



Image from VectorStock.com/7932032

MWL Fitting at the Counts Level

Marc Klinger*, Donggeun Tak, Andrew Taylor, Sylvia Zhu

18.05.2022

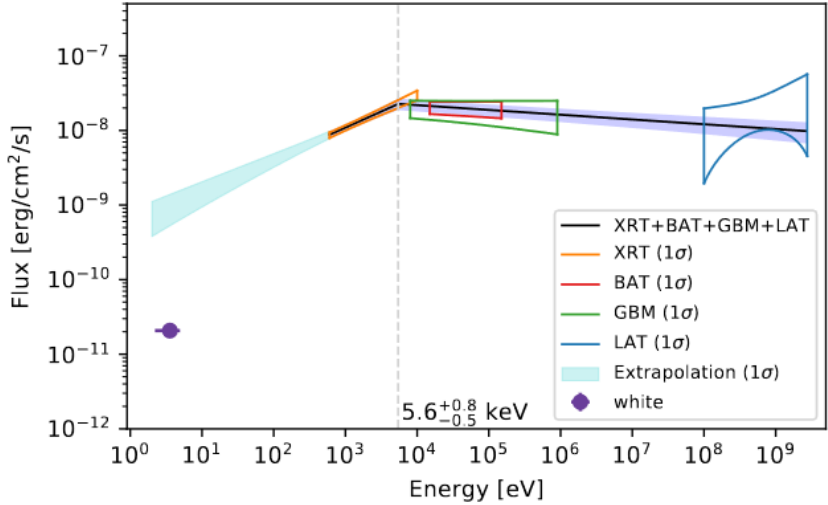
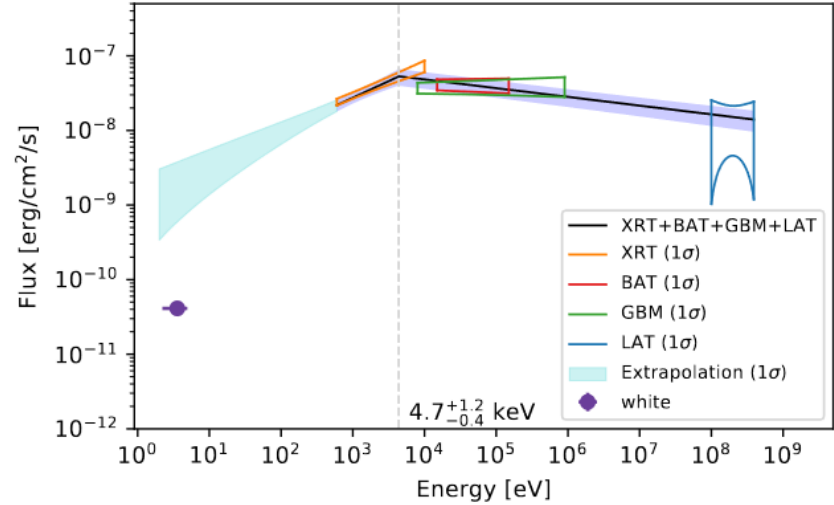
VHE GRB Workshop 2022, Berlin

Example for this talk: GRB 190114C

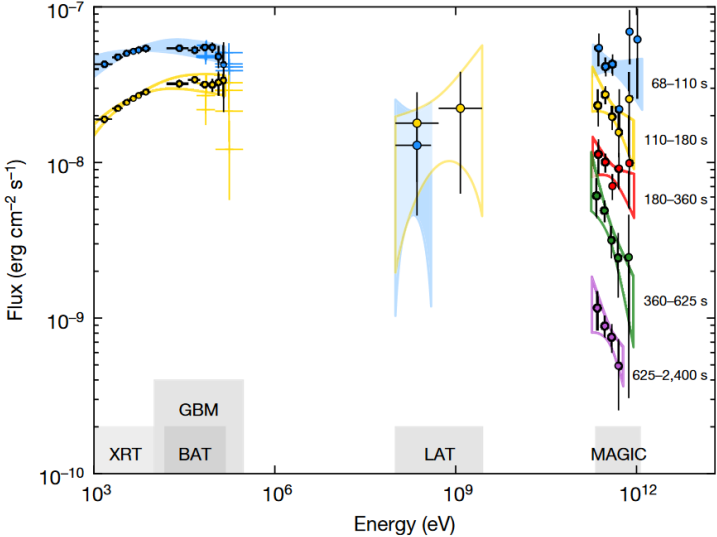
Ajello et al. 2020

$T_0 + 68 \text{ s} - 110 \text{ s}$

$T_0 + 110 \text{ s} - 180 \text{ s}$



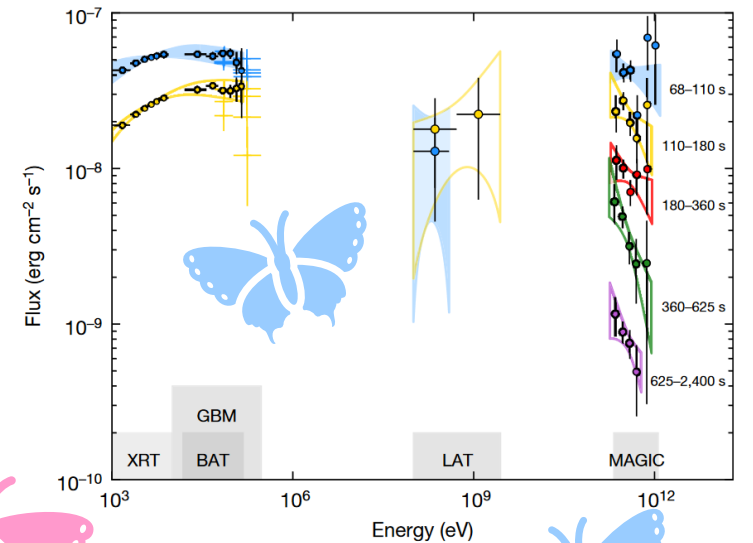
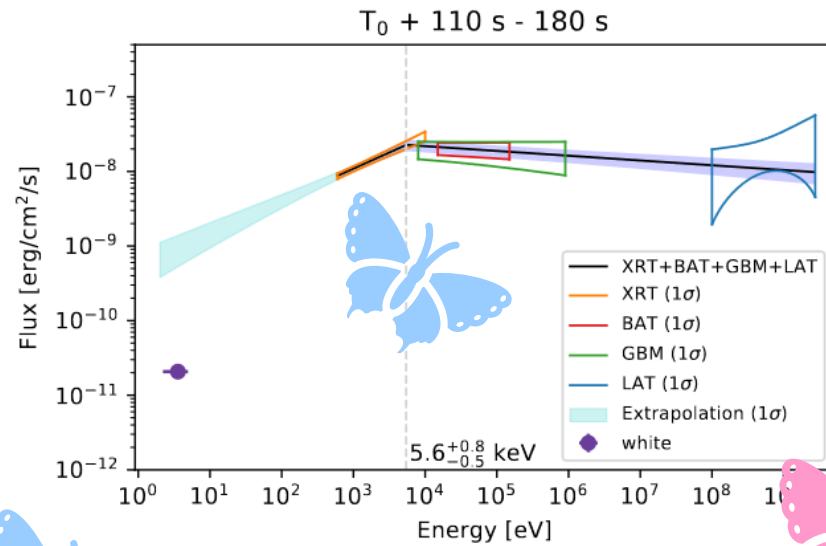
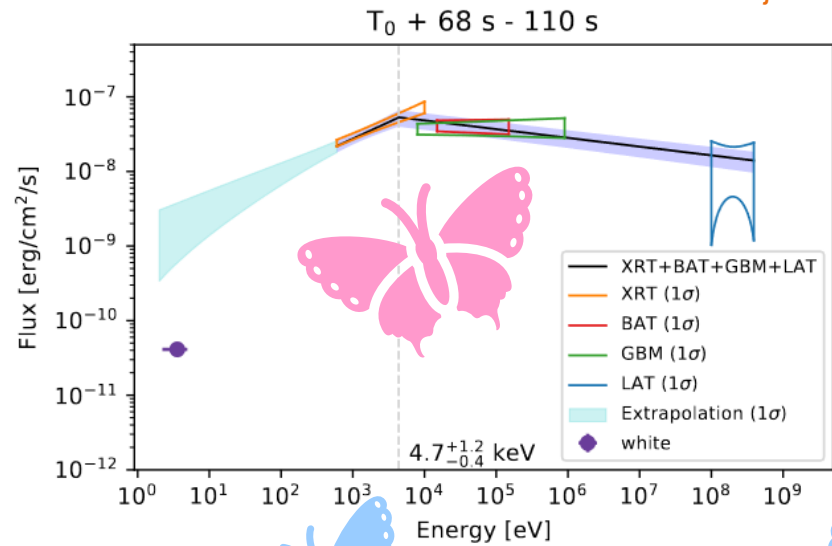
MAGIC Coll. et al. 2020



Example for this talk: GRB 190114C

Ajello et al. 2020

MAGIC Coll. et al. 2020



→ pretty to look at these, but scientific suggestiveness requires more than just pretty butterflies!

Fit ?

- Bayesian approach

→ $posterior = \frac{likelihood}{evidence} \cdot prior$

→ (sometimes log) uniform priors

→ evidence: $Z = \int d\vec{\theta} likelihood \cdot prior$

(→ likelihood averaged over parameter space weighted with priors)

- sample posterior

→ detect multiple maxima?

- model comparison via Bayes factor

→ quantitative way of measuring preference of model 1 over model 2

→ metric scale crucial

Fit ?

- Bayesian approach

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→ (sometimes log) uniform priors

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(→ likelihood averaged over parameter space weighted with priors)

We need to spend more efforts on this!

- sample posterior

→ detect multiple maxima?

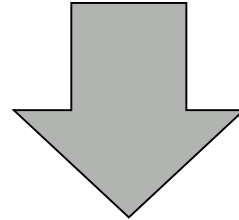
- model comparison via Bayes factor

→ quantitative way of measuring preference of model 1 over model 2

→ metric scale crucial

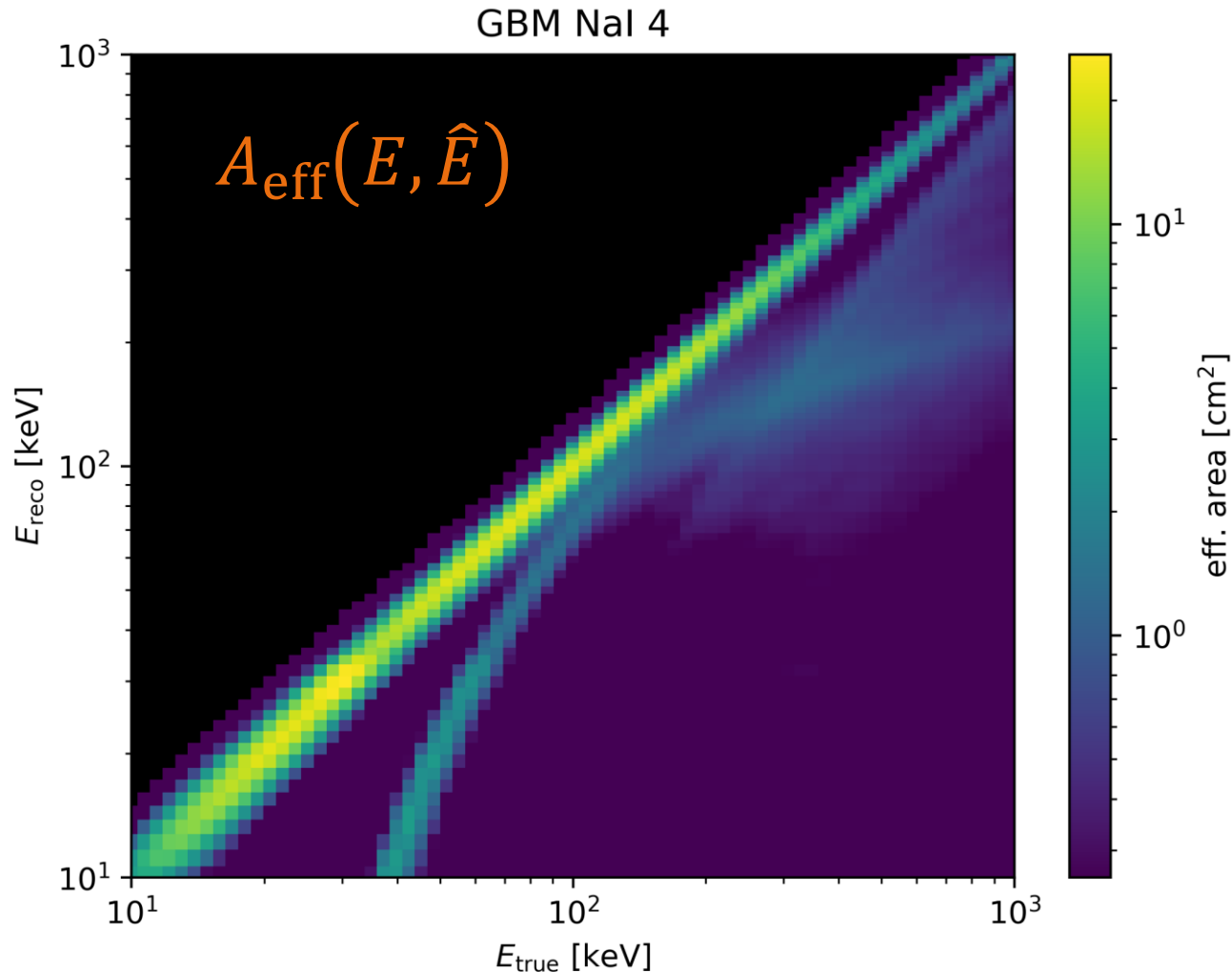
What is the task?

→ fit model to absorbed measurements of multiple detectors



$$\text{Counts rate } (E) = \int d\hat{E} \frac{dN_{\text{source}}}{dE dt dA} (\hat{E}) \exp(-\tau(\hat{E})) A_{\text{eff}}(E, \hat{E}) c_{\text{sys}}$$

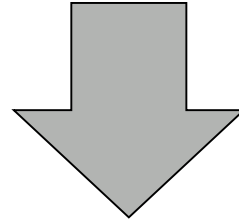
Instrument response for single detector



- detector consists of many energy channels
→ **energy dispersion**
- we cannot simply invert (unfold) this matrix
→ **forward folding**

What is the task?

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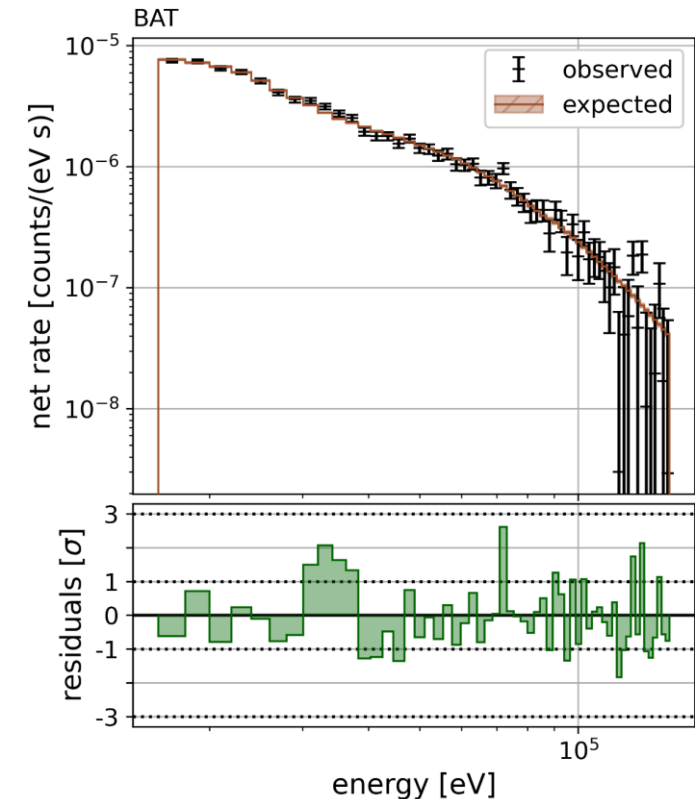
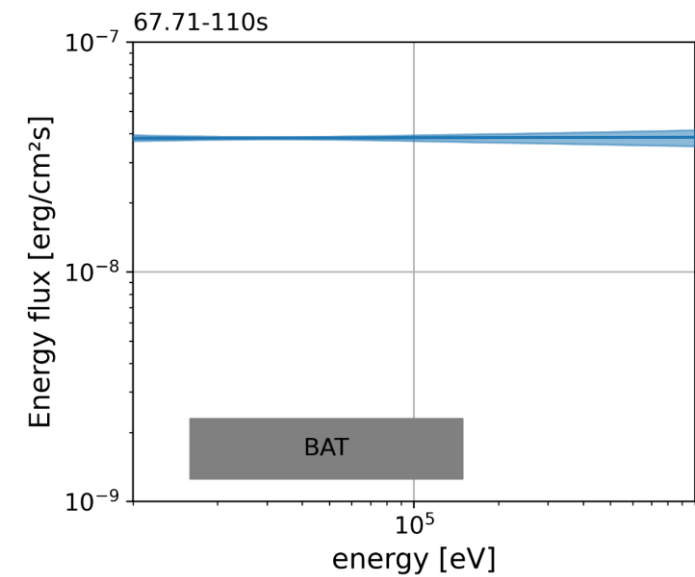
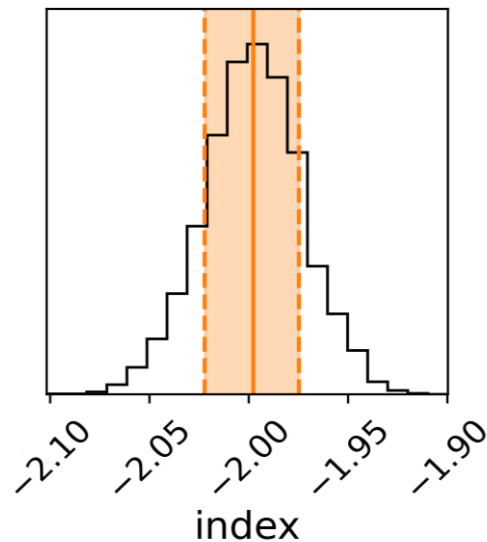
and

Background rate

**different detectors have
different statistics!**

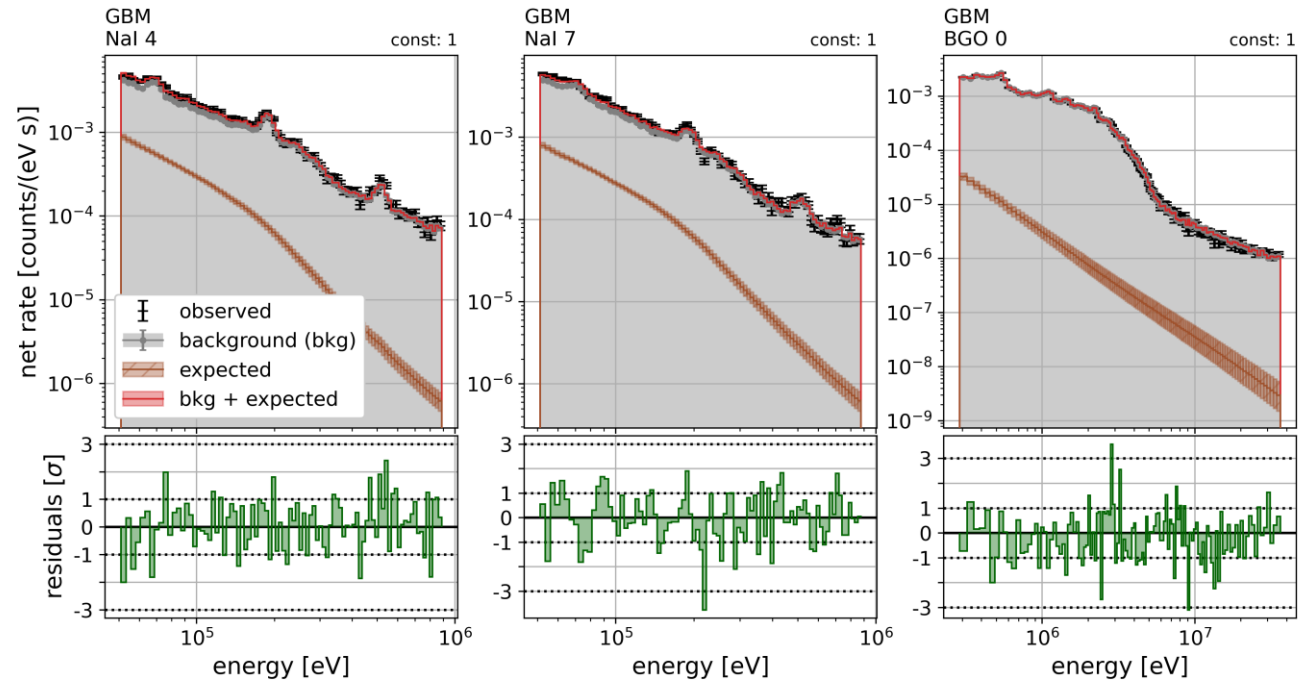
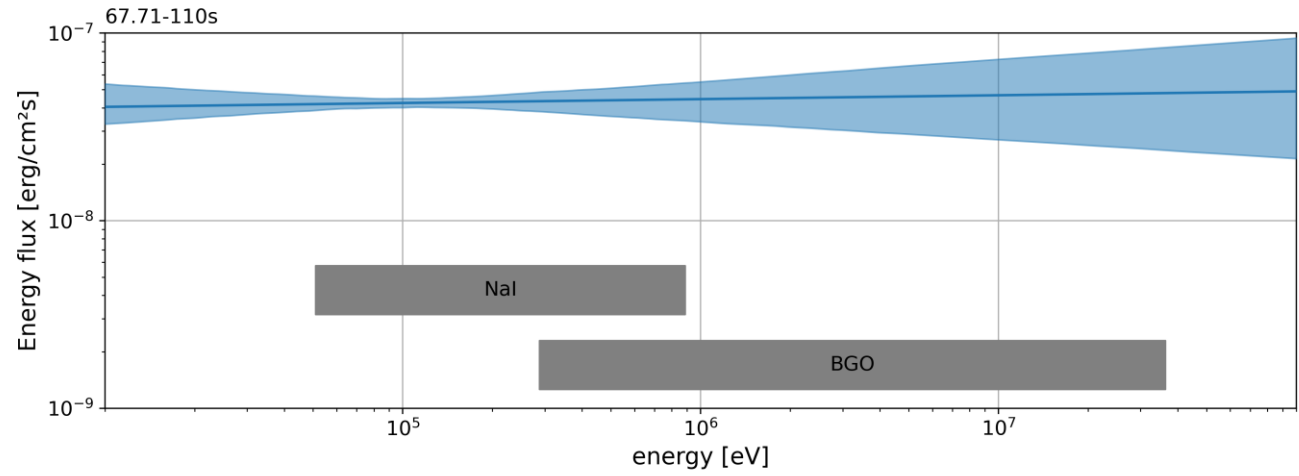
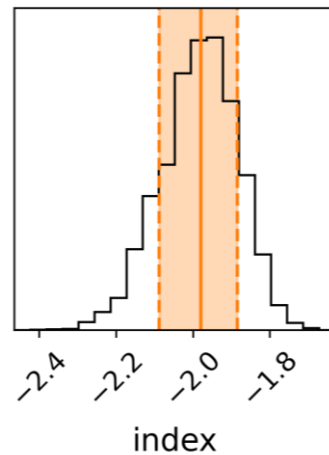
Swift BAT

- simplest instrument for us
- ON: Gaussian
- OFF: - (no background, rate fitted)
→ χ^2 (or S statistic)
- good approximation by power law:
→ index = $-1.998^{+0.023}_{-0.024}$



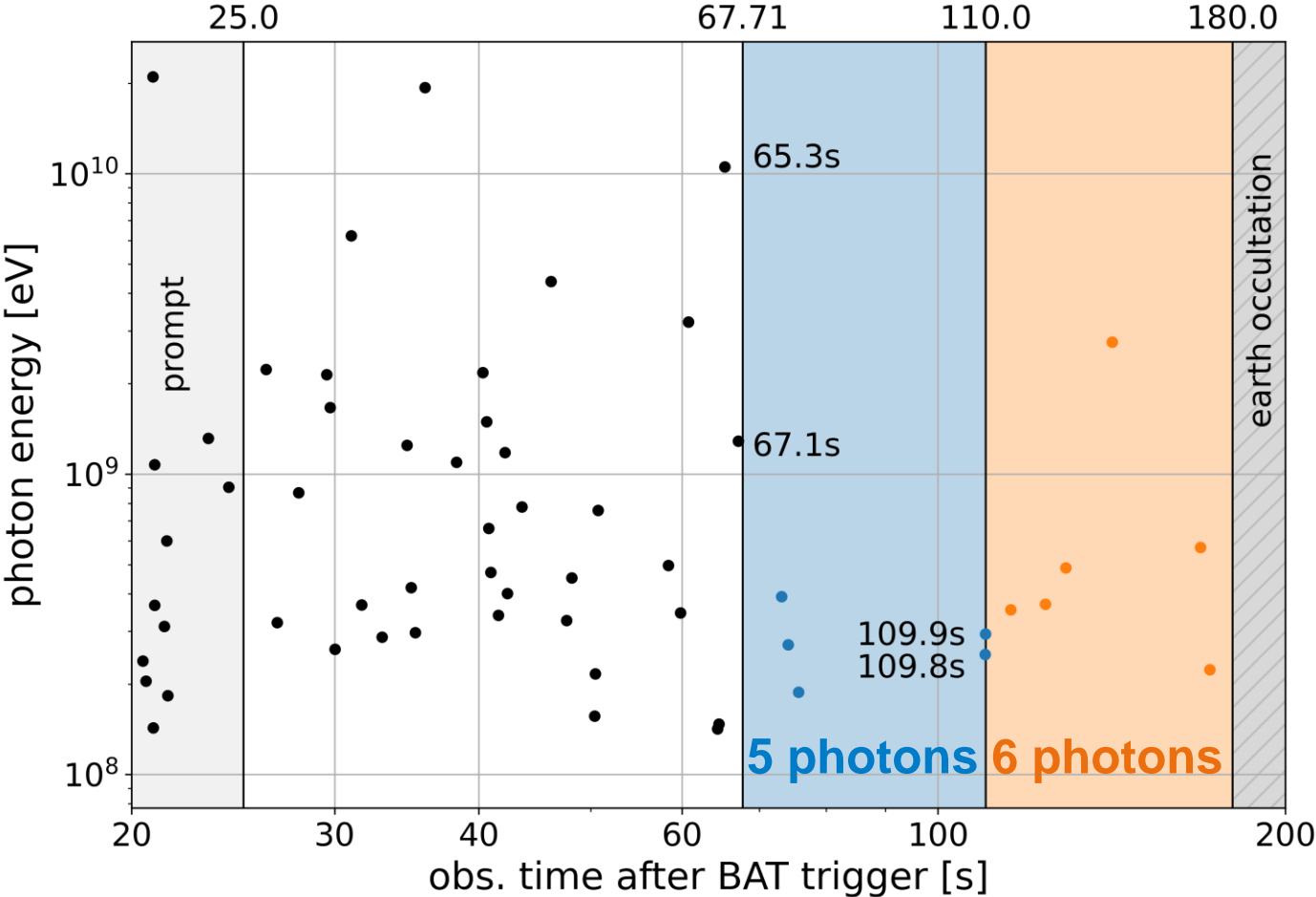
Fermi GBM

- multiple detectors (12 NaI + 2 BGO)
 - properly cross calibrated
- ON: Poisson
- OFF: Gaussian (bkg. fitted)
 - PGStat
- also flat power law
 - index = -1.98 ± 0.1



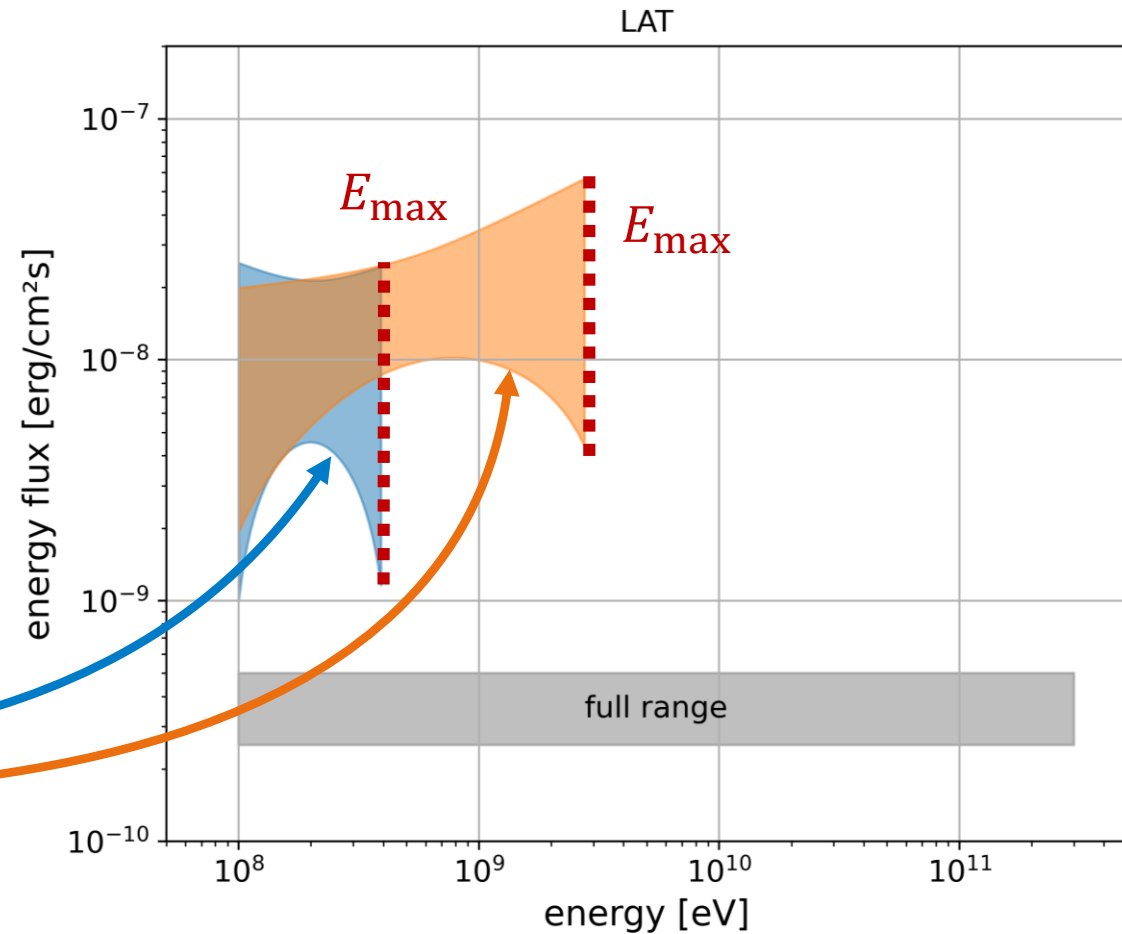
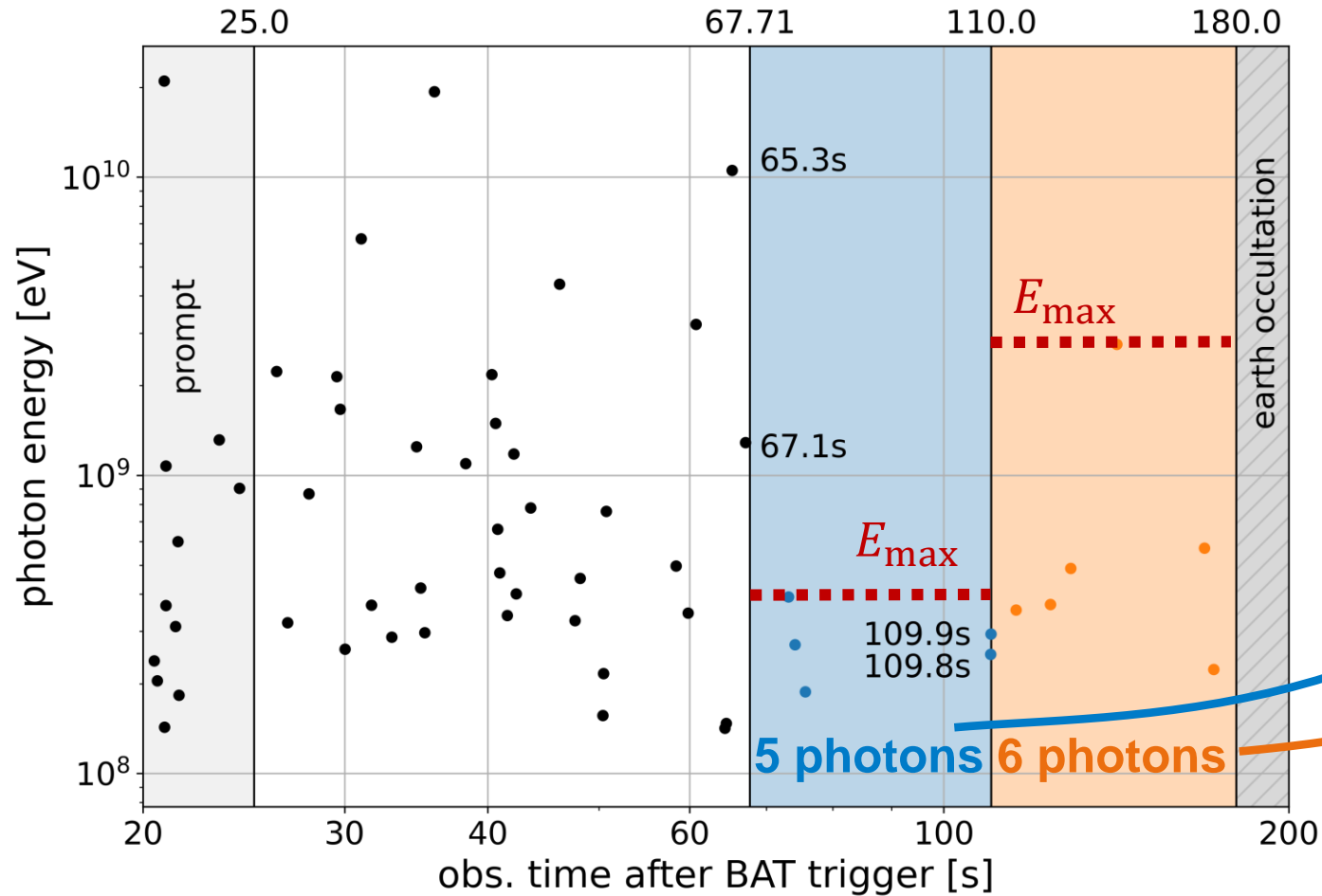
→ background dominated!

Fermi LAT



→ single photon counter

Fermi LAT

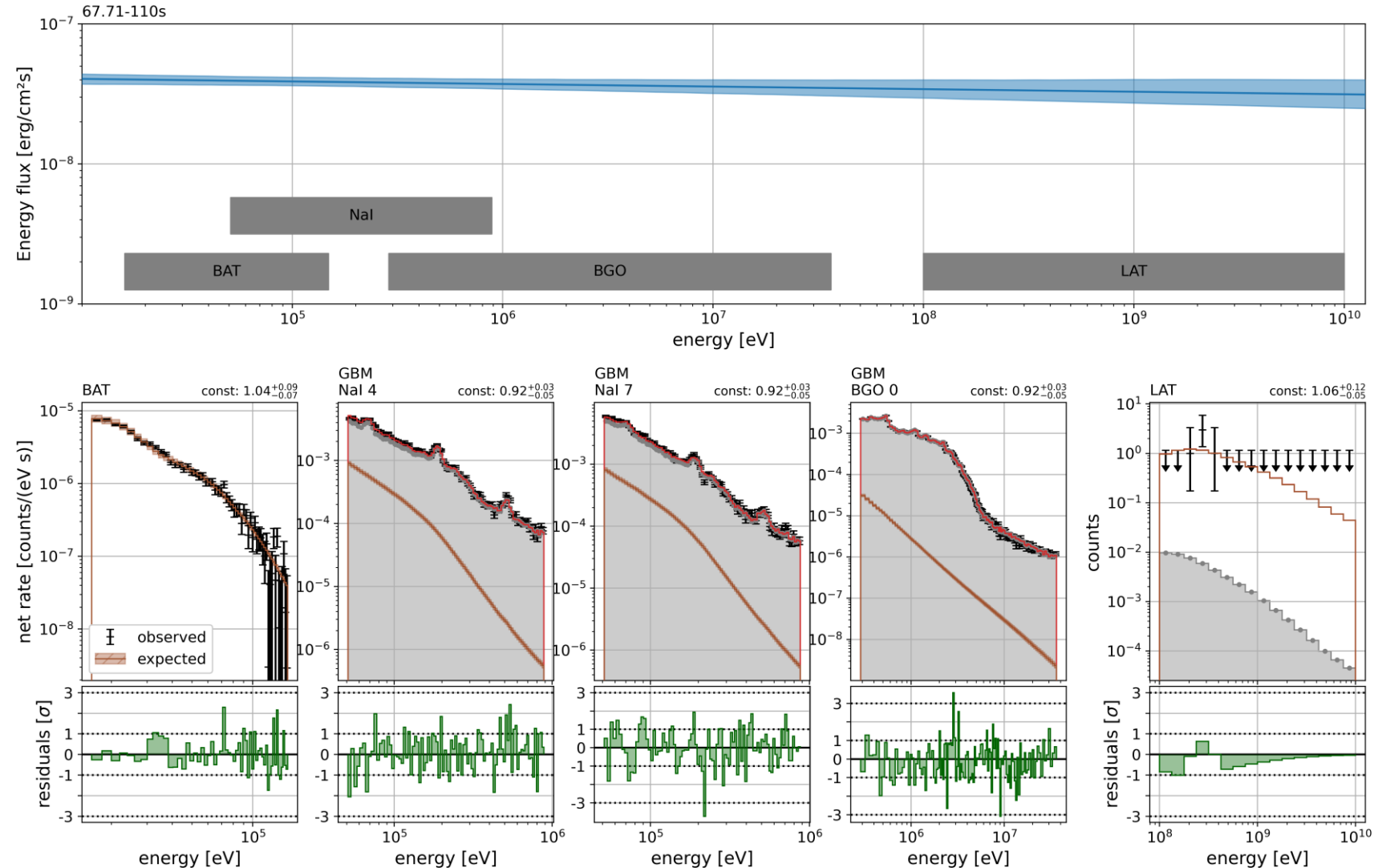


→ single photon counter

→ spectral index not really constrained

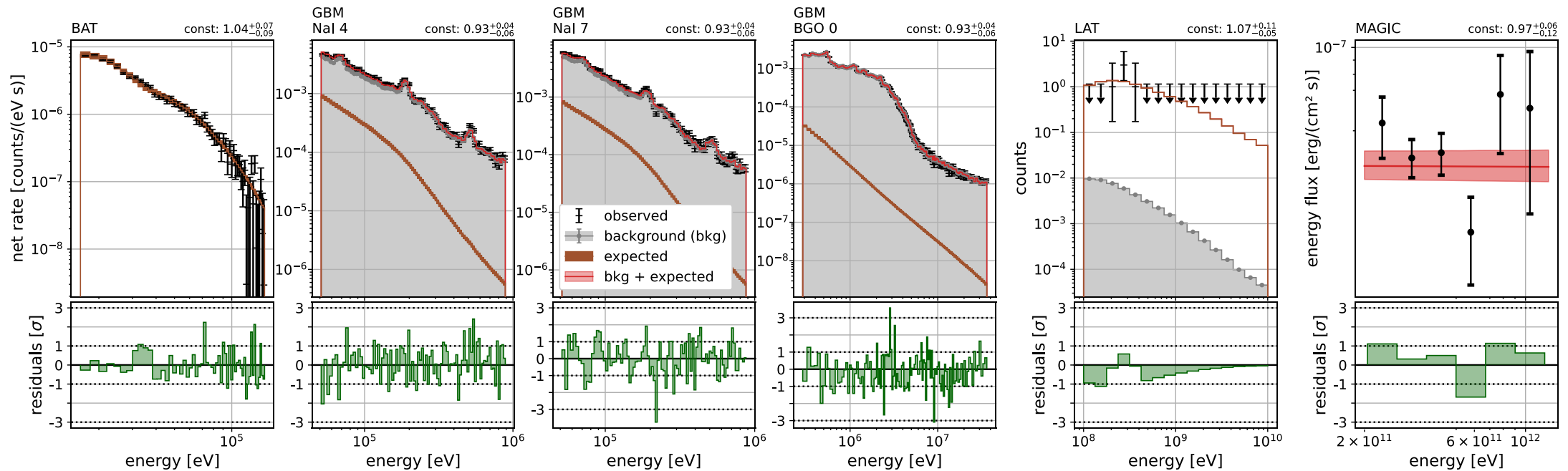
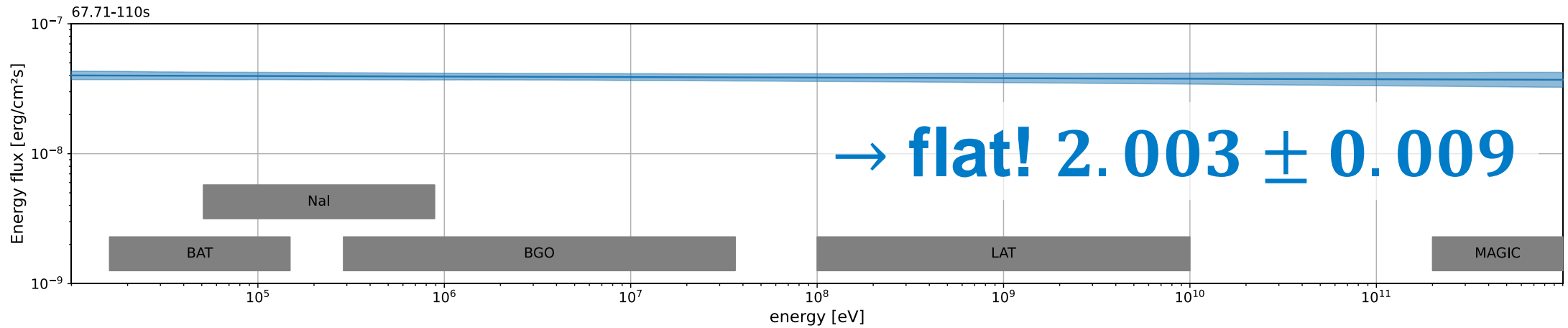
Combined BAT + GBM + LAT

- add additional cross calibration factor of $\pm 15\%$
 - non-trivial, why const?
simplest assumption



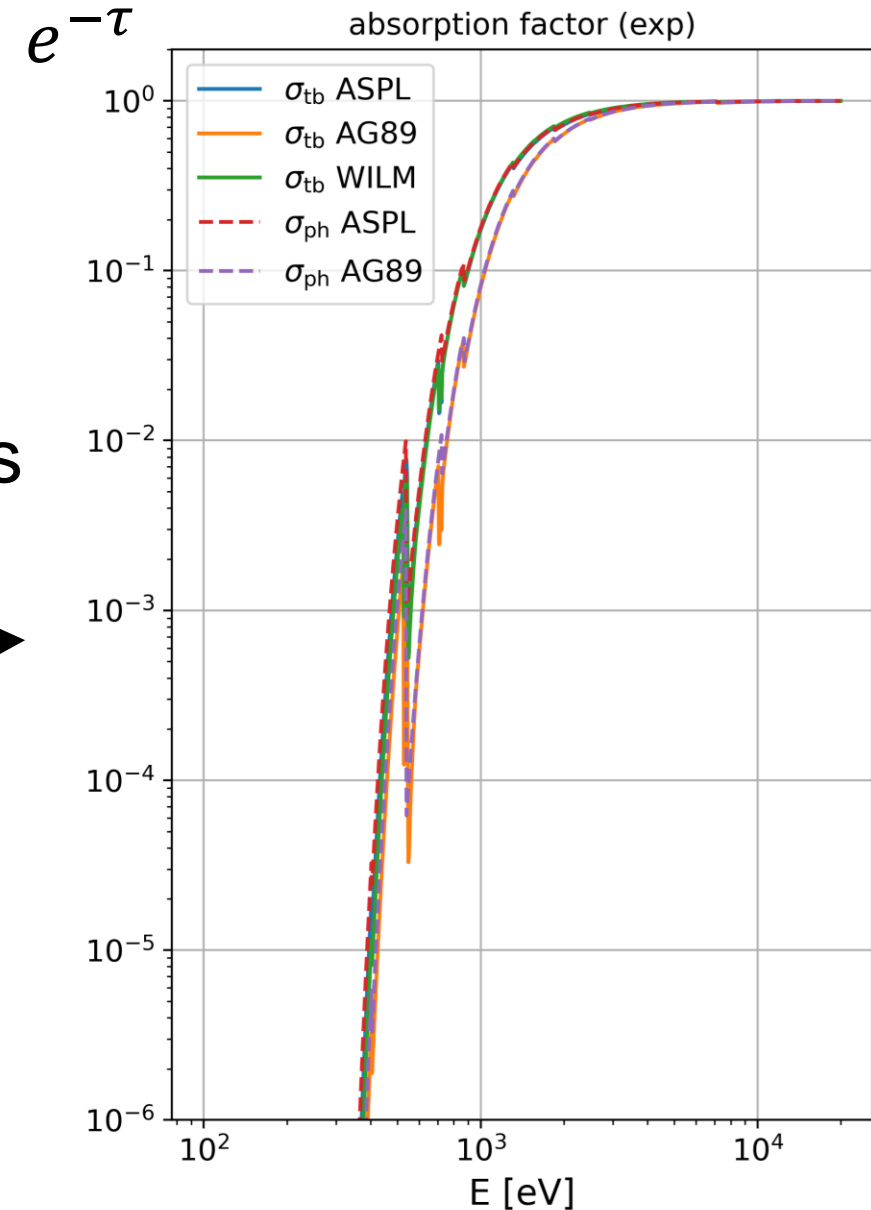
MAGIC?

→ no public IRF, only χ^2 from data points



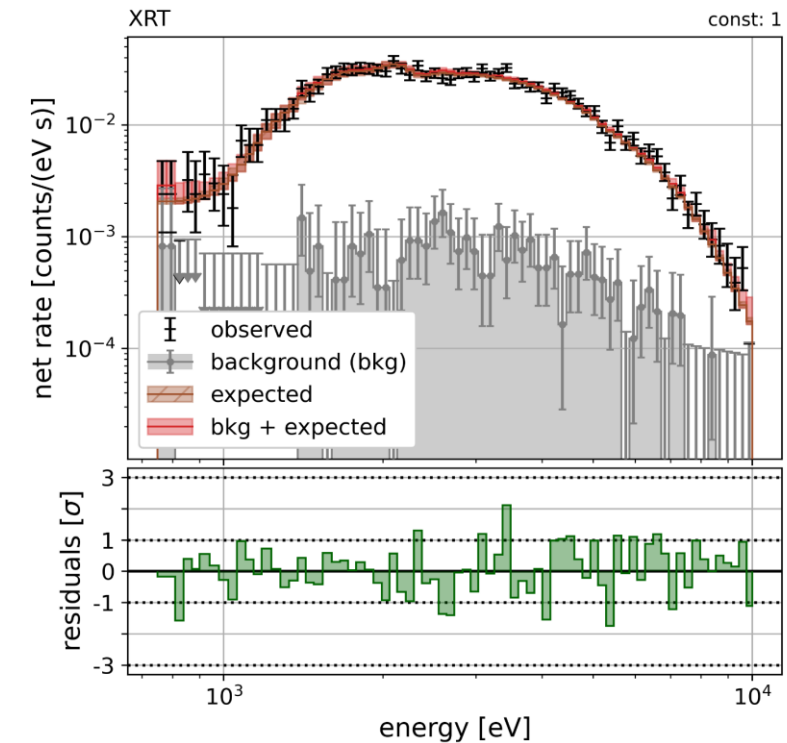
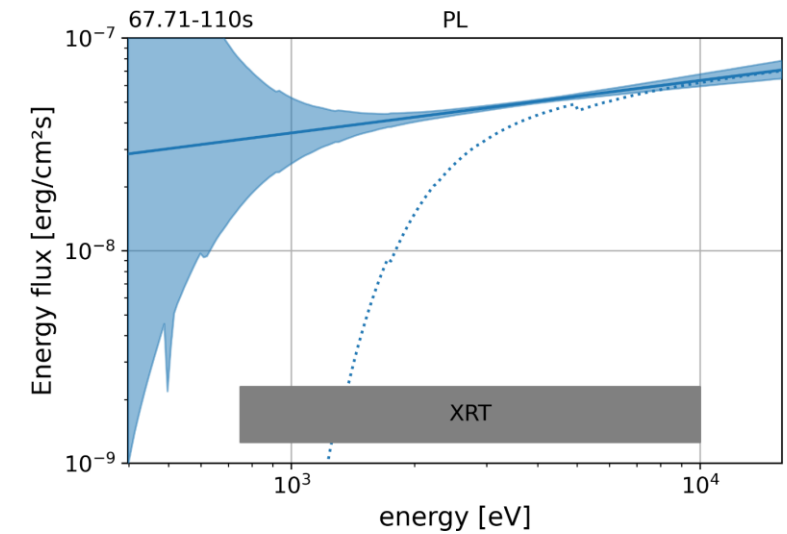
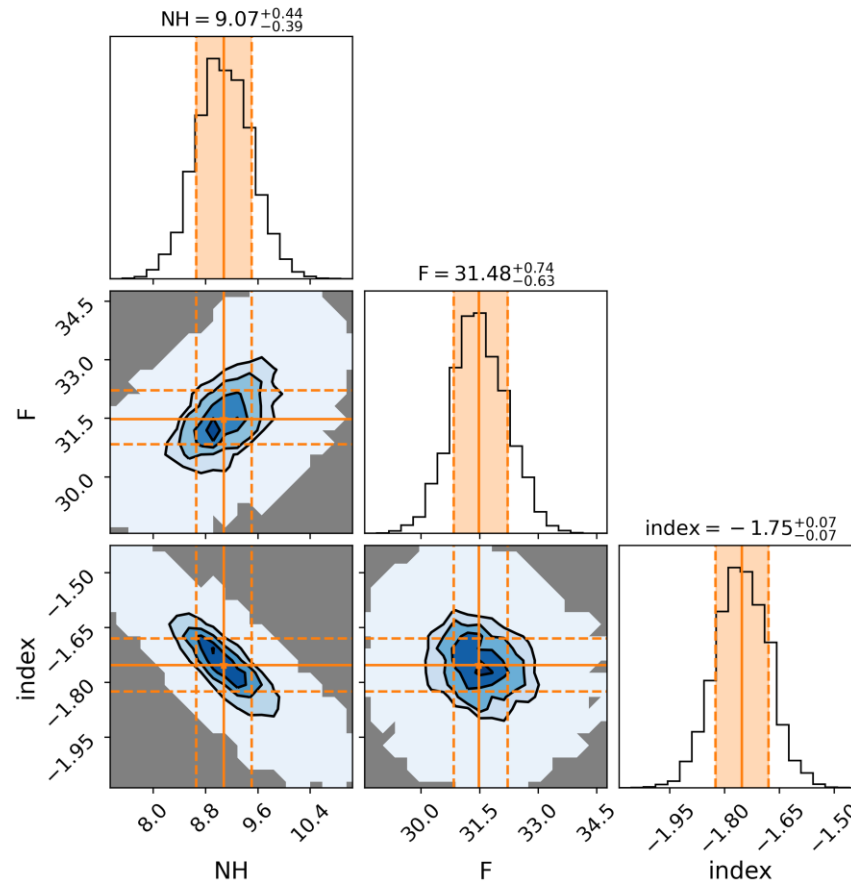
Exponential absorption

- we basically fit our box size of useful data
 - EBL at high energies
 - extinction (dust, photoelectric) at low energies
- exponential correction of orders of magnitude
- curvature
- steps in cross section introduce steps in correction
→ fit harder breaks than really in data?



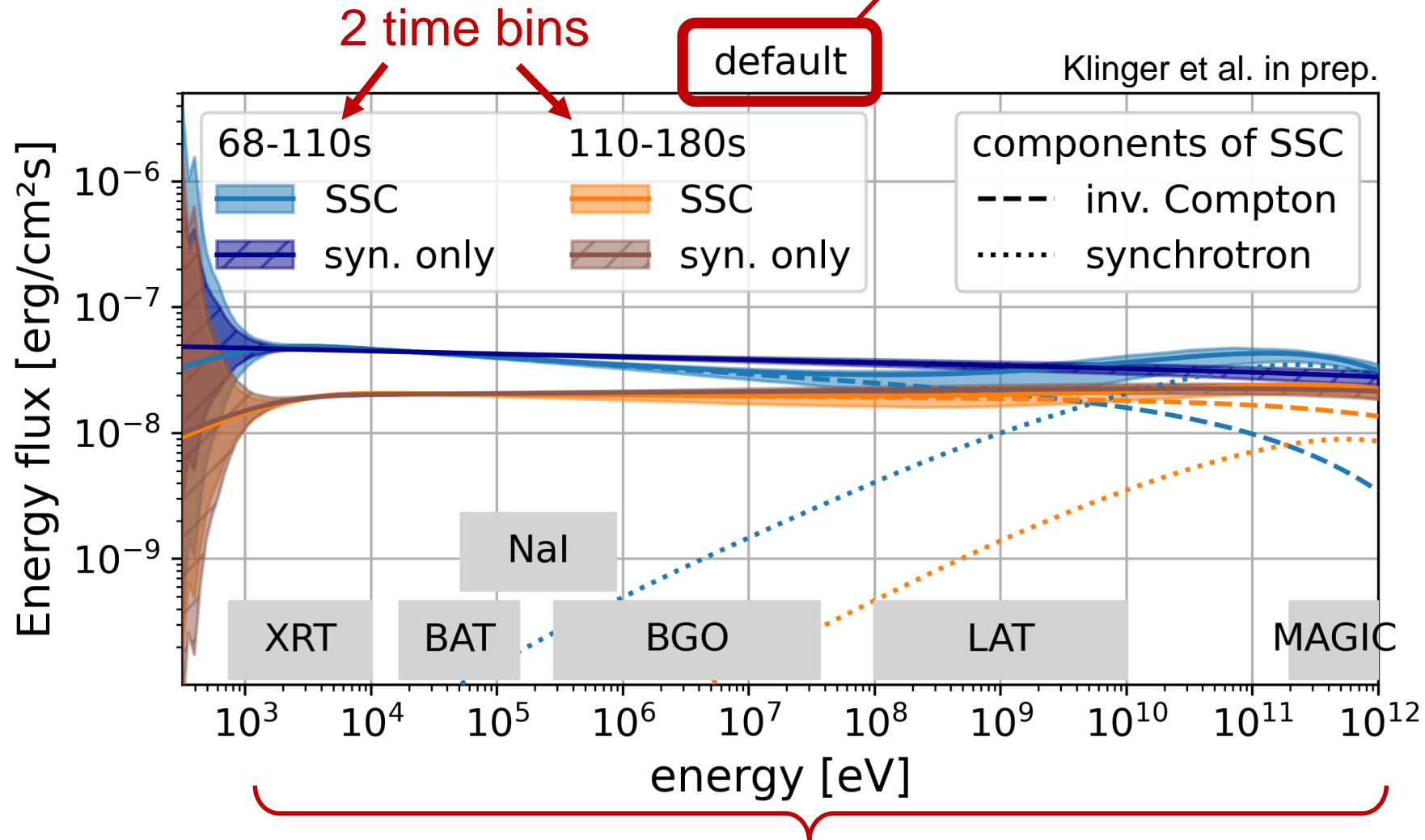
Swift XRT

- ON: Poisson
- OFF: Poisson
- CStat
- signal dominated!
- power law + abs:
- index = -1.75 ± 0.07
- break!?



Fitting a reduced SSC model

as in Ajello et al. 2020 (joint Swift+Fermi)
→ only BAT-GBM cross calibration included

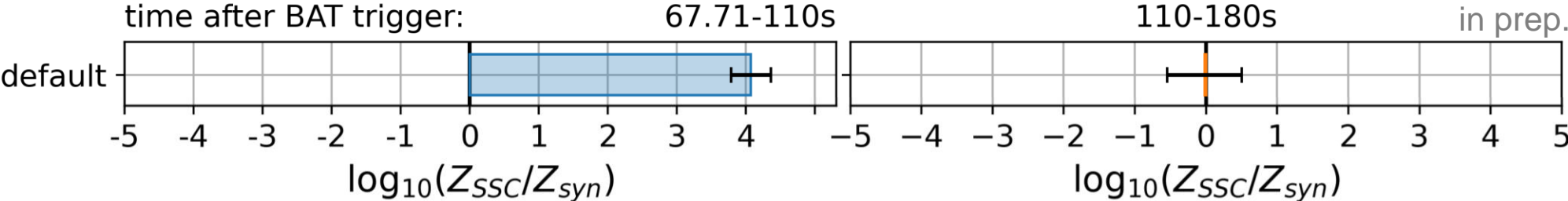


flat over 9 orders of magnitude!

Preference for new component?

Bayes factor for new component

Klinger et al.
in prep.



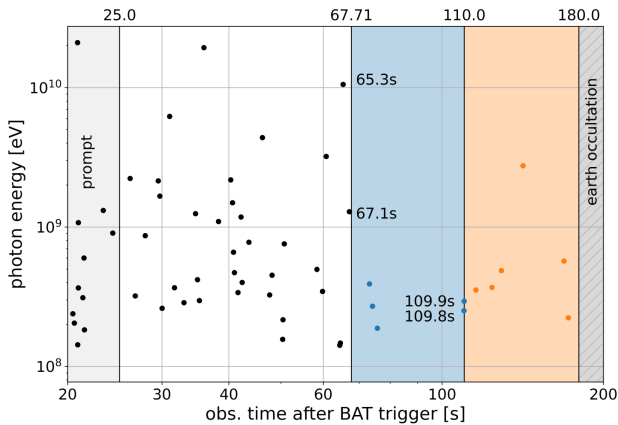
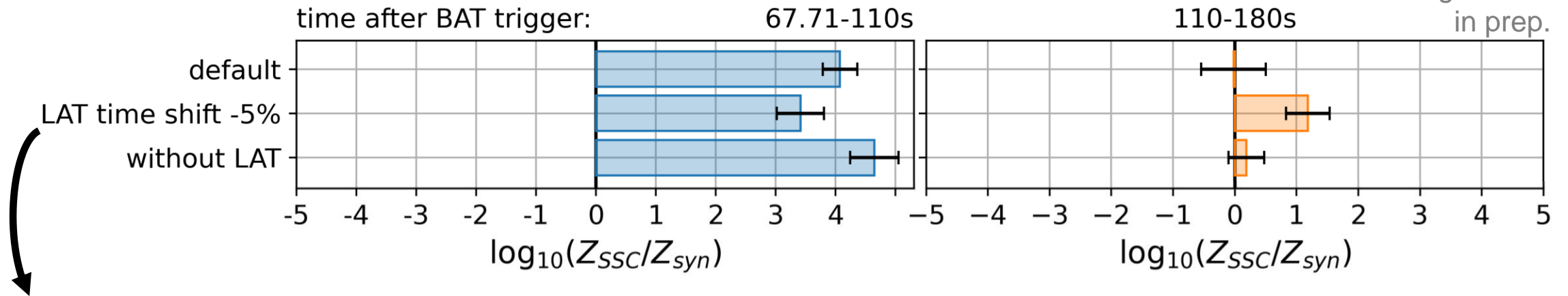
yes

no

Stability of Preference: LAT

Bayes factor for new component

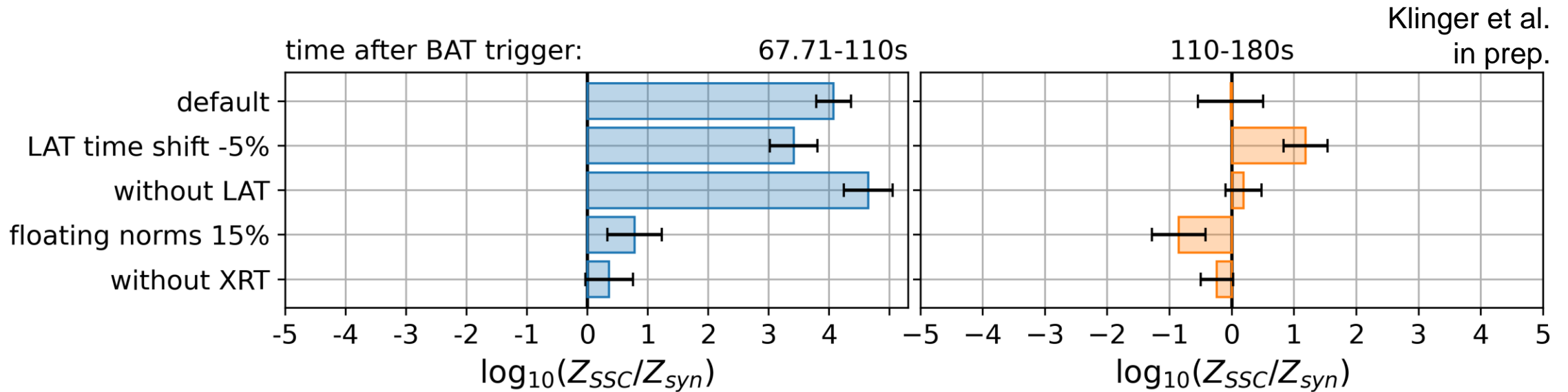
Klinger et al.
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- shift LAT time selection window by 5% (2.1s)
 - leave out LAT completely
- **LAT not very strong**

Stability of Preference: XRT

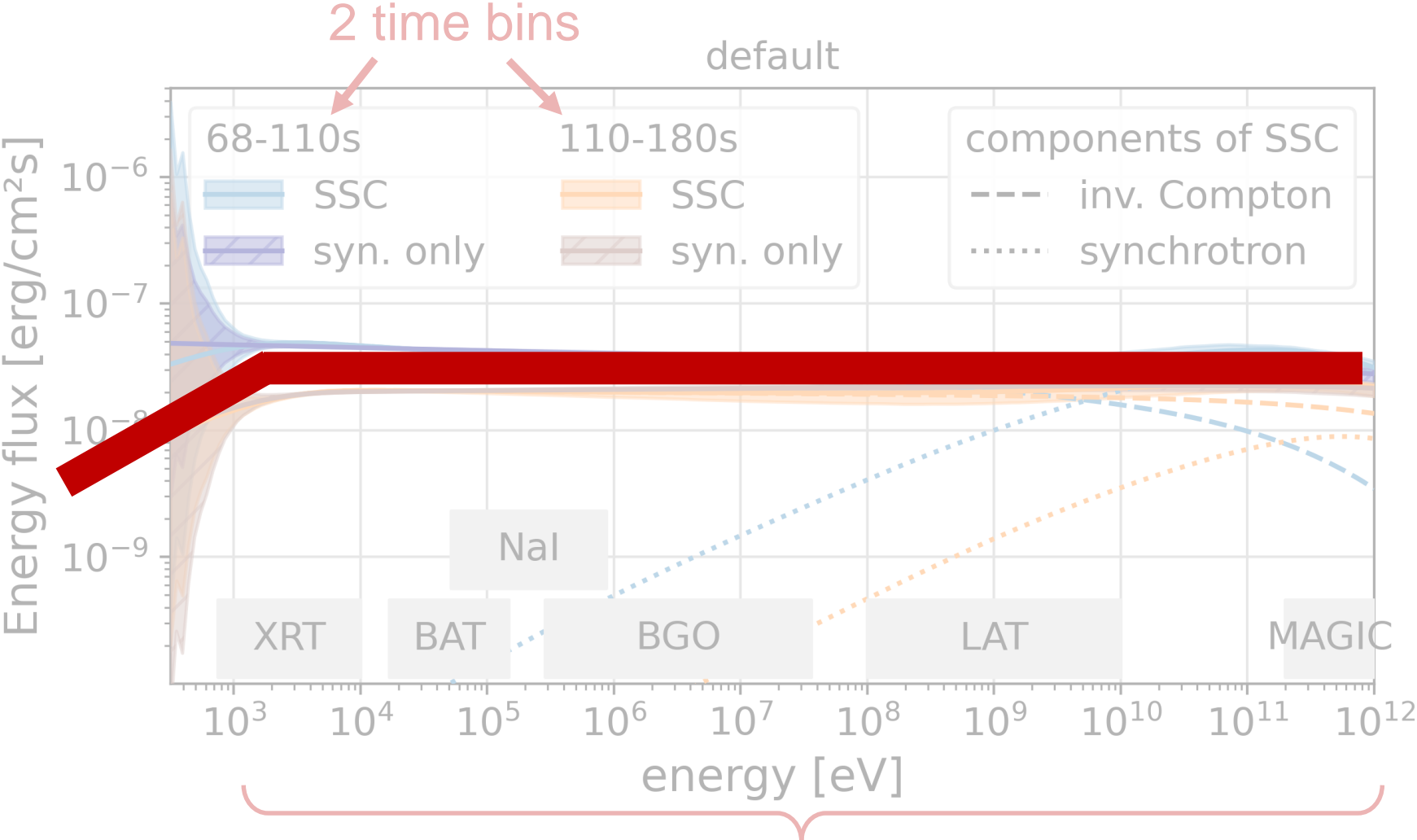
Bayes factor for new component



- systematic cross calibration uncertainty of 15% (a.k.a. floating norm or effective area correction)
- leave out XRT completely

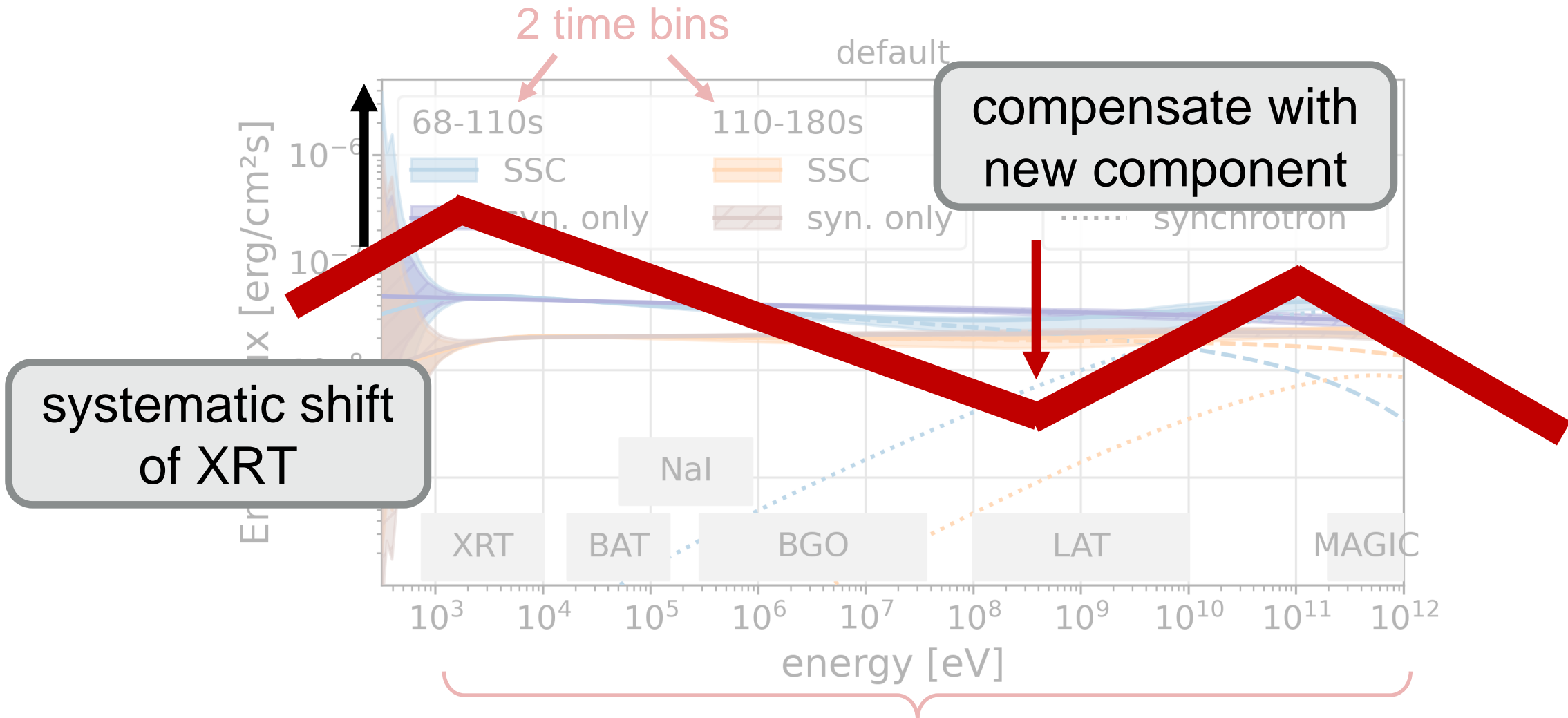
→ **XRT drives new component!**

Fitting a reduced SSC model



flat over 9 orders of magnitude!

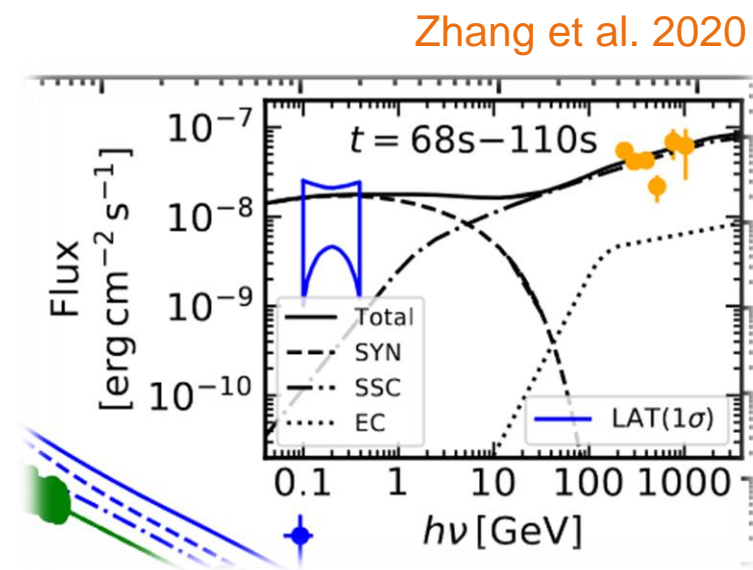
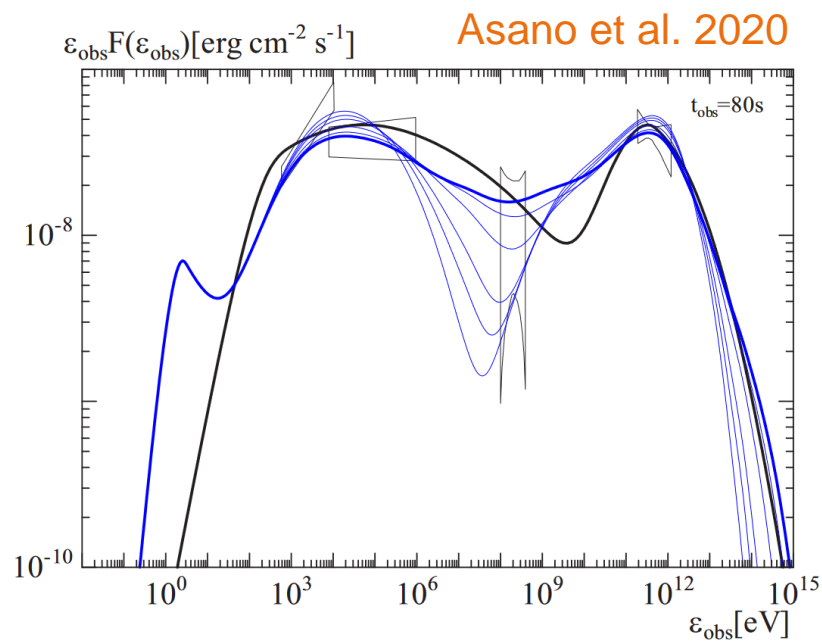
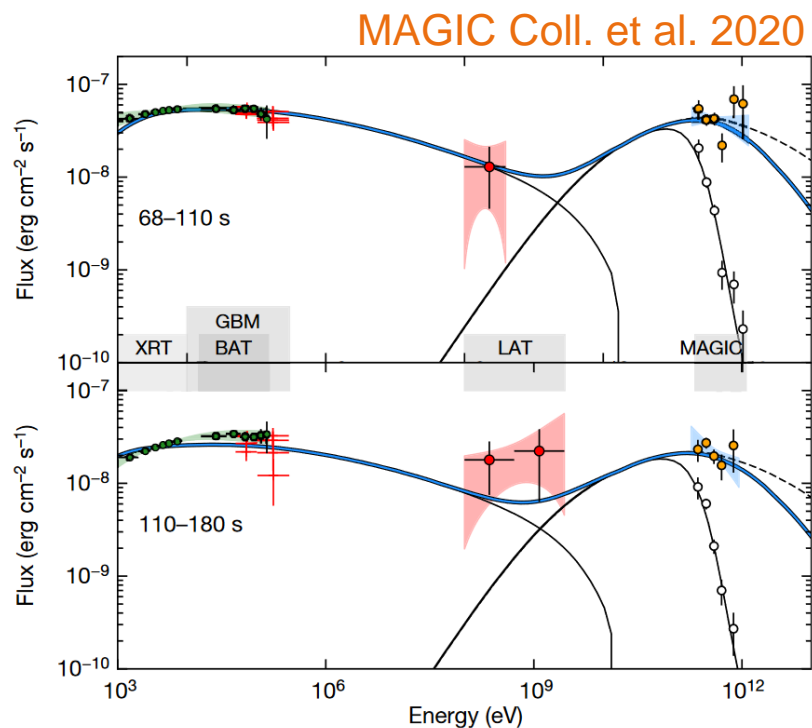
Fitting a reduced SSC model



More general remarks to stimulate discussion

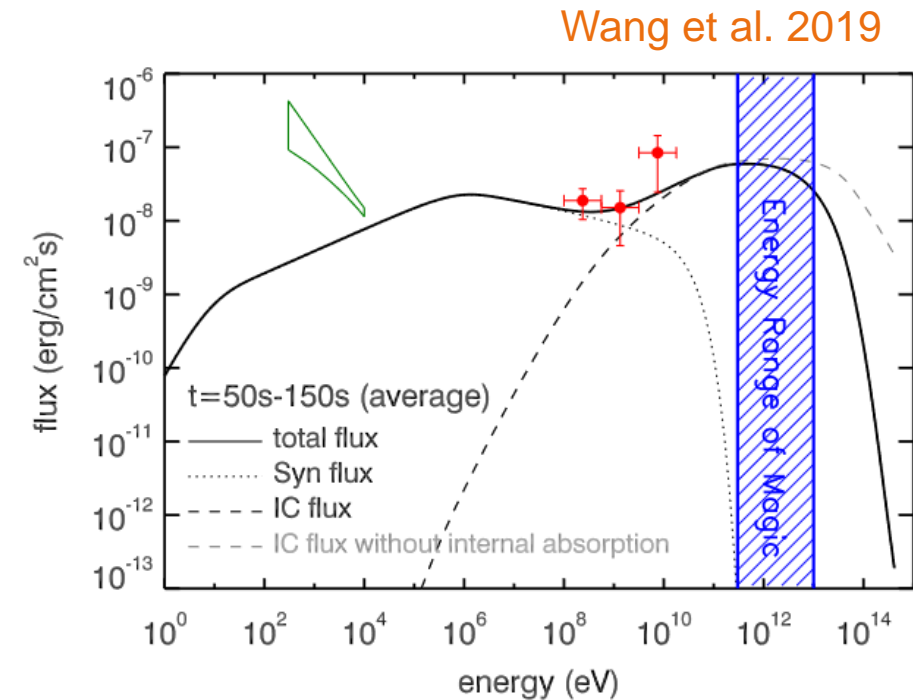
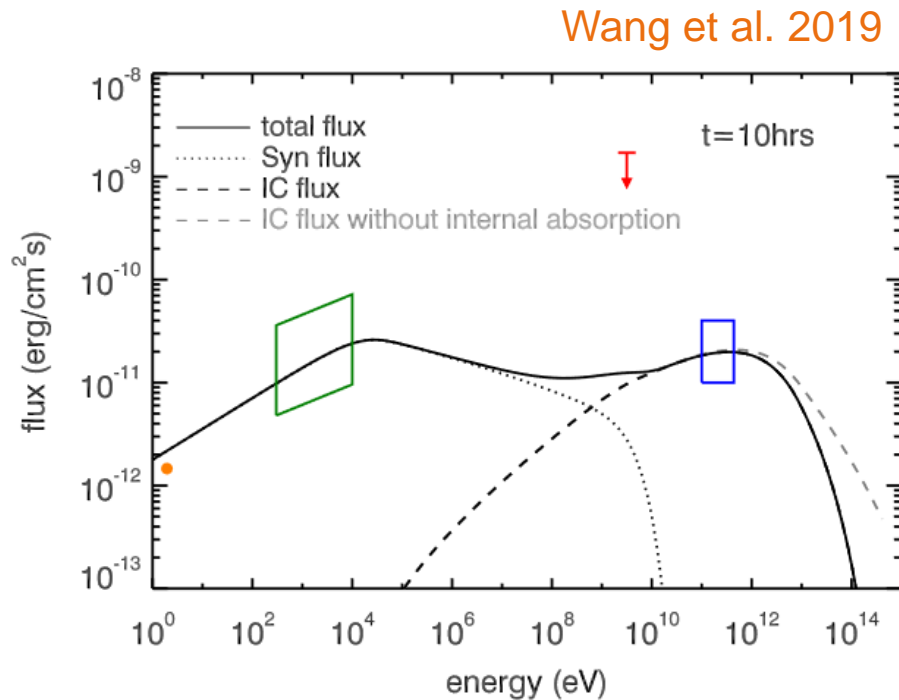
Common approaches to compare models to data

- tune parameters by hand such that they roughly can explain the data
→ no fit, thus statistically not meaningful



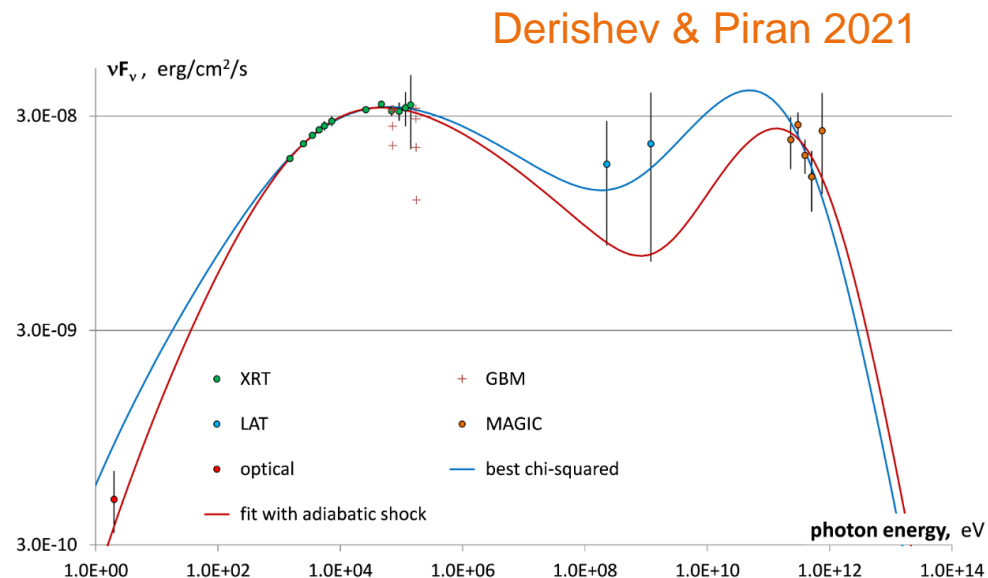
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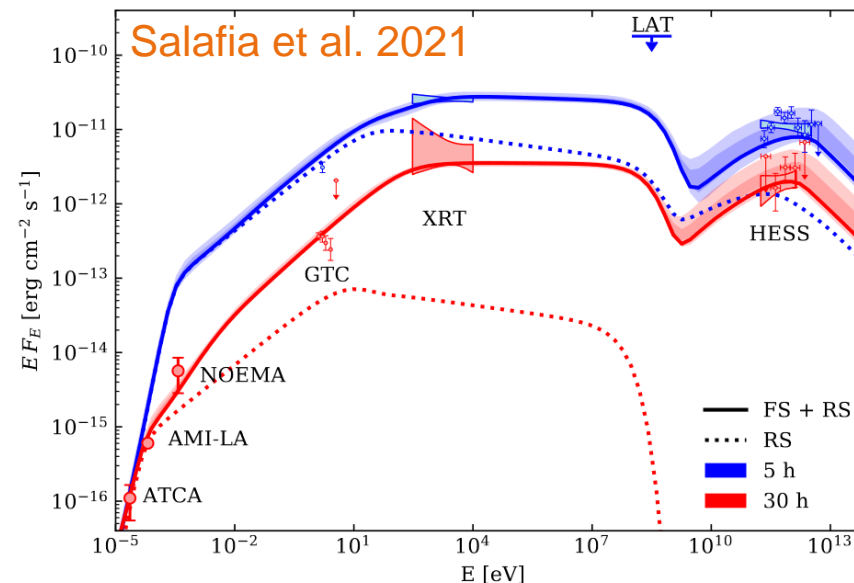
Common approaches to compare models to data

- tune parameters by hand such that they roughly can explain the data
 - no fit, thus statistically not meaningful
- take data points from publications and calculate (minimize) a χ^2
 - proper statistics? cross calibration? systematics? absorption?..
 - Why do we waste or energy to understand the instruments to ignore it in the fit?



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 - Why do we waste or energy to understand the instruments to ignore it in the fit?
- integrate an entire instrument to a flux and a slope and include this in the total likelihood

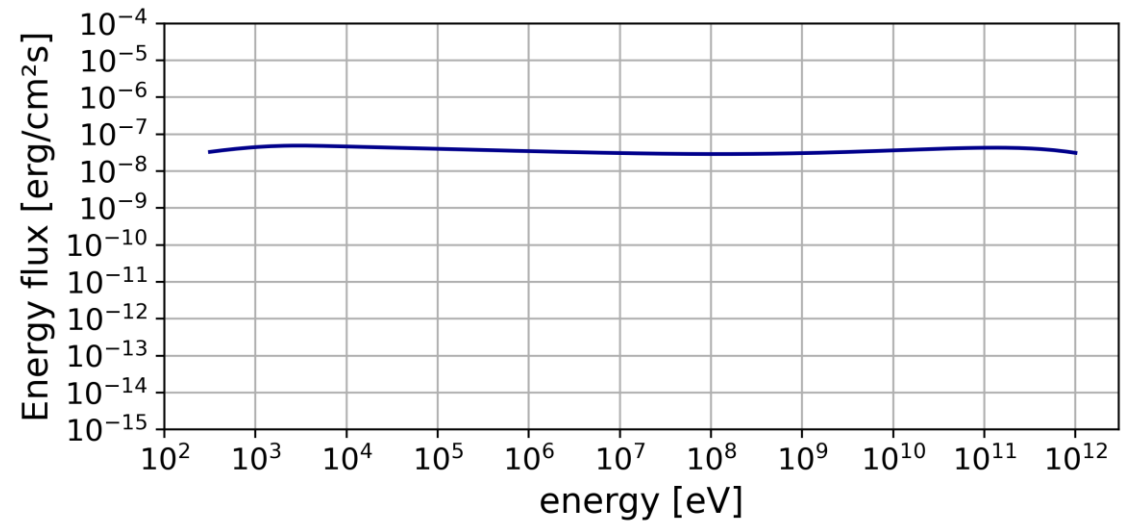
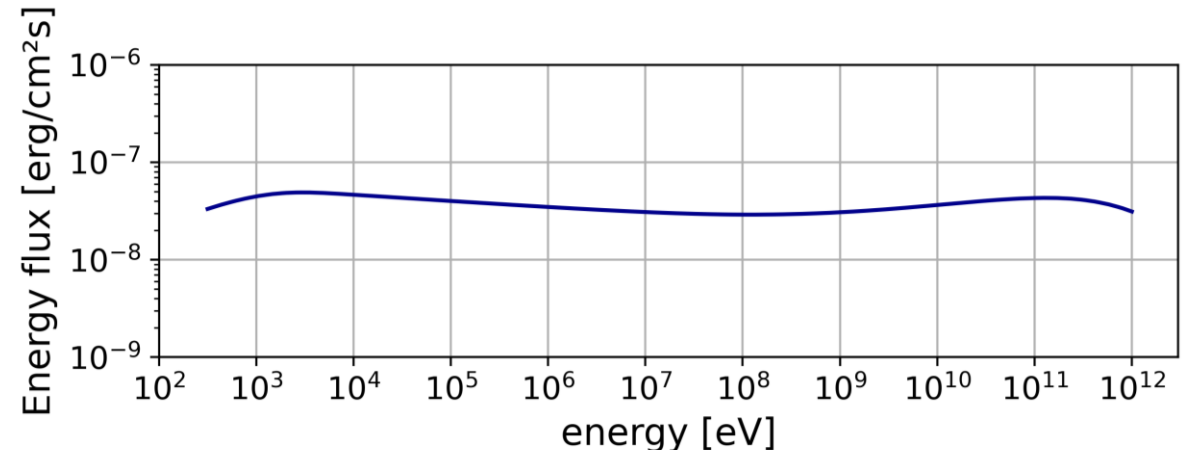
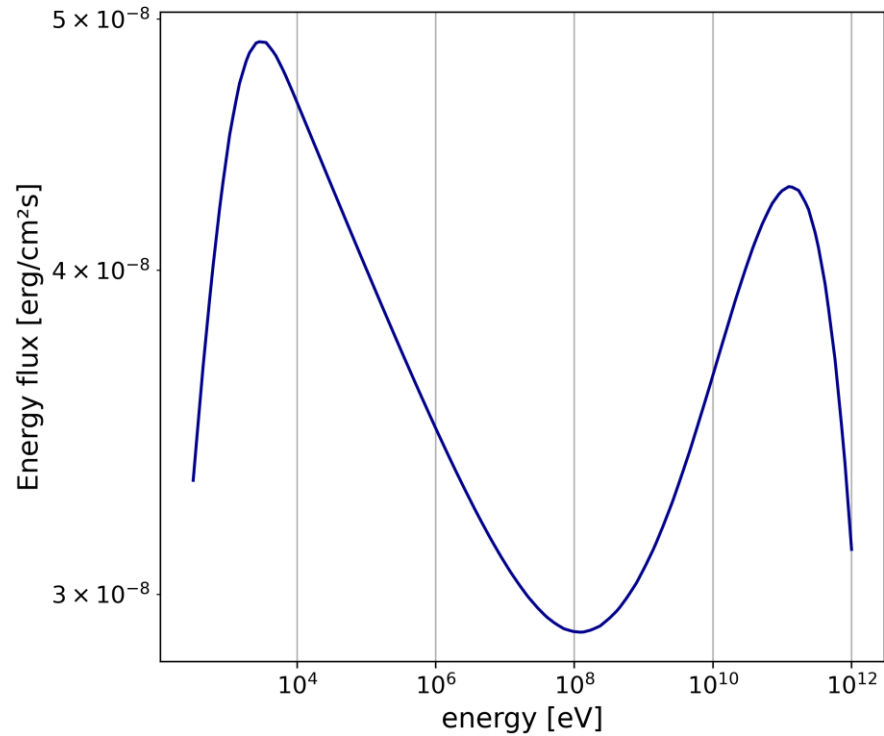


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- tune parameters by hand such that they roughly can explain the data
 - no fit, thus statistically not meaningful
- take data points from publications and calculate (minimize) a χ^2
 - proper statistics? cross calibration? systematics? absorption?..
 - Why do we waste or energy to understand the instruments to ignore it in the fit?
- integrate an entire instrument to a flux and a slope and include this in the total likelihood
- include 1 or 2 instruments

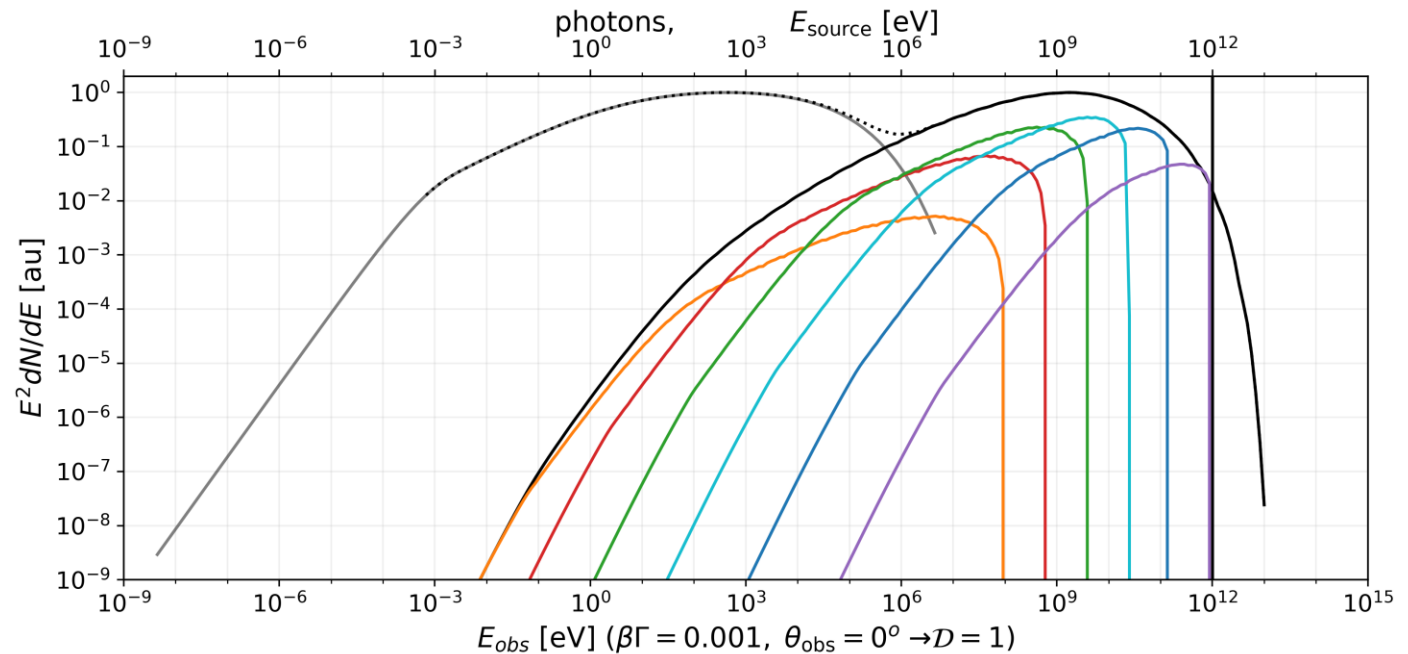
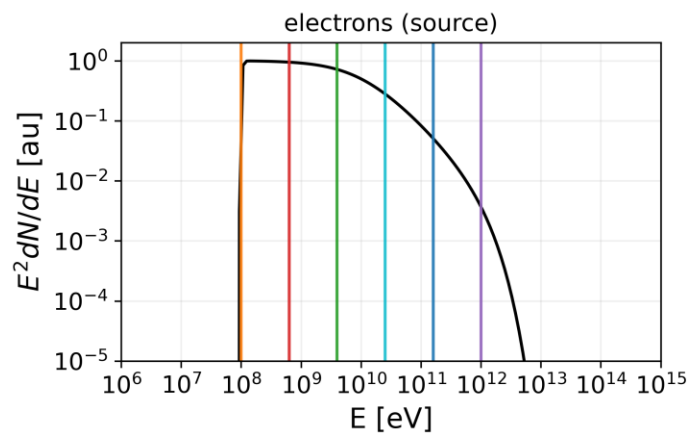
Reminder

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- we don't expect a bunch of power laws
 - power laws are good for intuition, but not for comparison to data
 - kernels are smooth, observations are the result of several convolutions!



Reminder

- aspect ratio makes new components
- we don't expect a bunch of power laws
 - power laws are good for intuition, but not for comparison to data
 - kernels are smooth, observations are the result of several convolutions!
- open source software for proper fitting is already there
 - Multi-Mission Maximum Likelihood framework (3ML, <https://threeml.readthedocs.io/en/stable/index.html#>)
 - Gammapy (<https://gammapy.org/>)