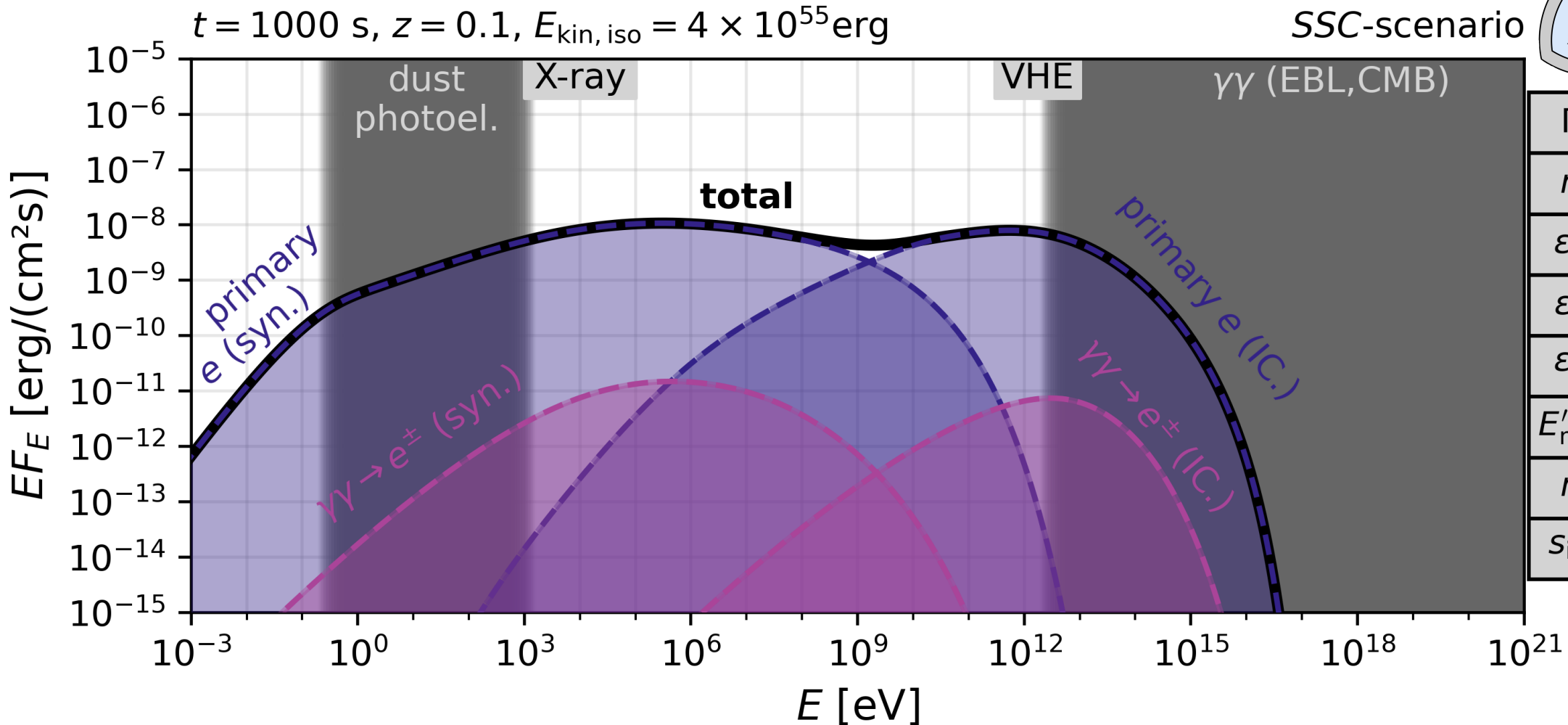
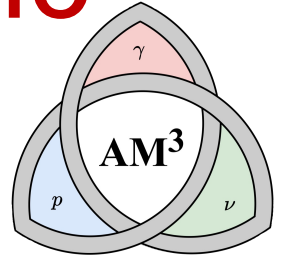
$$\gamma \approx 2$$

$$\gamma \approx 2.1$$

$$\gamma \approx 2.2$$

# Synchrotron-Self Compton (SSC) Scenario

MK++ ApJ 977 (2024)  
SSC-scenario



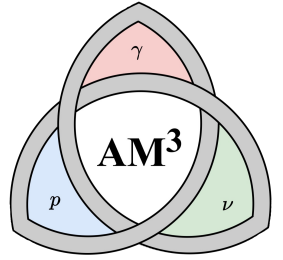
$\Gamma$	50	
$n$	1	$\text{cm}^{-3}$
$\epsilon_B$	$10^{-4}$	
$\epsilon_e$	$10^{-1.5}$	
$\epsilon_p$	0	
$E'_{\text{min}}$	$10^{9.0}$	eV
$\eta$	1	
$S_{\text{inj}}$	2.3	

→ Klein-Nishina suppression at VHE: 1) softening, 2) fine-tuned energy density

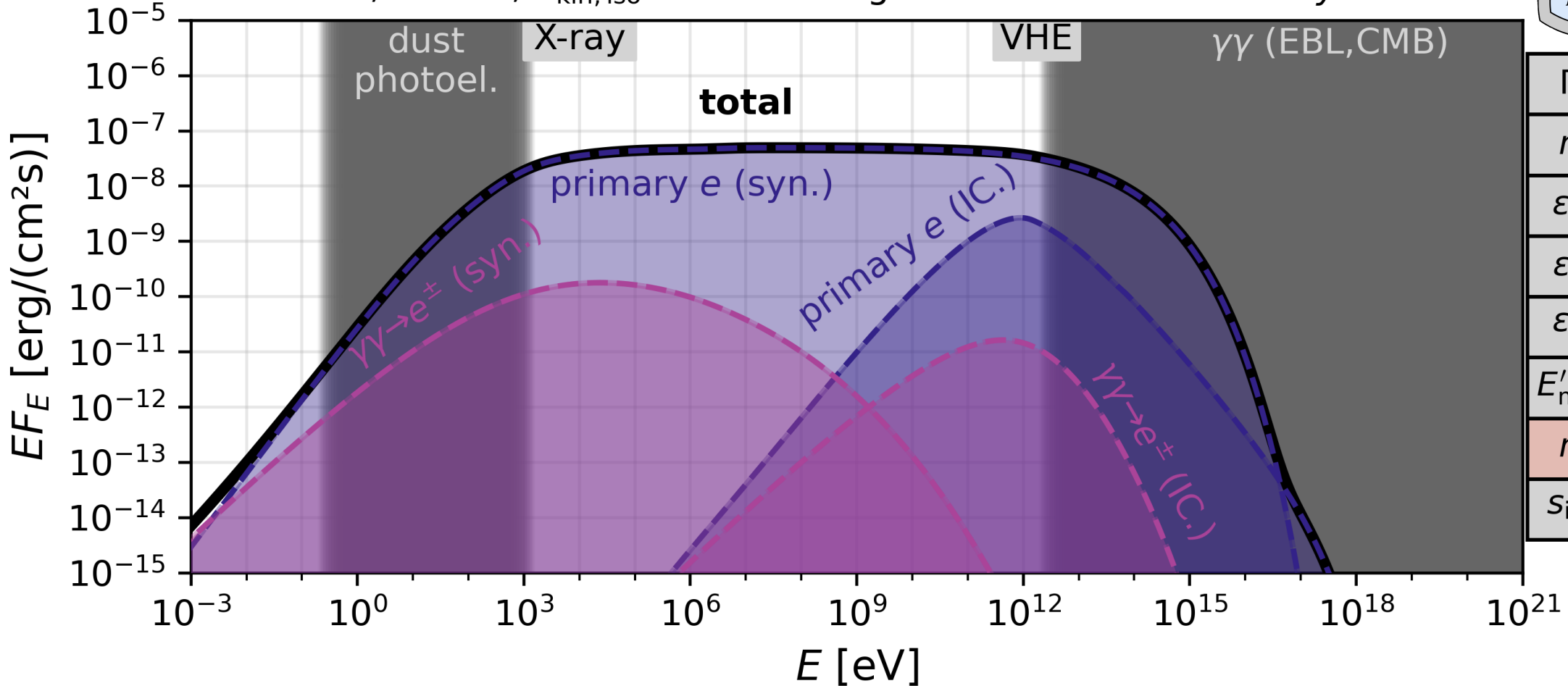
# Extended Synchrotron Scenario

MK++ ApJ 977 (2024)

Extended-syn-scenario



$t = 1000 \text{ s}, z = 0.1, E_{\text{kin, iso}} = 4 \times 10^{53} \text{ erg}$



$\Gamma$	50	
$n$	1	$\text{cm}^{-3}$
$\epsilon_B$	$10^{-3}$	
$\epsilon_e$	$10^{-1.5}$	
$\epsilon_p$	0	
$E'_{\text{min}}$	$10^{10.5}$	eV
$\eta$	$10^{-4}$	
$S_{\text{inj}}$	2	

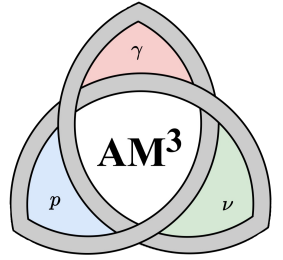
$\eta \ll 1$  (extremely fast acceleration)  $\rightarrow$  effective multi-zone parameter?

$\rightarrow$  e.g., Khangulyan++ APJ 947 (2021)

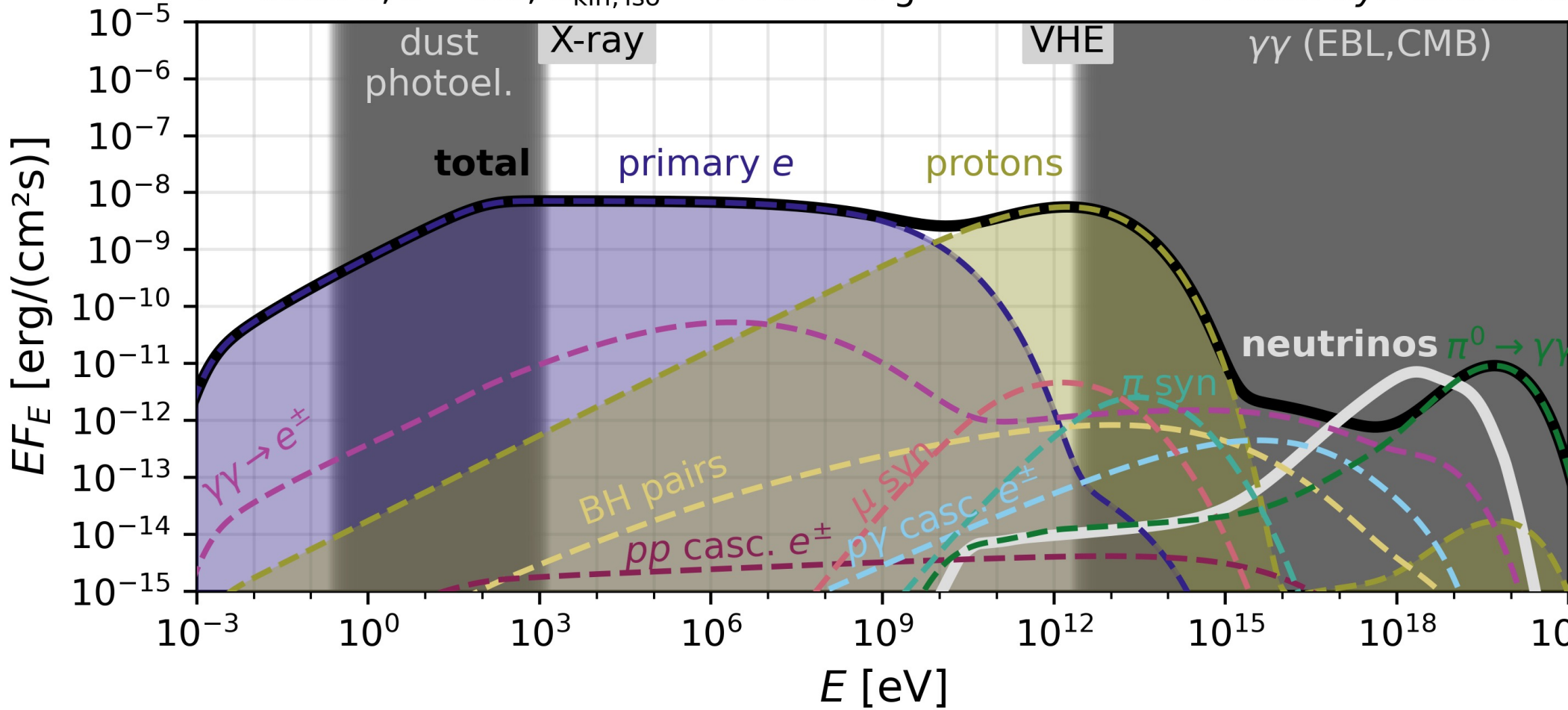
# Proton Synchrotron Scenario

MK++ ApJ 977 (2024)

Proton-syn-scenario



$t = 1000 \text{ s}, z = 0.1, E_{\text{kin, iso}} = 4 \times 10^{55} \text{ erg}$

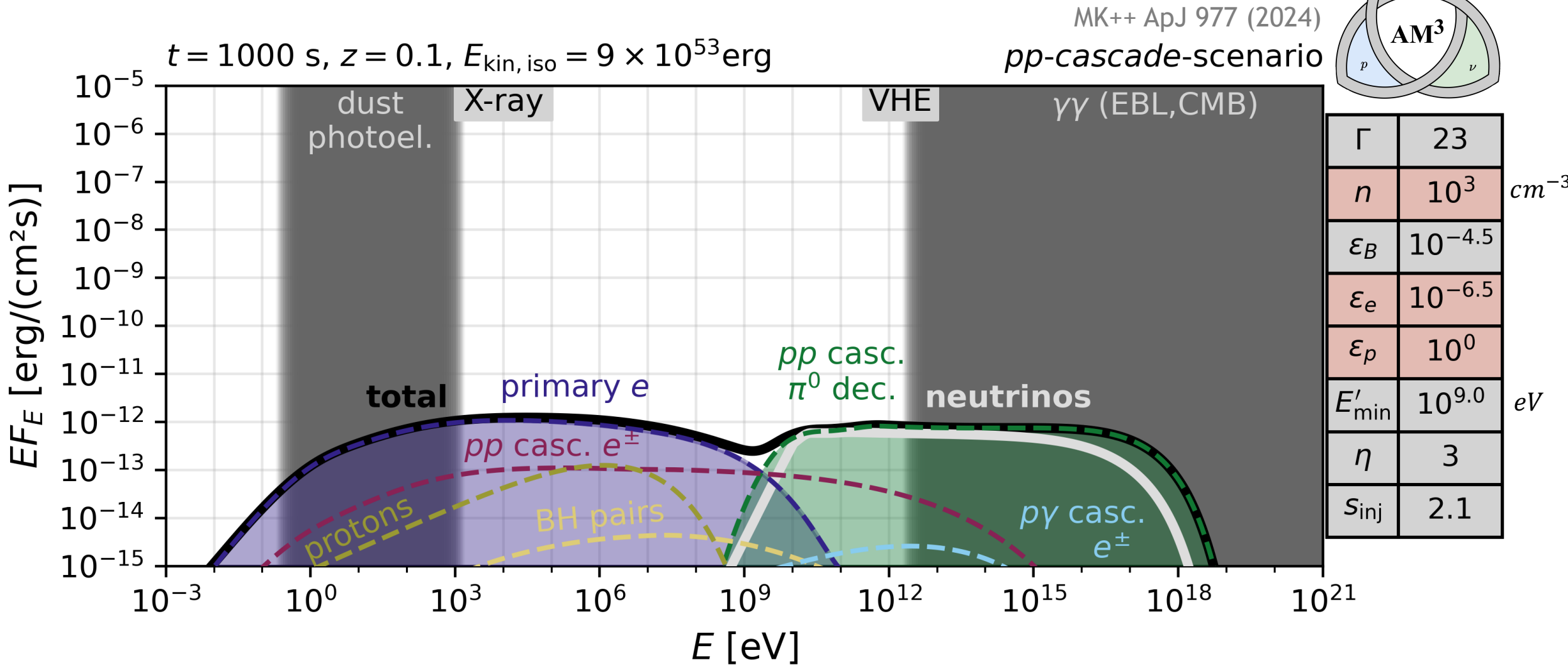


$\Gamma$	50	
$n$	$10^2$	$\text{cm}^{-3}$
$\epsilon_B$	$10^{-1}$	
$\epsilon_e$	$10^{-4.5}$	
$\epsilon_p$	$10^{-3}$	
$E'_{\text{min}}$	$10^{9.0}$	$\text{eV}$
$\eta$	1	
$S_{\text{inj}}$	2	

→ fine-tuned exponential cut-off

see also: Isravel et al. ApJ 955 (2023),  
Cao et al. Sci. Adv. 9 (2023)

# Proton-Proton Cascade Scenario



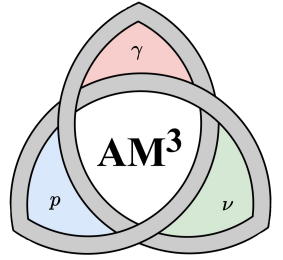
→ *pp*-interactions inefficient!



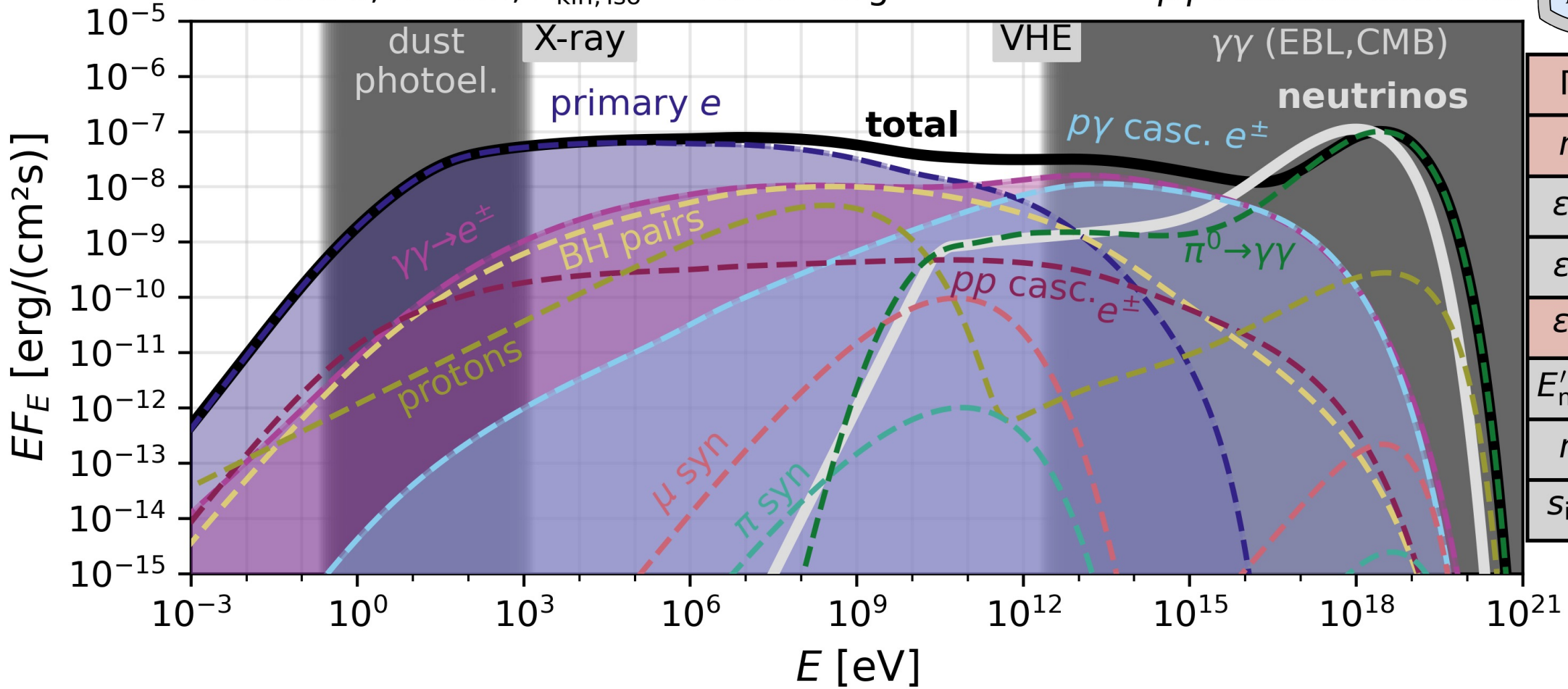
# Proton-Photon Cascade Scenario

MK++ ApJ 977 (2024)

*pγ*-cascade-scenario



$t = 1000 \text{ s}, z = 0.1, E_{\text{kin, iso}} = 4 \times 10^{56} \text{ erg}$



$\Gamma$	50	
$n$	$10^3$	$\text{cm}^{-3}$
$\epsilon_B$	$10^{-5}$	
$\epsilon_e$	$10^{-4.5}$	
$\epsilon_p$	$10^0$	
$E'_{\text{min}}$	$10^{9.5}$	$\text{eV}$
$\eta$	1	
$S_{\text{inj}}$	2	

→ extreme energy + density requirements

# Large energy requirements of $10^{57} \text{ erg}$ ?

massive star collapse

→ accreted mass  $M \approx 10M_{\odot}$

→  $\varepsilon_{\text{kin}} \approx 10\%$  converted to kinetic energy of outflow

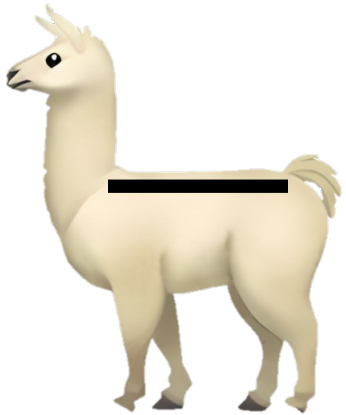
→ into cone with opening angle  $\theta = 3^{\circ}$

→  $E_{\text{kin,iso}} \approx 10^{57} \text{ erg} \left( \frac{M}{10M_{\odot}} \right) \left( \frac{\varepsilon_{\text{kin}}}{0.1} \right) \left( \frac{3^{\circ}}{\theta} \right)^2$

→ **extreme, but not crazy!**

# Scenarios

**observations:**  
something  
close to



electrons



SSC



Extended syn



Proton syn



$pp$ -cascade



$p\gamma$ -cascade

electrons  
+ protons

**advantages:**

**limitations:**

bright

Klein-Nishina suppression

bright  
simple

$\eta \ll 1$  (super Bohm)

bright

exponential cut-off

extends  
to  $>10\text{TeV}$

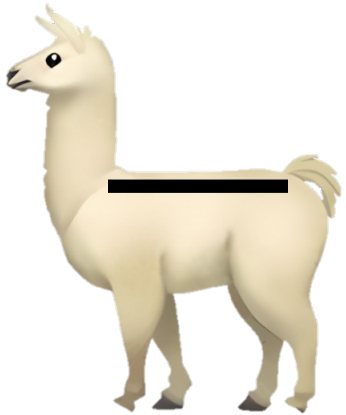
inefficient

bright

extreme energy + density

# Scenarios

observations:  
something  
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electrons  
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SSC

Extended syn

Proton syn

$pp$ -cascade

$p\gamma$ -cascade

advantages:

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extends  
to  $>10\text{TeV}$

bright

limitations:

Klein-Nishina suppression

$\eta \ll 1$  (super Bohm)

exponential cut-off

inefficient

extreme energy + density

→ **no scenario really  
convincing**  
→ **multi-zone?**

# GRB afterglows to power UHECRs?

UHECRs:  $E_p > 10^{18} eV$

→  $p$ -syn,  $p\gamma$ -cascade

total energy?

→ assume all UHECRs powered by GRB afterglows of same type

→ at rate  $\sim 1 \text{ Gpc}^{-3} \text{ yr}^{-1}$

→ total required power:  $\sim 10^{53} \frac{\text{erg}}{\text{Gpc}^3 \text{ yr}}$

→ required energy per GRB:

$$E_{\text{UHECR,iso}} \approx 10^{53} \text{ erg} \approx \varepsilon_{\text{esc}} f_{\text{bol}} \varepsilon_p E_{\text{kin,iso}}$$

→ **compatible with powering the UHECRs**

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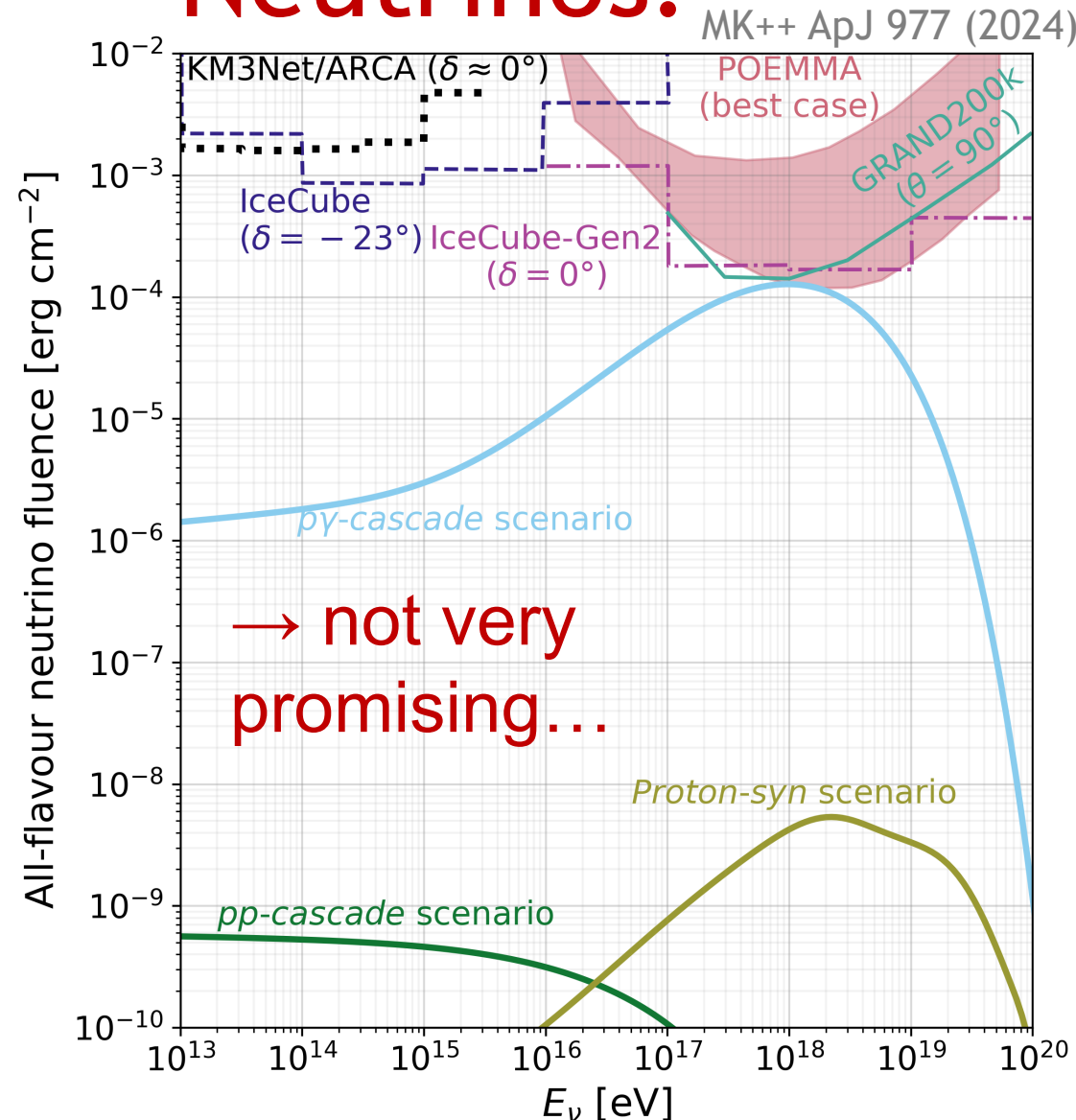
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→ required energy per GRB:

$$E_{\text{UHECR,iso}} \approx 10^{53} \text{ erg} \approx \varepsilon_{\text{esc}} f_{\text{bol}} \varepsilon_p E_{\text{kin,iso}}$$

→ **compatible with powering the UHECRs**

# Neutrinos?



rough estimate ( $t \times E F_E$ ) against optimistic scenarios

# Take Home

<https://am3.readthedocs.io/en/latest/>

[contact-am3@desy.de](mailto:contact-am3@desy.de)



<https://gitlab.desy.de/am3/am3>

**AM<sup>3</sup>**: astrophysical multi-messenger modelling

→ fast, modular, C++/Python, documented

→ public: [Klinger et al. ApJS 275 4 \(2024\)](#)

New **GRB afterglow** MWL spectra up to TeV energies

→ challenge single zone models

→ even when including lepto-hadronic scenarios

- consistent with UHECR limits, low neutrino fluences

→ time to depart towards multizone

→ [Klinger et al. ApJ 977 2 \(2024\)](#)

# Take Home

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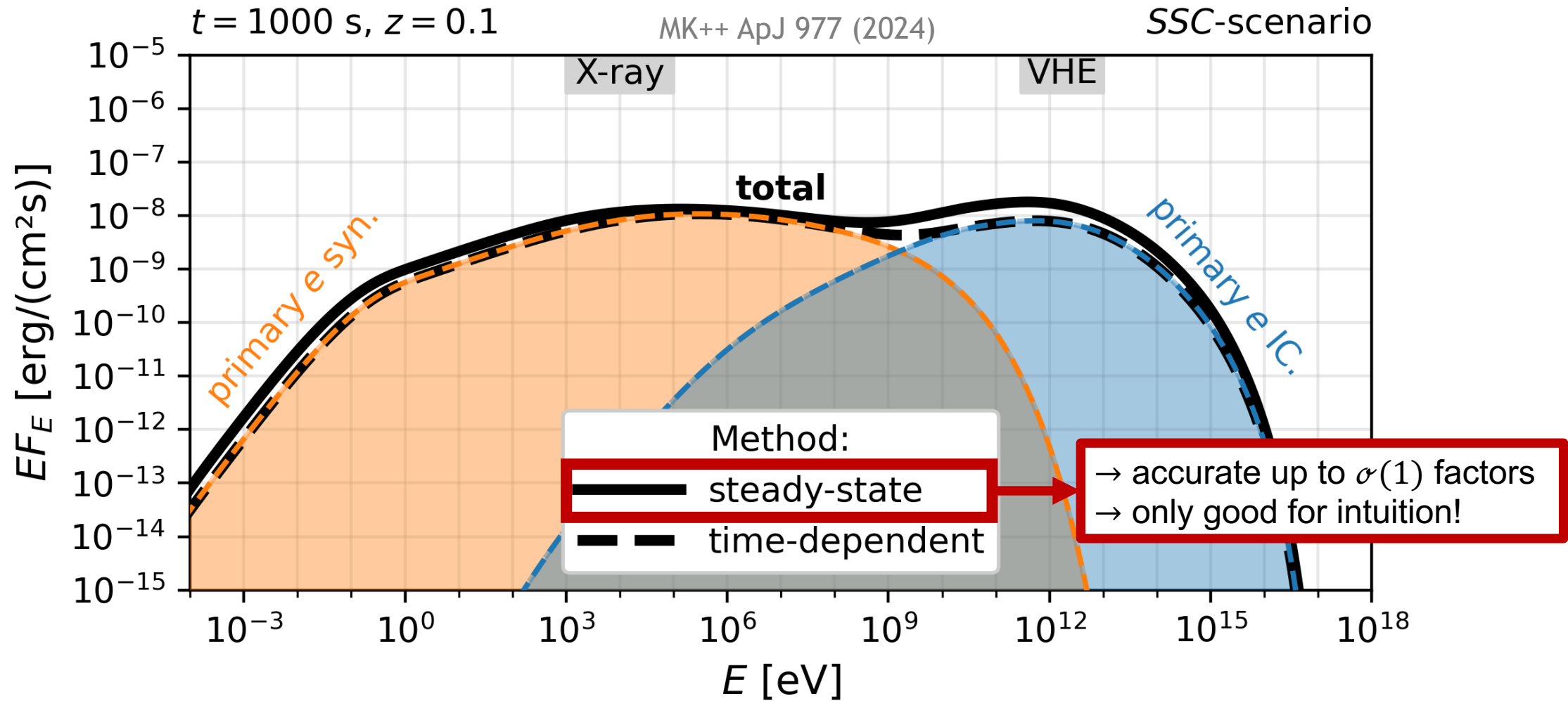
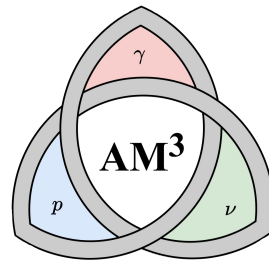
→ [Klinger et al. ApJ 977 2 \(2024\)](#)

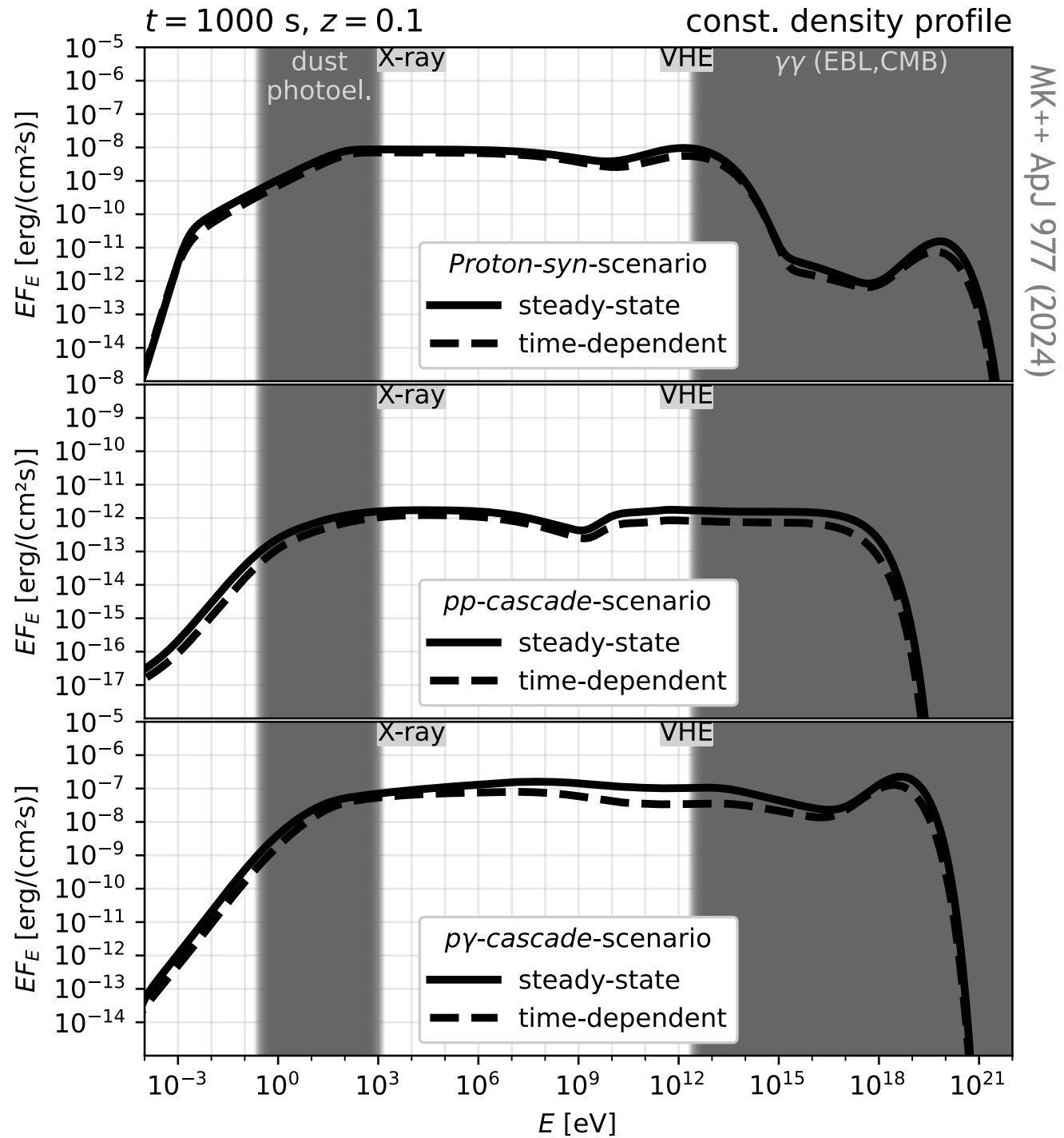
**Thank you for your attention!**



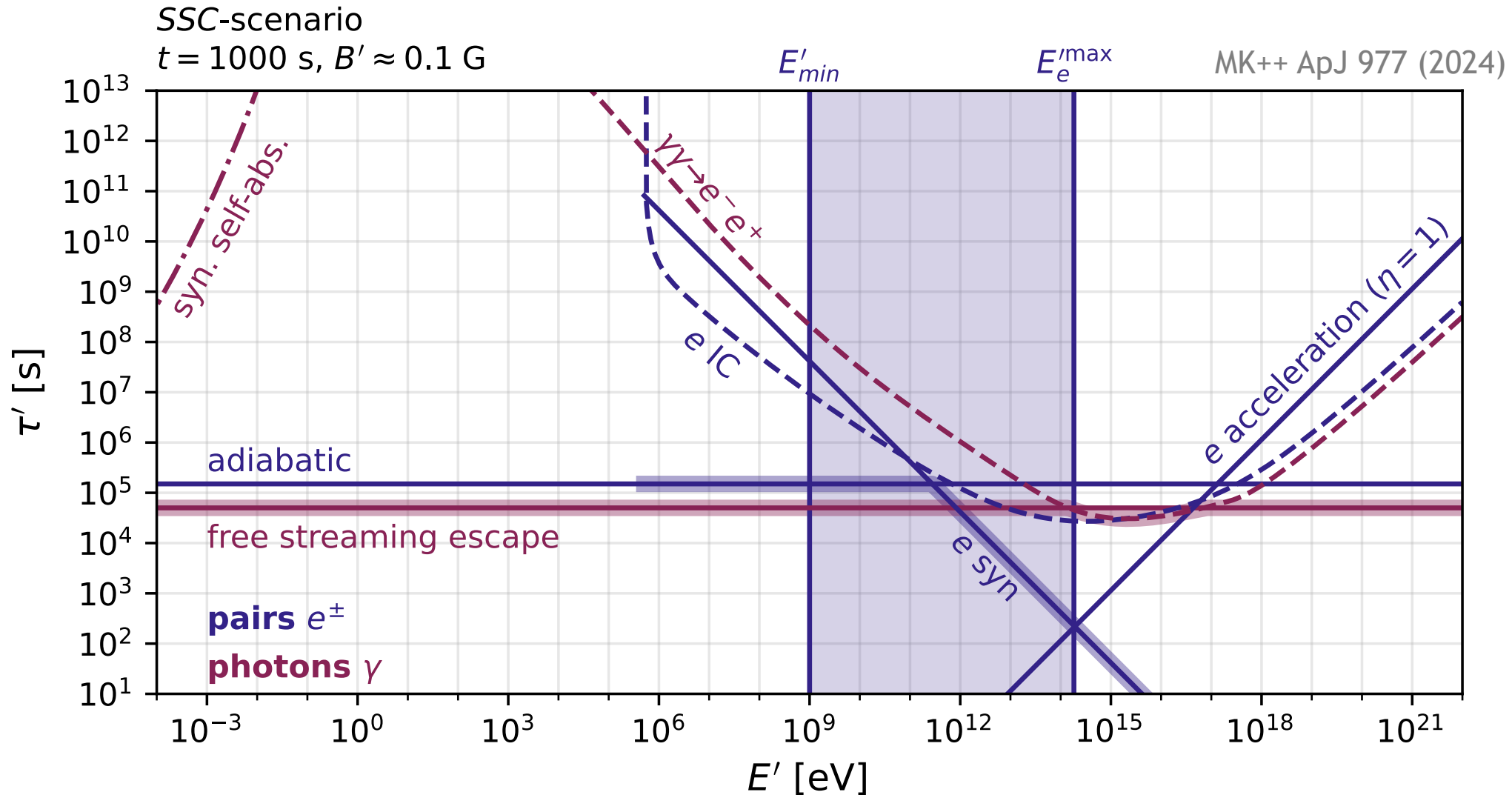
**BACKUP**

# Time-dependent $\approx$ quasi-steady state

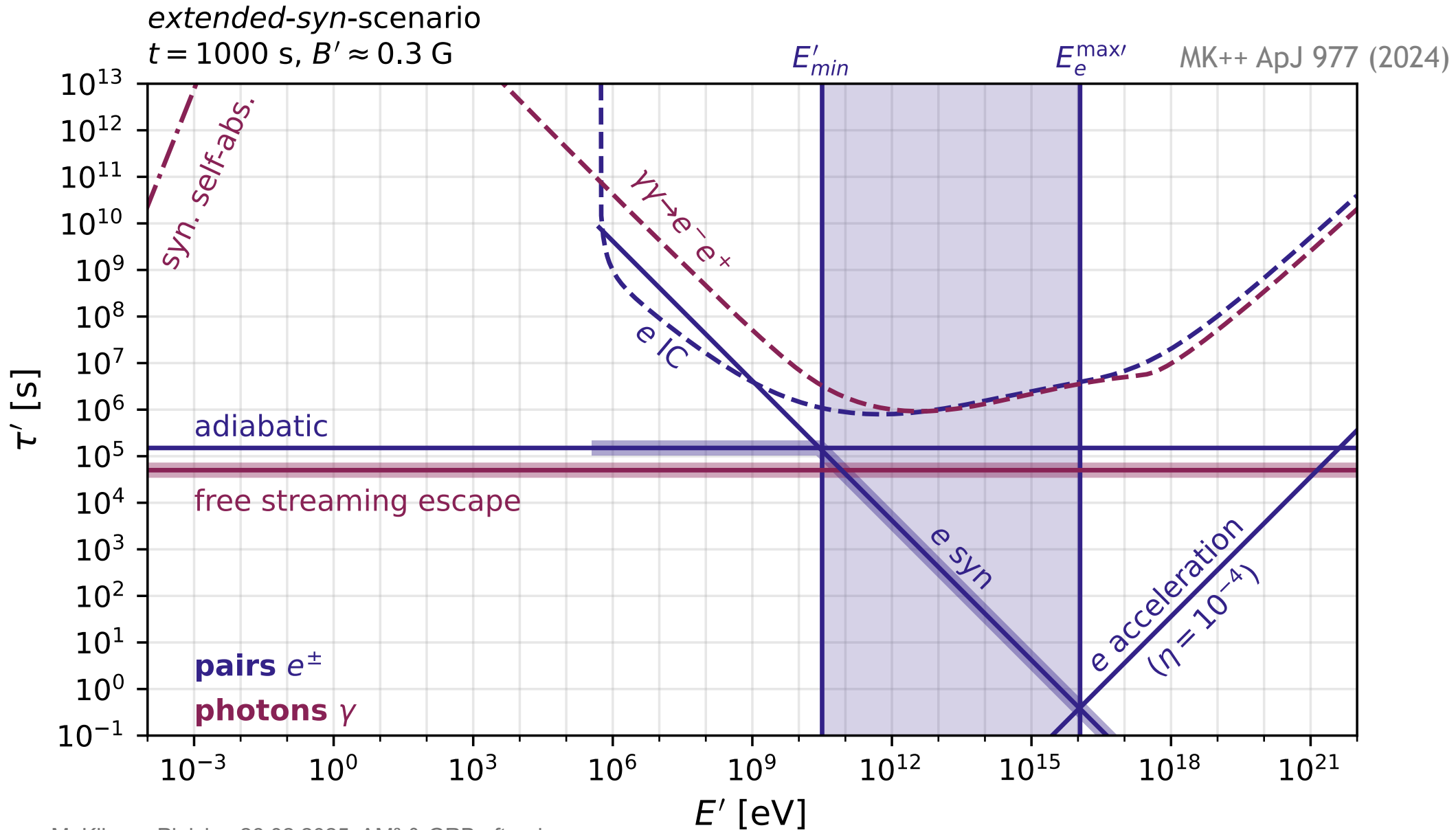




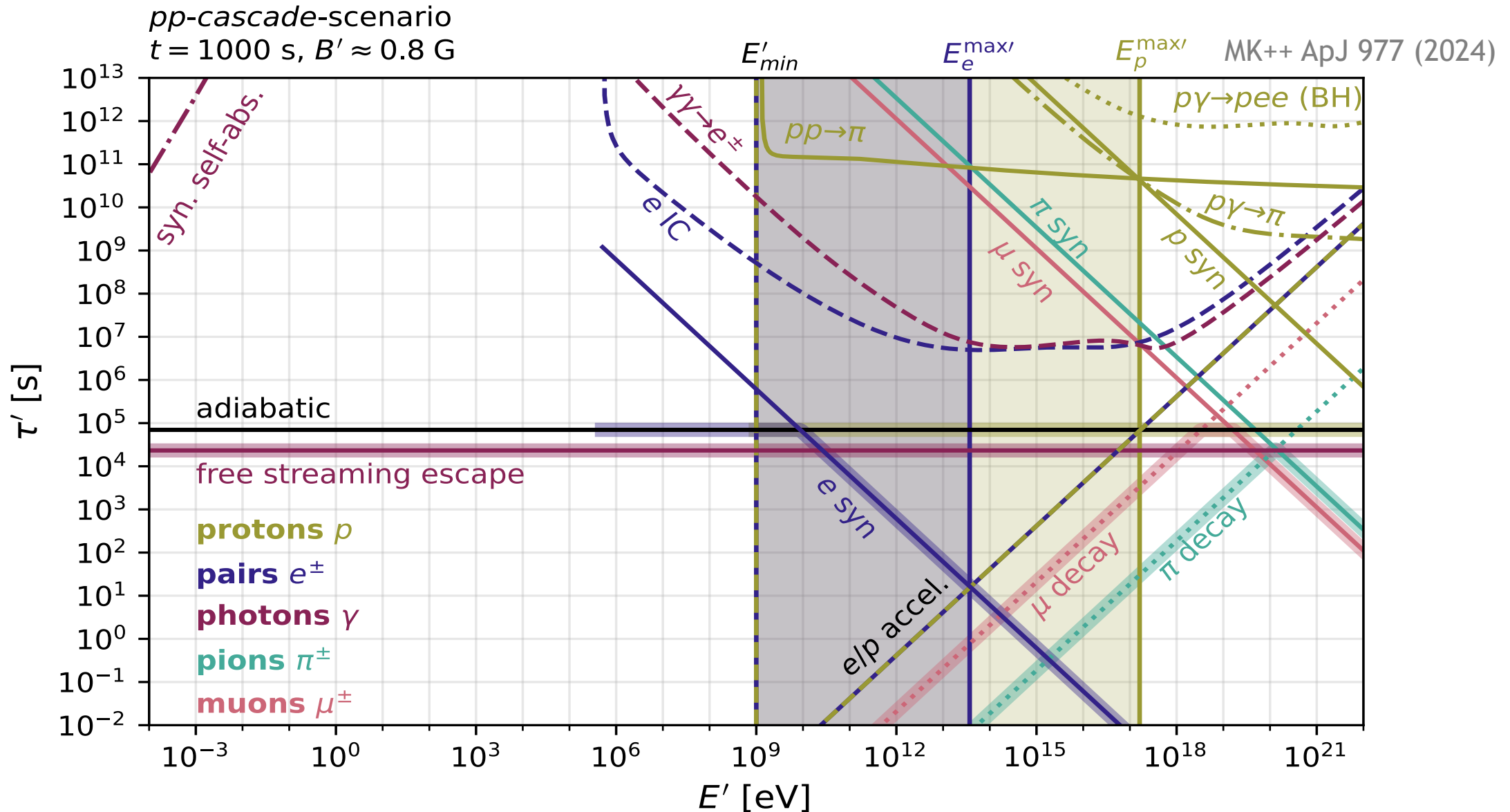
# Time scales - SSC scenario



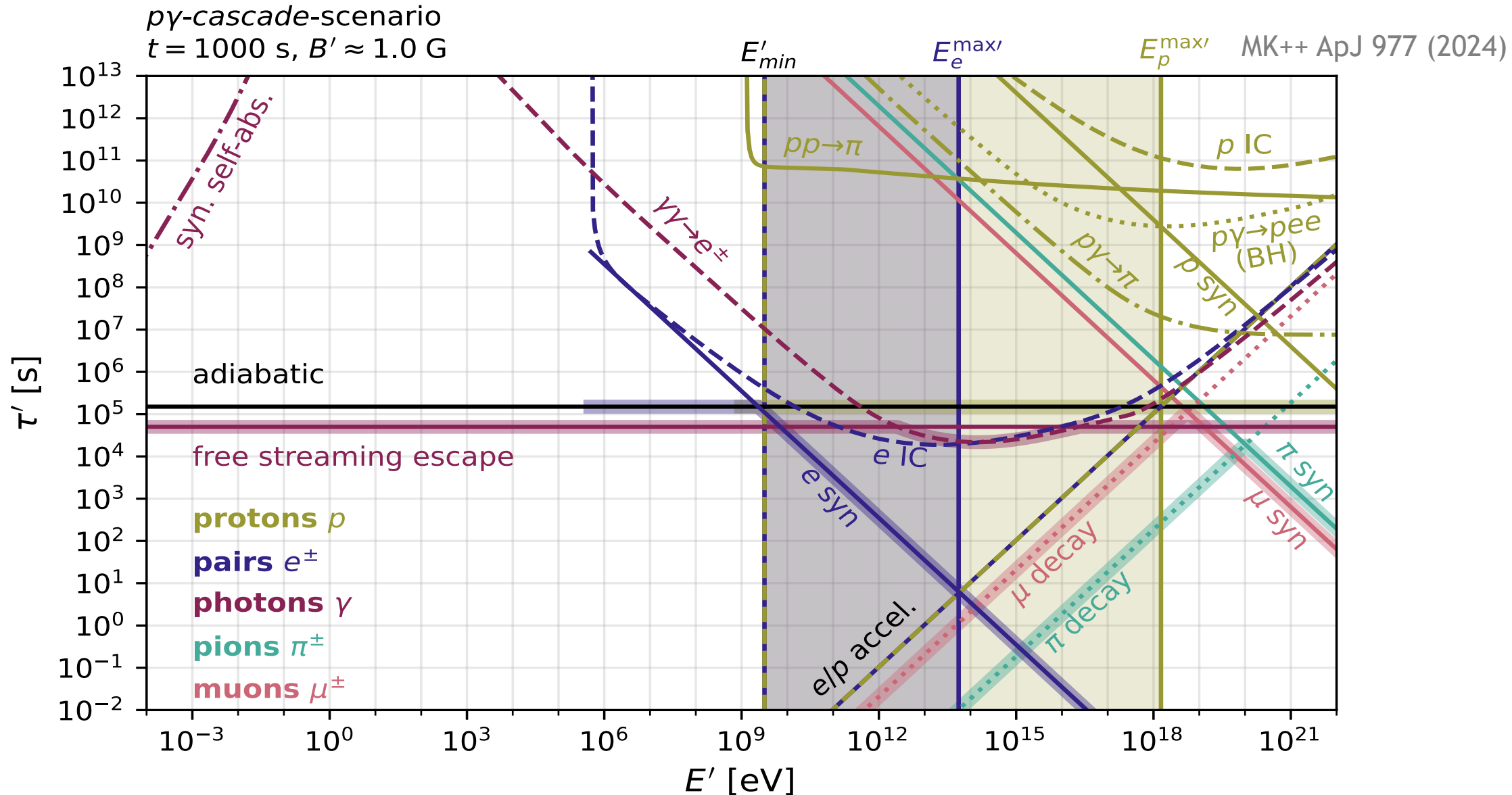
# Time scales - extended syn scenario



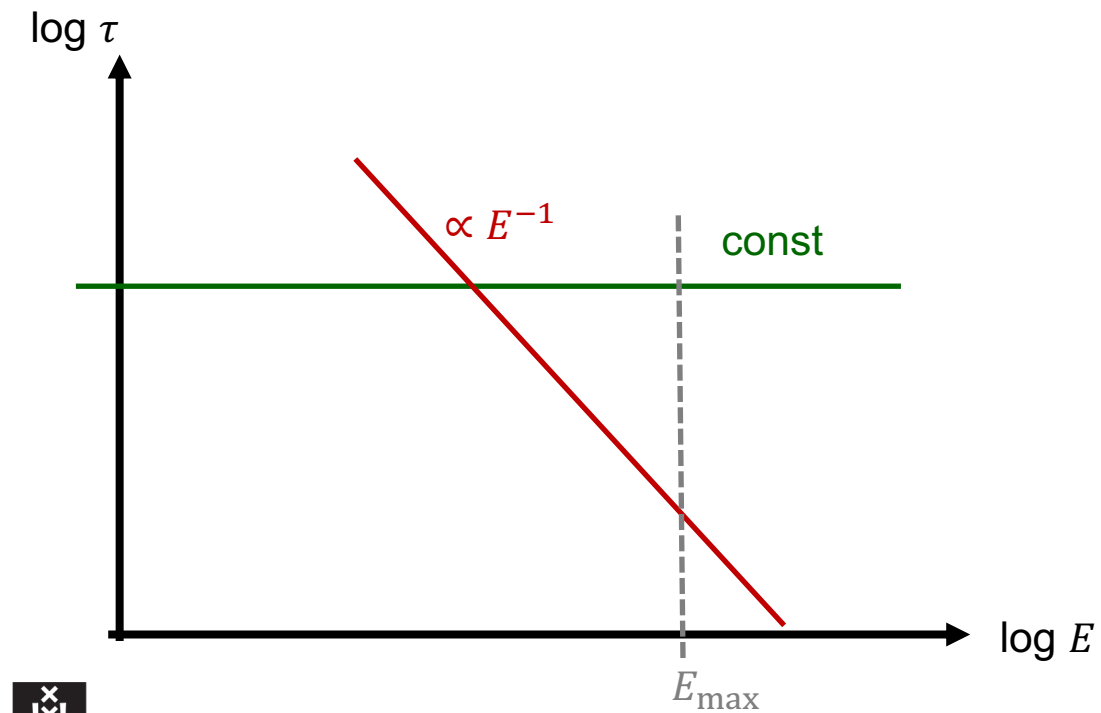
# Time scales - $pp$ -cascade scenario



# Time scales - $p\gamma$ -cascade scenario

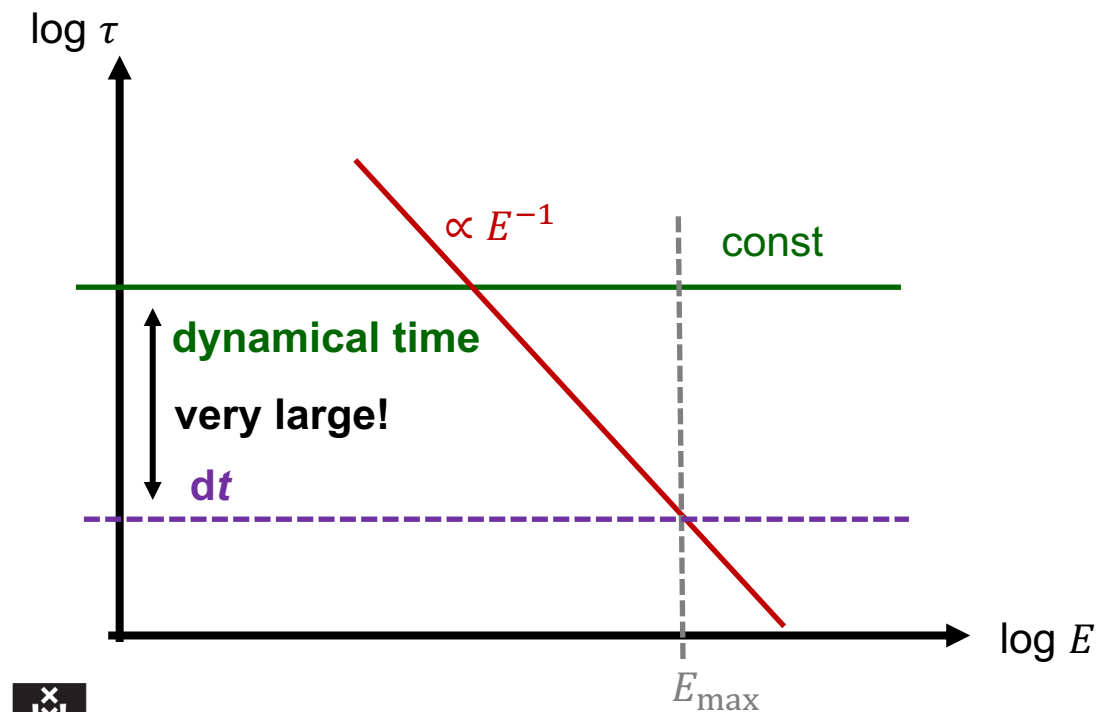


# Evolve the particle densities

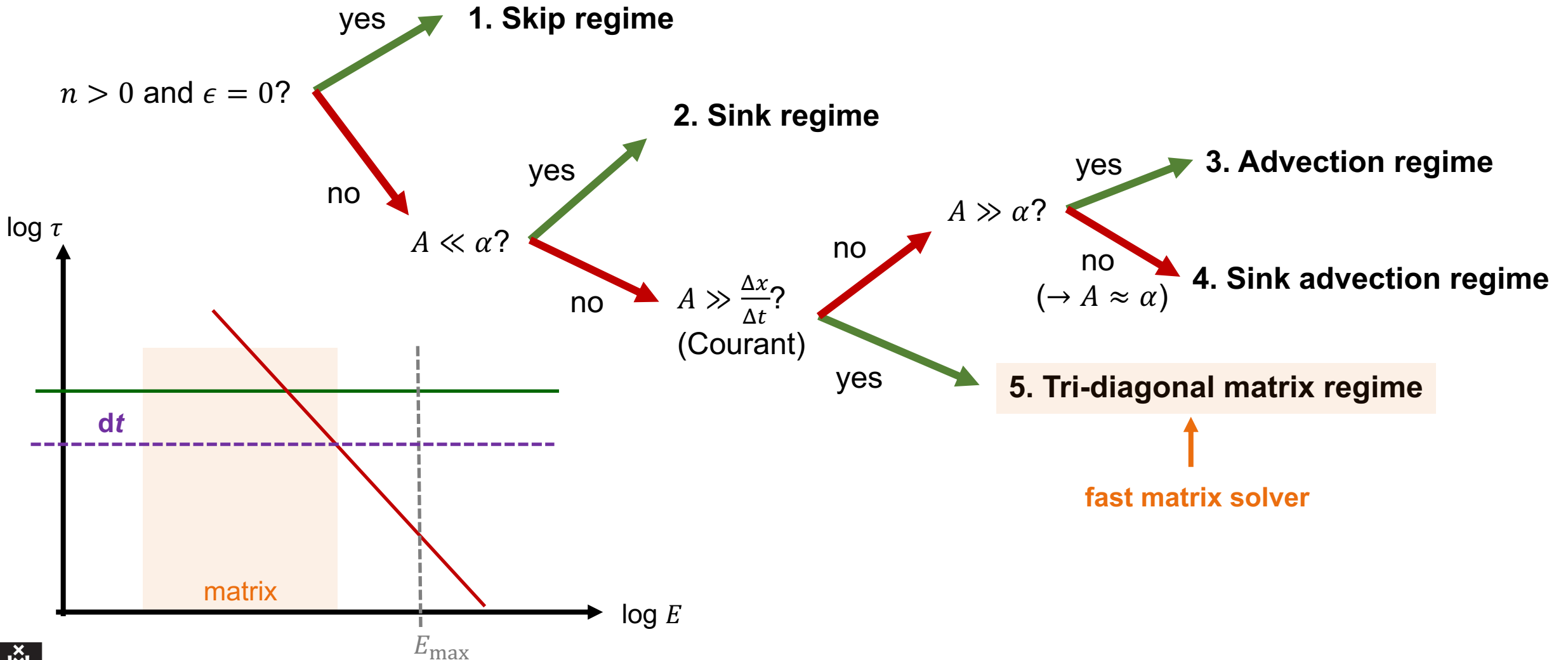




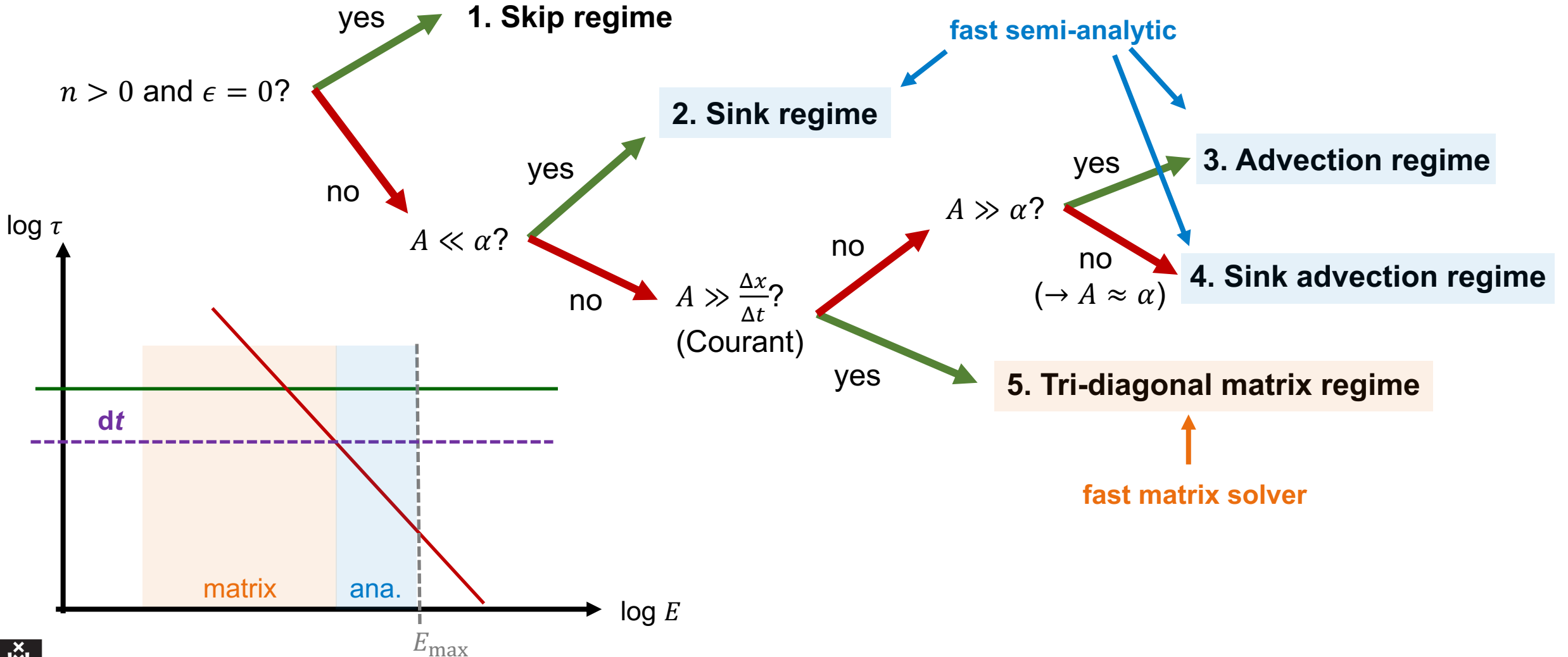
# Evolve the particle densities



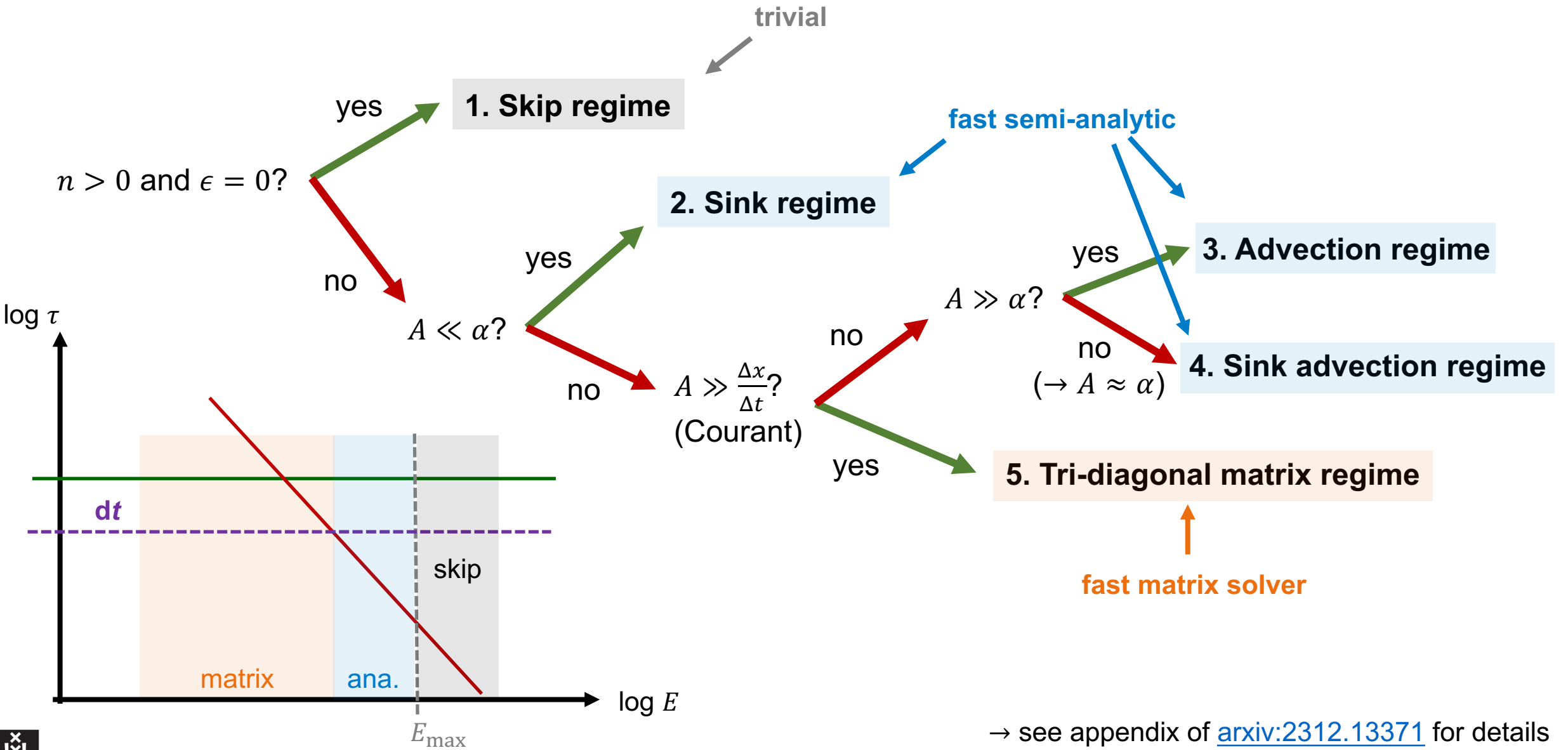
# Evolve the particle densities



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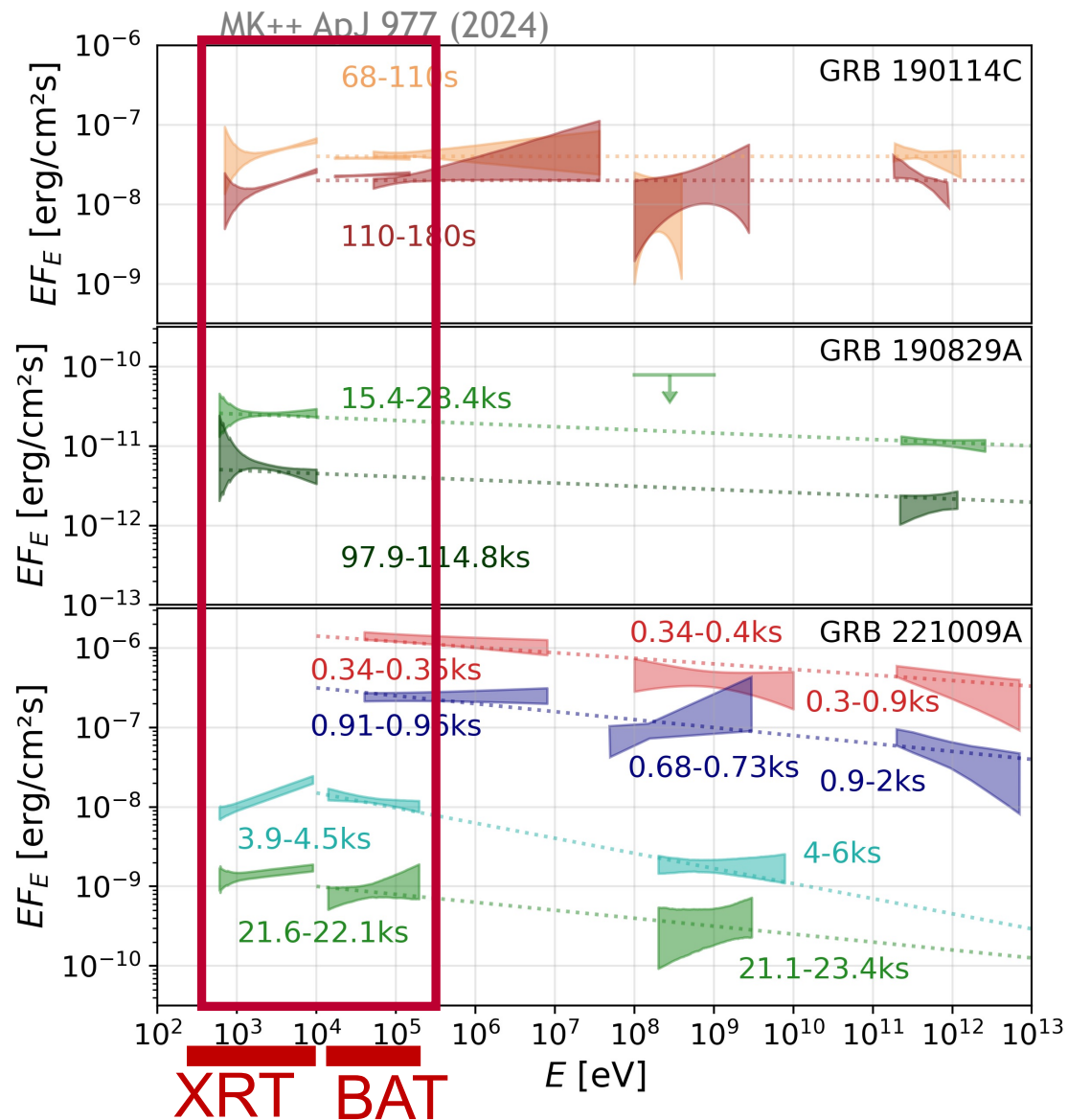


# Evolve the particle densities

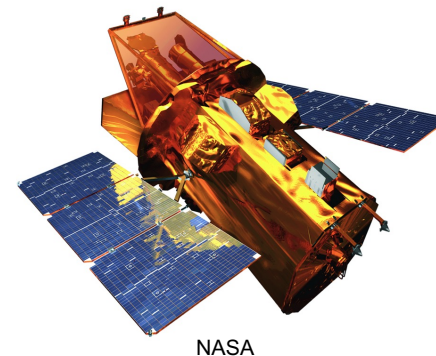


→ see appendix of [arxiv:2312.13371](https://arxiv.org/abs/2312.13371) for details

# GRB afterglows detected at X-rays!

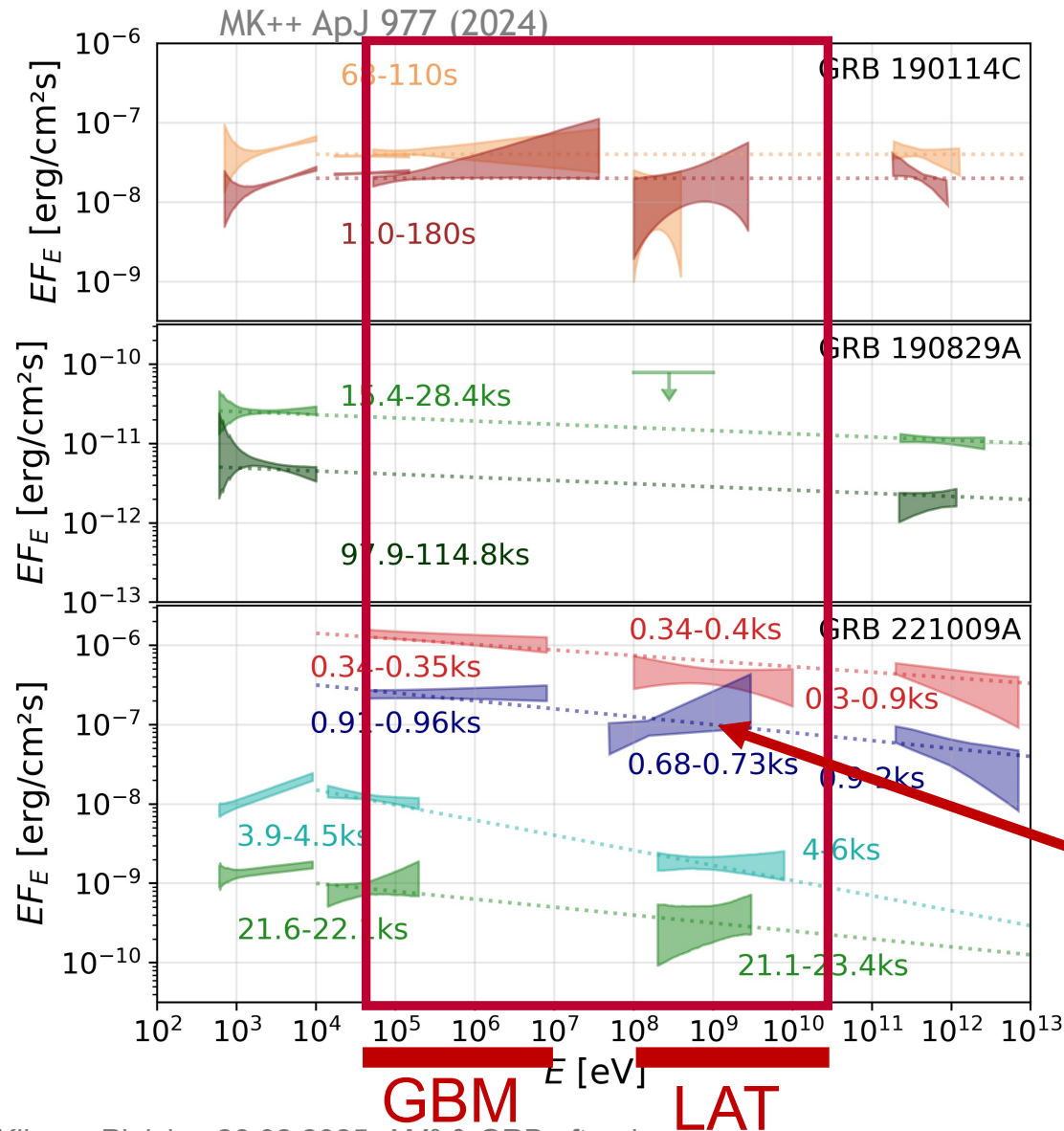


## Swift satellite

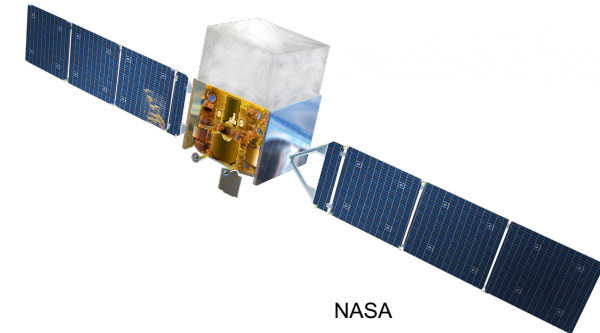


data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
 Liu++ APJL 943 (2023)  
 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)

# GRB afterglows detected at HE!



## Fermi satellite



## AGILE GRID

data from:  
 MAGIC Nature 575 (2019)  
 Swift+Fermi ApJ 890 (2020)  
 MK++ MNRAS 520 (2023)  
 H.E.S.S. Science 372 (2021)  
 Zhang++ ApJL 956 (2023)  
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 Tavani++ ApJL 956 (2023)  
 LHAASO Science 380 (2023)  
 MK++ MNRAS 529L (2024)